

Terramechanics IV

- Defeating the dreaded bulldozing!
- Getting muddled in drawbar pull!
- Asking an expert! (virtually...)
- Note - these are the slides I would have shown yesterday (141120) had they been available at the time. I am making minor revisions (e.g., making sure the nomenclature is consistent) and plan to post an “all singing, all dancing guide to terramechanics” shortly, but this should get you through the problem set. Sorry about the confusion...



Compaction Resistance, $n=1$

$$R_c = \frac{1}{2}(k_c + bk_\phi)z^2$$

$$R_c = 56.92 \text{ N (per side)} \implies$$

$$R_c = 113.8 \text{ N}$$



Or, You Could Cheat...

Approximation formulas for $n=1$

Two wheels in tandem

$$R_c = \frac{1.7}{2} (k_c + bk_\phi) z^2$$

Three wheels in tandem

$$R_c = \frac{2.3}{2} (k_c + bk_\phi) z^2$$

z is the sinkage depth of the front wheel in both cases

R_g, R_f are straightforward



Bulldozing Resistance

General case:

All angles in radians!

$$R_b = \frac{b \sin(\alpha + \phi)}{2 \sin \alpha \cos \phi} (2zcK_c + \gamma z^2 K_\gamma) + \frac{\ell_o^3 \gamma}{3} \left(\frac{\pi}{2} - \phi \right) + c\ell_o^2 \left[1 + \tan \left(\frac{\pi}{4} + \frac{\phi}{2} \right) \right]$$
$$\ell_o = z \tan^2 \left(\frac{\pi}{4} - \frac{\phi}{2} \right)$$

$\ell_o \equiv$ soil disruption depth, and is *not* the same as contact length ℓ

For tracked vehicles, only the first term applies:

$$R_b = \frac{b \sin(\alpha + \phi)}{2 \sin \alpha \cos \phi} (2zcK_c + \gamma z^2 K_\gamma)$$



Bulldozing Resistance (Rb)

| Symbol | Description | Value |
|-----------------------|---|---|
| ϕ | Angle of internal friction | 30-40 degrees for Lunar Regolith |
| γ | Soil density | 1.6 gm 0.002595 N/cm |
| C_0 | Cohesive strength of soil | 0.017 |
| L_0 (degrees) | Distance of rupture | $l_0 = z \tan^2 \left(45^\circ - \frac{\phi}{2} \right)$ |
| K_c (degrees) | Modulus of cohesion of soil deformation | $k_c = (N_c - \tan(\phi))(\cos^2(\phi))$ |
| K (degrees) | Modulus of density of soil deformation | $K_v = \left(\frac{2N_v}{\tan \phi} + 1 \right) \cos^2(\phi)$ |
| N_c (radians) | Coefficient of passive earth pressure | $N_c = \cot(\phi) \left(\frac{e^{2\left(\frac{3\pi}{4} - \frac{\phi}{2}\right) \tan(\phi)}}{2 \cos^2 \left(\frac{\pi}{4} + \frac{\phi}{2} \right)} - 1 \right)$ |
| α (degrees) | Angle of approach of the wheel | $\alpha = \cos^{-1} \left(1 - \frac{2z}{D} \right)$ |



Bulldozing Example (1)

$$\phi = 33^\circ = 0.576 \text{ rad}$$

$$\alpha = \cos^{-1} \left(1 - \frac{2z}{d} \right) = \cos^{-1} \left(1 - \frac{2(1.812)}{81.2} \right) = 17.18^\circ = 0.2999 \text{ rad}$$

$$\ell_o = z_1 \tan^2 \left(\frac{\pi}{2} - \frac{\phi}{4} \right) = 0.5341$$

$$N_q = \frac{e^{(1.5\pi - \phi) \tan \phi}}{2 \cos^2 \left(\frac{\pi}{4} + \frac{\phi}{2} \right)} = 32.23$$

$$N_c = \frac{N_q - 1}{\tan \phi} = 40.09$$



Bulldozing Example (2)

$$N_{\gamma} = \frac{2(N_q + 1) \tan \phi}{1 + 0.4 \sin 4\phi} = 33.27$$

$$K_c = (N_c - \tan \phi) \cos^2 \phi = 33.37$$

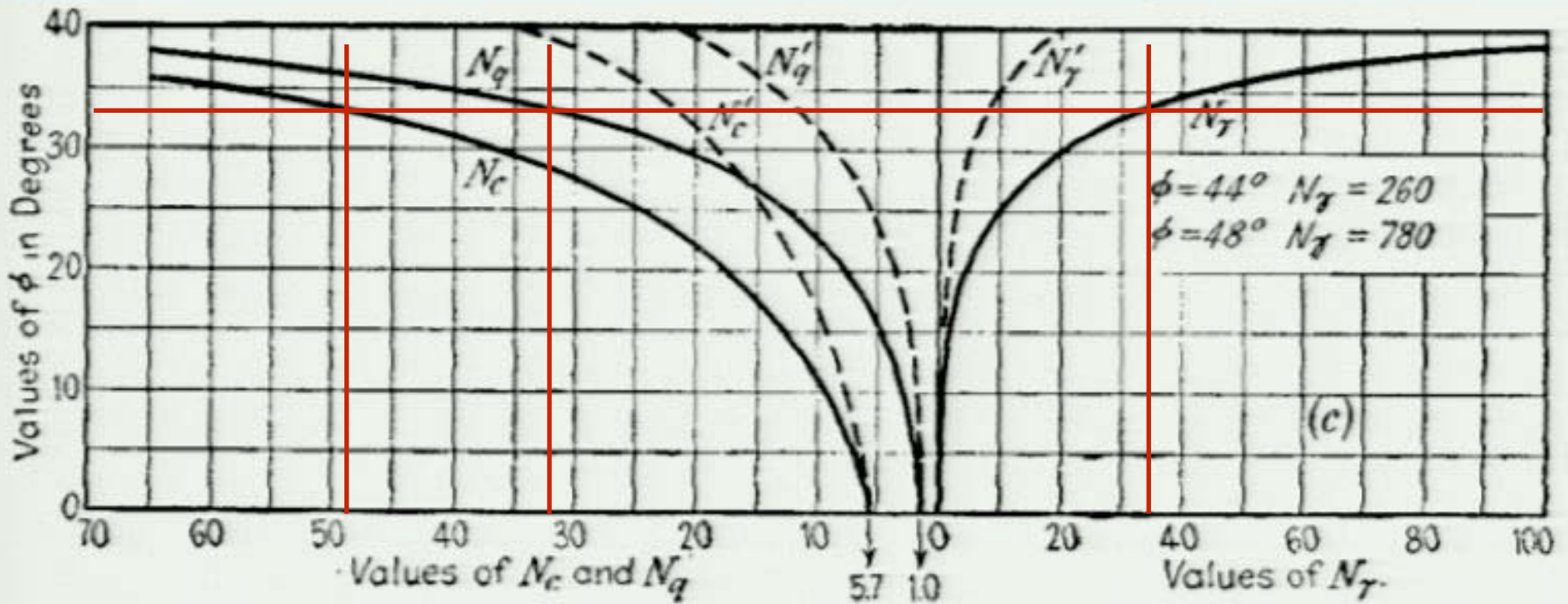
$$K_{\gamma} = \left(\frac{2N_{\gamma}}{\tan \phi} + 1 \right) \cos^2 \phi = 72.77$$

$$\ell = \frac{d}{2} \cos^{-1} \left(1 - \frac{2z}{d} \right) = 12.18 \text{ cm}$$

$$\gamma = 0.002595 \frac{N}{\text{cm}^3}; \quad c_o = 0.017 \frac{N}{\text{cm}^2}$$



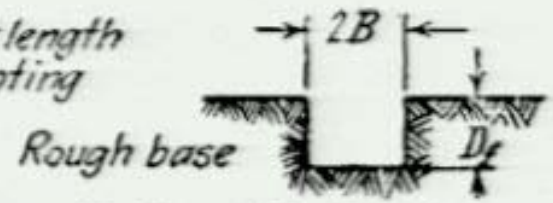
Terzhagi Parameters



General shear failure: $Q_D = 2B(cN_c + \gamma D_f N_q + \gamma B N_\gamma)$ } per unit length
 Local shear failure: $Q'_D = 2B(\frac{2}{3}cN'_c + \gamma D_f N'_q + \gamma B N'_\gamma)$ } of footing

Circular footing, Diameter $2R$,

Total critical load: $Q_{Dr} \approx R^2 \pi (1.3cN_c + \gamma D_f N_q + 0.6\gamma R N_\gamma)$



Unit weight of earth = γ

Unit shear. resistance $s = c + \sigma \tan \phi$

Red lines represent values calculated for this example



Bulldozing Example (3)

$$R_b = \frac{b \sin(\alpha + \phi)}{2 \sin \alpha \cos \phi} (2zcK_c + \gamma z^2 K_\gamma) + \frac{l_o^3 \gamma}{3} \left(\frac{\pi}{2} - \phi \right) + cl_o^2 \left[1 + \tan \left(\frac{\pi}{4} + \frac{\phi}{2} \right) \right]$$
$$\langle R_b \rangle = cm \left(cm \frac{N}{cm^2} + \frac{N}{cm^3} cm^2 \right) + cm^3 \frac{N}{cm^3} + \frac{N}{cm^2} cm^2$$

$$R_b = 94.98 + 0.000131 + 0.014 = 95.00 \text{ N per leading wheel}$$

$$R_{b,total} = 190.0 \text{ N}$$



Tractive Force per Wheel (No Grousers)

$$H = [AC_b + W_w \tan \phi_b] \left[1 - \frac{K}{\ell} \left(1 - e^{-\frac{s\ell}{K}} \right) \right]$$

A = area of contact = $b\ell$

C_b = coefficient of soil/wheel cohesion

ϕ_b = wheel/soil friction angle

s = wheel slip ratio

K = coefficient of soil slip

ℓ = length of contact patch



Tractive Force per Wheel (With Grousers)

$$H = \left[blC_b \left(1 + \frac{2h}{b} \right) N_g + W \tan \phi_b \left(1 + 0.64 \frac{h}{b} \arctan \frac{b}{h} \right) \right] \left[1 - \frac{K}{\ell} \left(1 - e^{-\frac{s\ell}{K}} \right) \right]$$

A = area of contact $\cong bl$

C_b = soil/wheel cohesion = 0.017 N/cm^2

ϕ_b = wheel/soil friction angle = 35°

s = wheel slip ratio (typ. 0.02-0.05)

K = coefficient of soil slip = 1.8 cm

ℓ = length of contact patch = $\frac{D}{2} \cos^{-1} \left(1 - \frac{2z}{D} \right)$

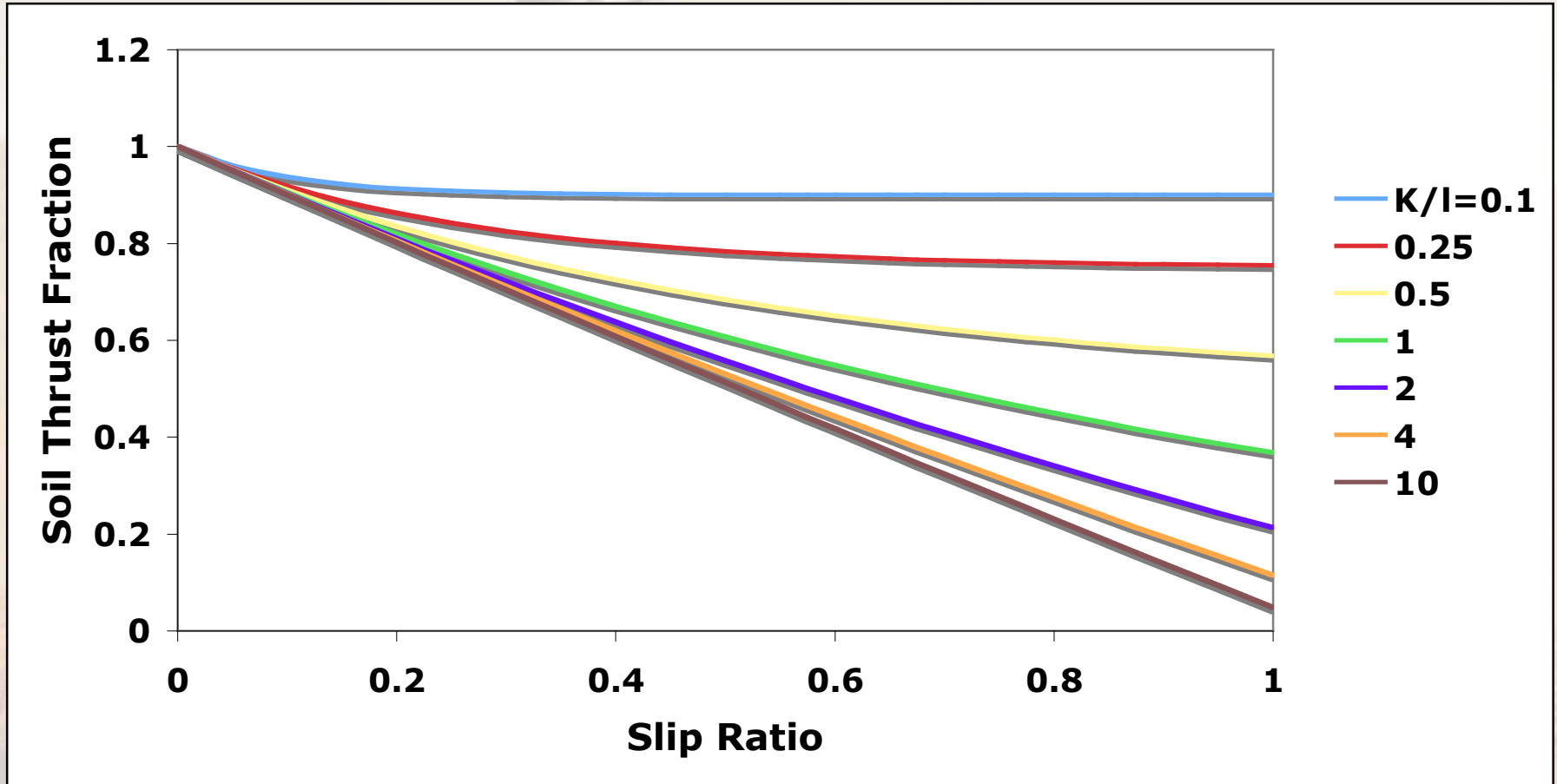
h = height of grouser

All values typical for lunar soil



Effect of Soil Thrust Fraction

Soil Thrust Fraction $\left[1 - \frac{K}{\ell} \left(1 - e^{-\frac{s\ell}{K}} \right) \right]$



Basic Equation of Vehicle Propulsion

$$DP = H - (R_c + R_b + R_g + R_r)$$

- DP: Drawbar pull (residual drive force)
- H: Maximum tractive force of wheels
- R_c : Compaction resistance
- R_b : Bulldozing resistance
- R_g : Gravitational resistance
- R_r : Rolling resistance (internal)





Surface Interaction Modeling

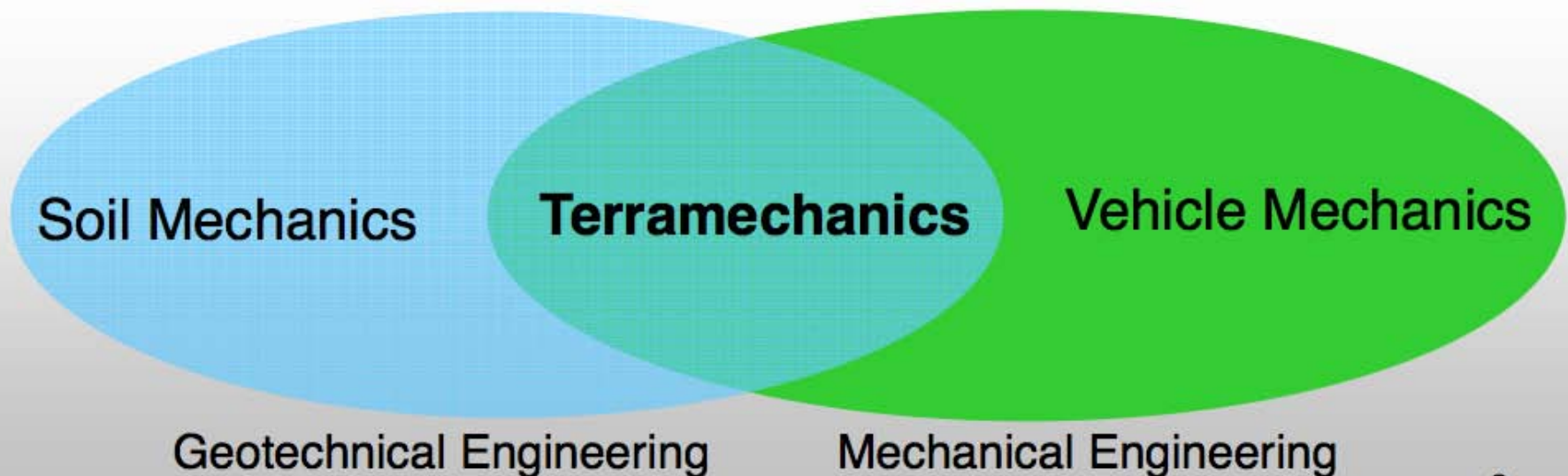
Engineering Methods

Karl Iagnemma, Ph.D.
Massachusetts Institute of Technology



Terramechanics

- Terramechanics
 - Engineering science that studies the interaction between vehicles and (deformable) terrain
- Soil mechanics and vehicle mechanics
- Analysis of wheeled, tracked, legged systems





An Engineer's Job

- Design vehicle for robust mobility on Mars surface
 - Wheels, tracks, legs?
 - Number, diameter and width?
 - Required nominal torque?
 - Required peak power?
 - Obstacle crossing performance?
 - Suspension configuration?
 - Steering mechanism?
- **How to address in a principled, systematic fashion?**



NASA's Mars Science Laboratory (MSL)
Design/Test Model (DTM) in the sandy Mars Yard at JPL



An Engineer's Reality

- How to model this scenario?
 - High sinkage
 - High slip ratio
 - Material transport effects
 - Clogged grousers
 - Variables of interest
 - Soil properties
 - Soil state
 - Wheel load
 - Wheel geometric properties
 - Wheel linear and angular velocity





Terramechanics

- Limitations of terramechanics modeling
 - Attempt to model all soil types with single set of relations
 - Frictional soils, crusty materials, clay
 - Assumption of homogeneity
 - Attempt to apply (semi)-empirical models in predictive manner
 - Little consideration of off-nominal operation
 - Difficulty in employing quasi-static models for dynamic simulation
- Assertion: General approach remains valid
 - Not all limitations are fundamental
- Goals
 - Understand limits of applicability of terramechanics
 - Identify areas requiring new research



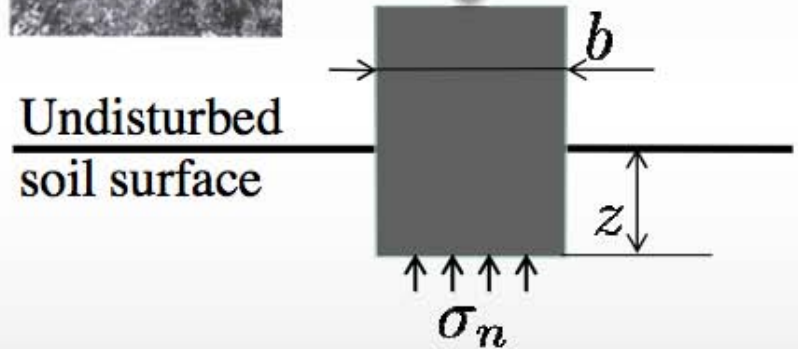
Pressure-Sinkage

- Pressure-sinkage relationship for geomaterials

$$\sigma = kz^n$$

- σ is normal pressure
- k is empirical constant
- z is sinkage from free surface

- Bekker proposed semi-empirical formulation



Cohesion-dependent soil coefficient

Friction-dependent soil coefficient

$$\sigma_n = \left(\frac{k_c}{b} + k_\phi \right) z^n$$

Sinkage exponent

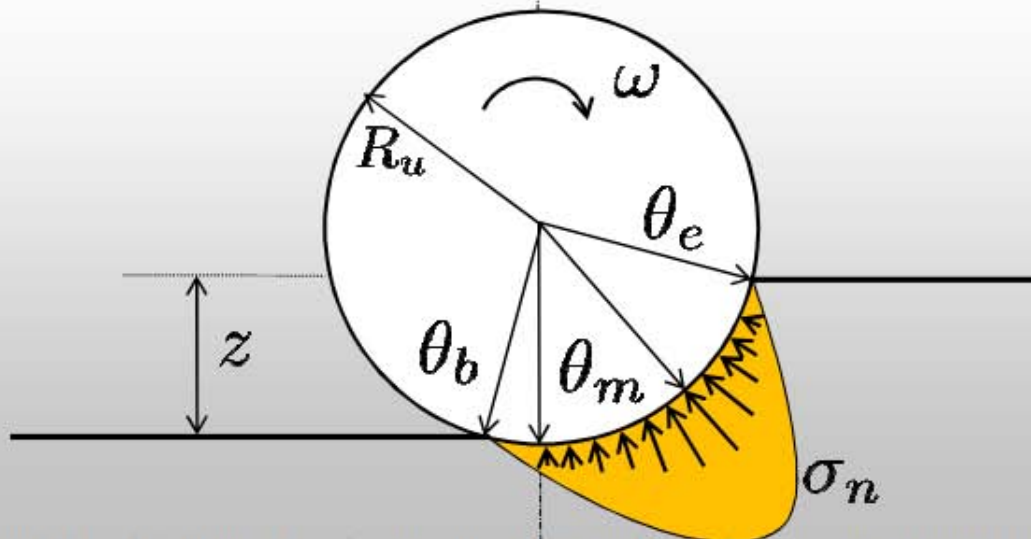


Pressure-Sinkage for Wheels

- Can compute normal stress for wheels along terrain interface

$$\sigma_{nf} = \left(\frac{k_c}{b} + k_\phi \right) [R (\cos(\theta) - \cos(\theta_e))]^n \quad \theta_m < \theta \leq \theta_e$$

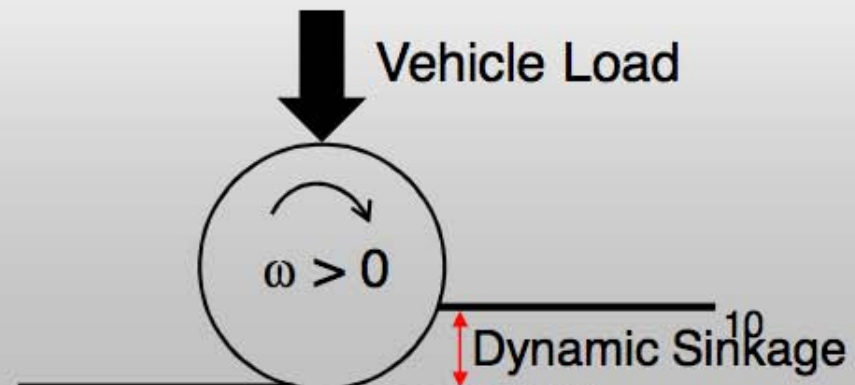
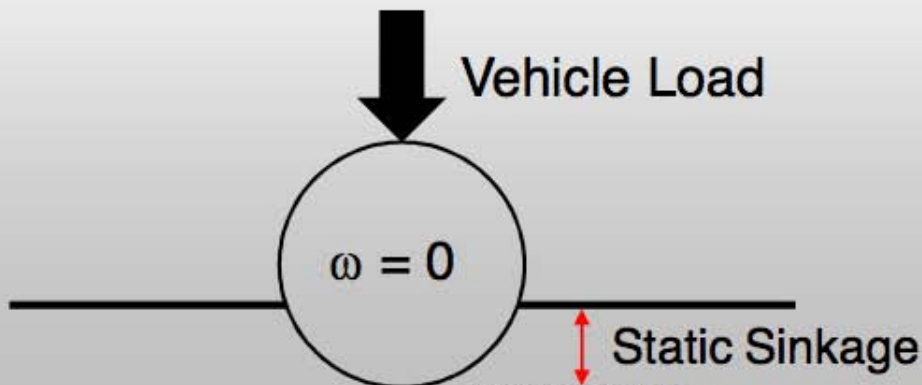
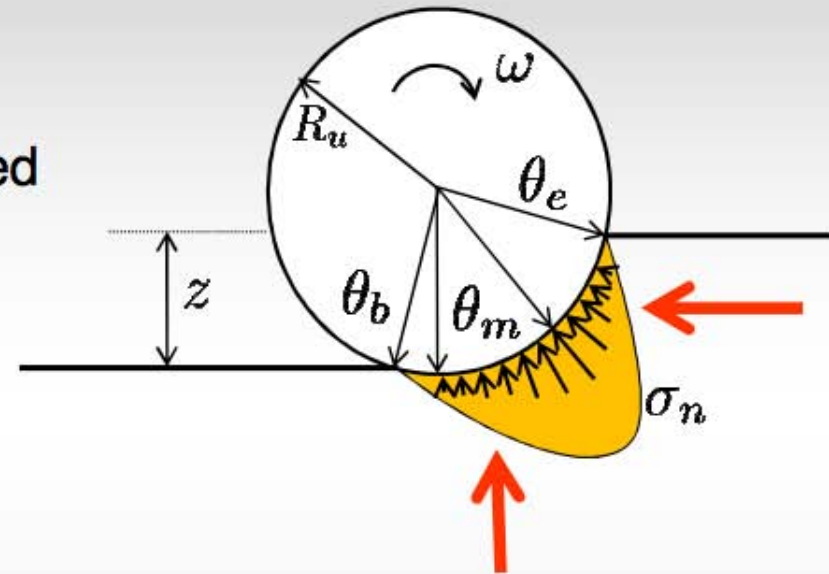
$$\sigma_{nr} = \left(\frac{k_c}{b} + k_\phi \right) \left[R \left(\cos \left(\theta_e - \left(\frac{\theta - \theta_r}{\theta_N - \theta_r} \right) (\theta_e - \theta_N) \right) - \cos(\theta_e) \right) \right]^n \quad \theta_b \leq \theta \leq \theta_m$$





Pressure-Sinkage for Wheels

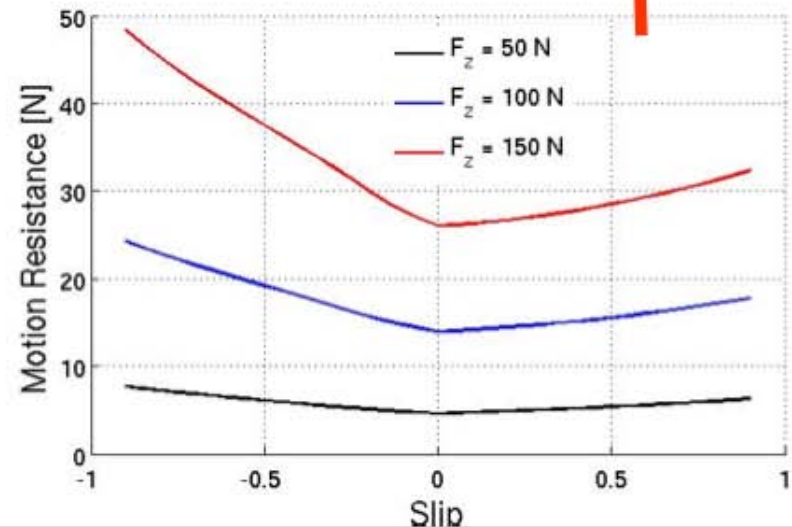
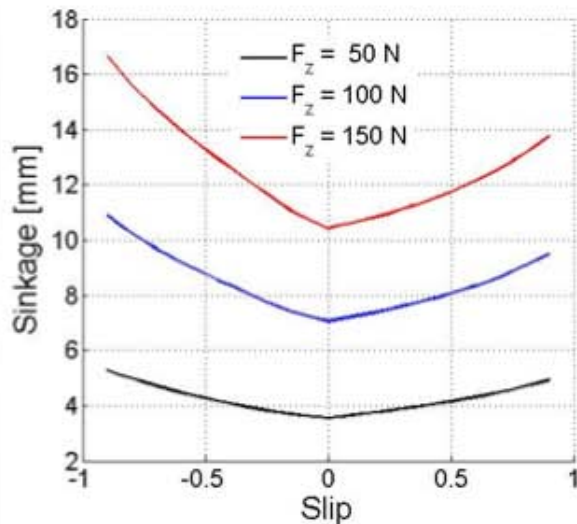
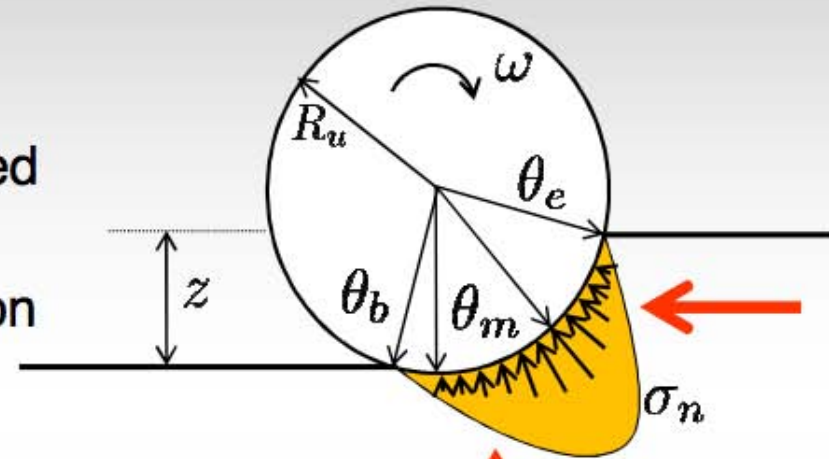
- Sinkage plays critical role in mobility
 - Increased sinkage causes increased motion resistance
 - Energy lost in terrain compaction
- Sinkage can be divided in two components
 - Static sinkage
 - Dynamic sinkage (or slip-sinkage)





Pressure-Sinkage for Wheels

- Sinkage plays critical role in mobility
 - Increased sinkage causes increased motion resistance
 - Energy lost in terrain compaction





Shearing Properties of Soil

- Can compute shear stress at wheel-terrain interface
 - Janosi-Hanamoto formulation

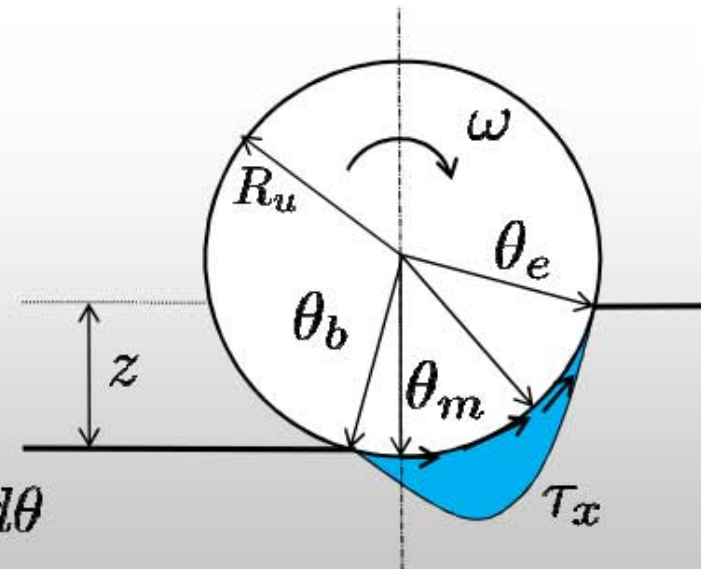
$$\tau_x(\theta) = \tau_{max} \left(1 - e^{\frac{-j_x}{k_x}} \right)$$

Limit tangential stress \downarrow τ_{max} \uparrow Soil shear deformation modulus k_x
 j_x \leftarrow Soil shear displacement

$$\tau_{max} = c + \sigma_n(\theta) \tan \phi$$

- Soil shear displacement

$$j_x(\theta) = \int_{\theta_b}^{\theta_e} R_u [1 - (1 - s_d) \cos(\theta)] d\theta$$

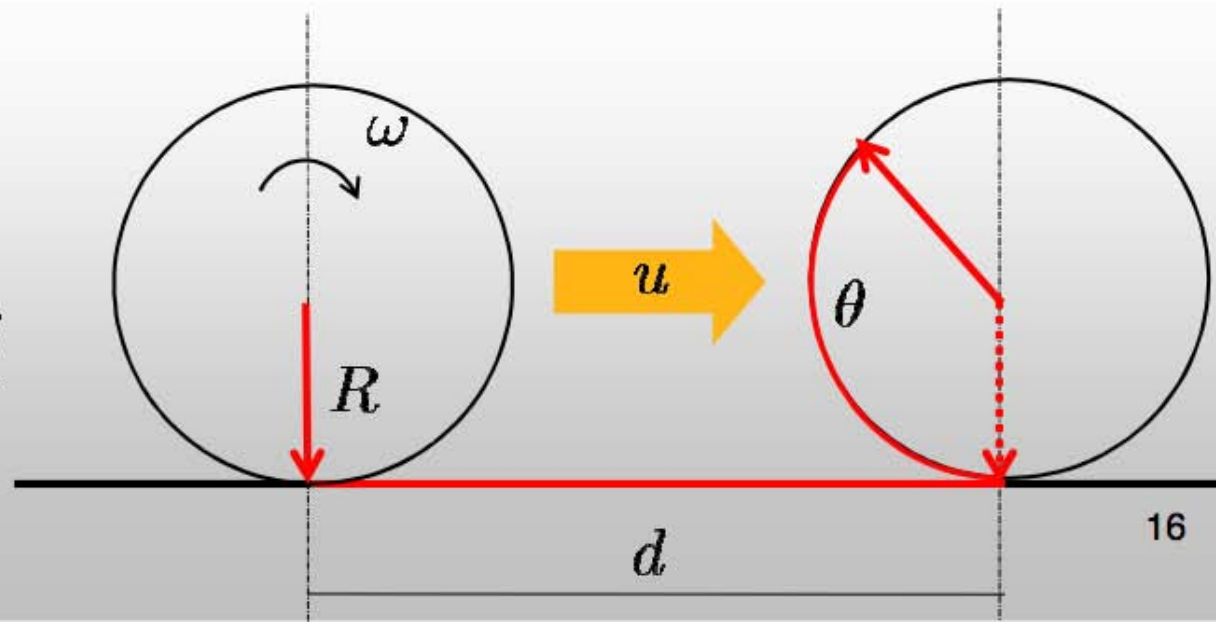




Slip Ratio

- Slip ratio is measure of relative motion between wheel and terrain surface
 - For driven wheel, distance traveled is less than that in free rolling
 - When slip ratio = 1, spinning in place
 - When slip ratio = 0, pure rolling
 - When slip ratio = -1, skidding

$$u \leq \omega R$$
$$d \leq \theta R$$
$$s_d = 1 - \frac{u}{\omega R}$$





Terrain Interaction Forces

- Forces between wheel and terrain can be computed from stress distribution along contact path
- Vertical load

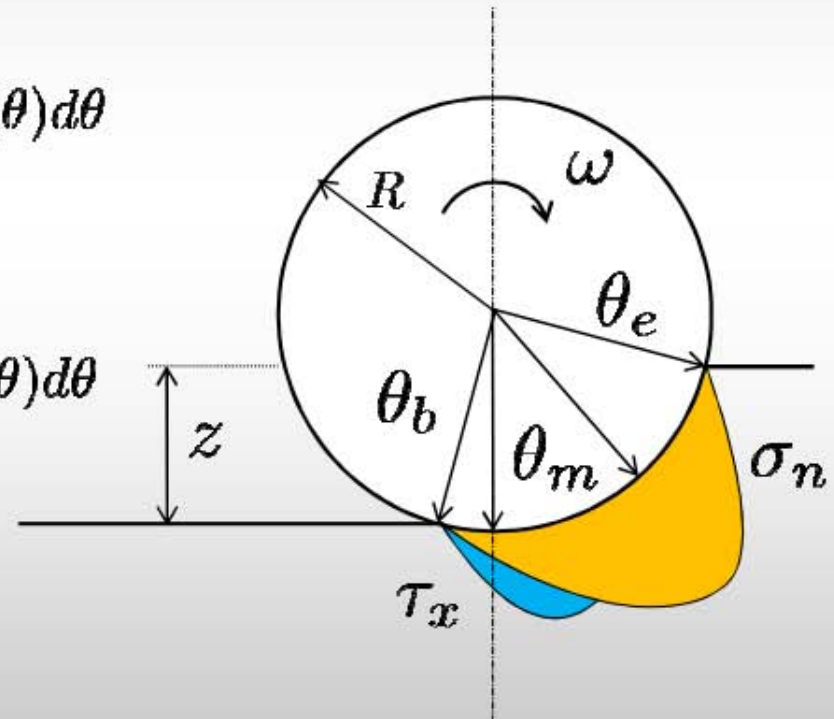
$$W = bR \int_{\theta_b}^{\theta_e} \tau_x(\theta) \sin(\theta) + \sigma_n(\theta) \cos(\theta) d\theta$$

- Longitudinal force

$$F_x = bR \int_{\theta_b}^{\theta_e} \tau_x(\theta) \cos(\theta) - \sigma_n(\theta) \sin(\theta) d\theta$$

- Torque on wheel axle

$$T = bR^2 \int_{\theta_b}^{\theta_e} \tau_x(\theta) d\theta$$





Summary

- Stresses at wheel-terrain interface
 - Decompose into normal and shear stresses
 - Modeled with semi-empirical formulations
 - Integration yields forces acting on vehicle
- Given
 - Terrain properties
 - Slip
 - Loading conditions
- Can compute
 - Sinkage
 - Thrust
 - Required torque

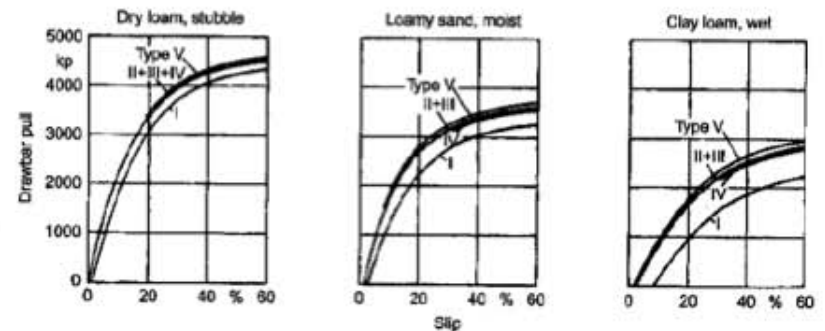
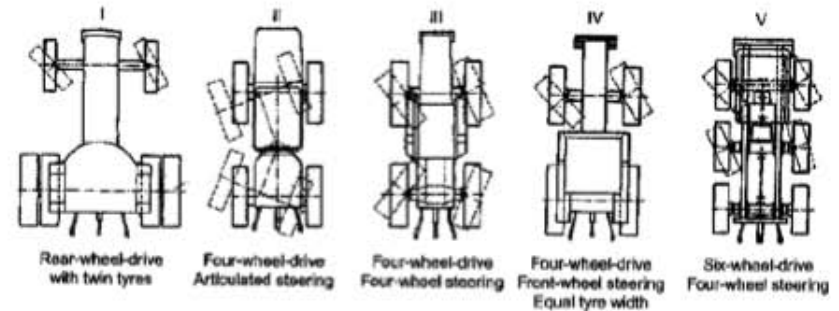


Figure 1.3: Comparison of various configurations for agricultural tractors (Reprinted by permission of ISTVS from Sohne, 1976)



Effect of Grousers

- Grousers are small features on wheel surface
 - Designed to improve traction and climbing performance
- Have been modeled through Terzaghi's bearing capacity theory



Pathfinder, MER, and MSL wheels

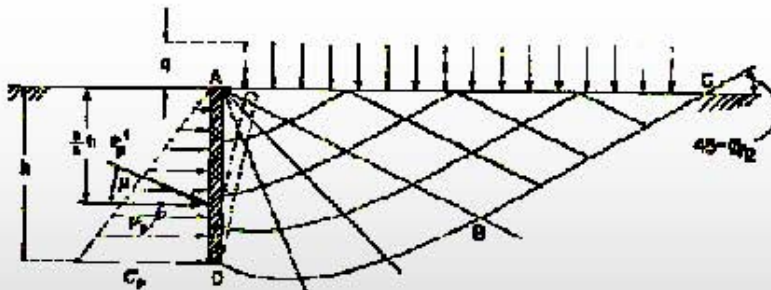


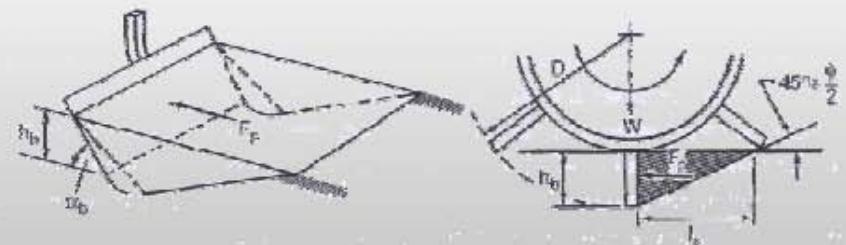
Fig. 69

The value of the force P_p assumed for $\mu = 0$ may be calculated by integrating the pressure σ_p determined by equation (134):

$$P_p = \int_0^h \sigma_p dz = \int_0^h (\gamma N_D + 2c \sqrt{N_D} + \gamma \pi N_D) dz$$

and

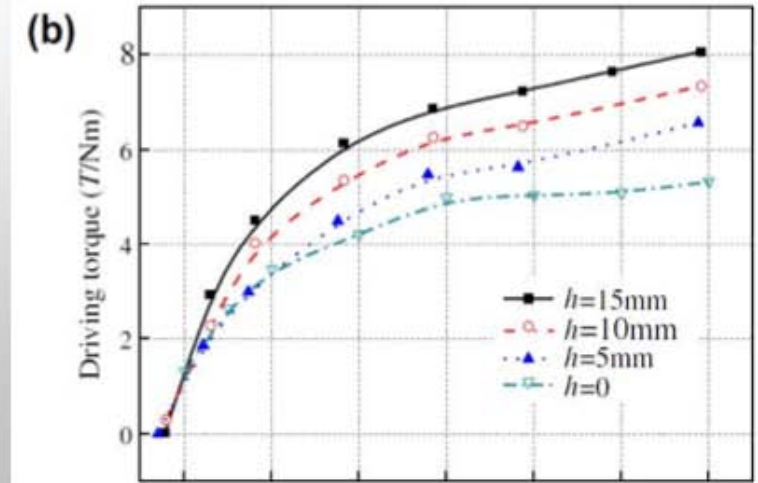
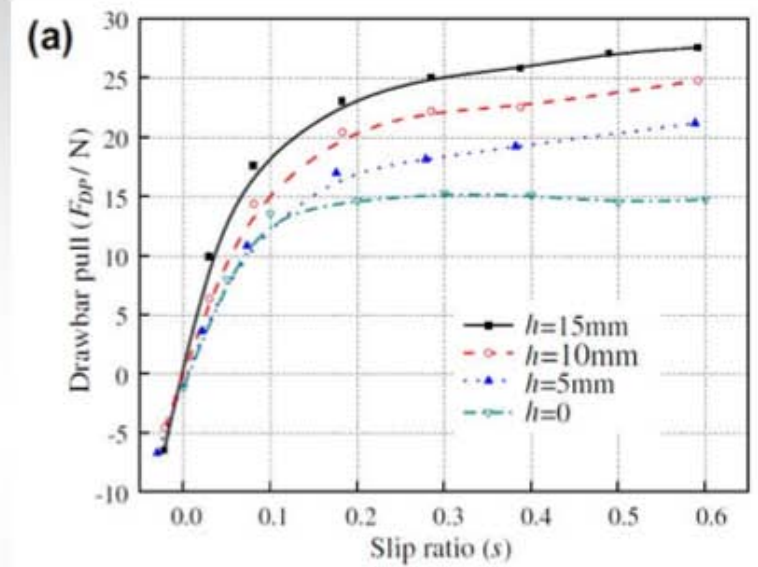
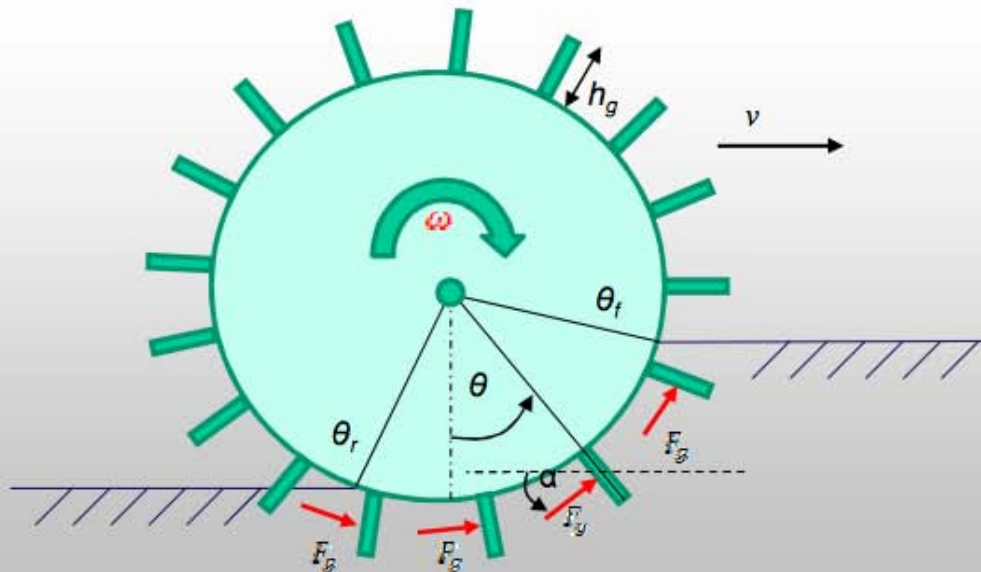
$$P_p = q h N_D + 2 c h \sqrt{N_D} + \frac{1}{2} \gamma h^2 N_D$$





Effect of Grousers

- Grouser effect has also been empirically studied
 - Grouser height, spacing, geometry affect torque, traction, turning performance

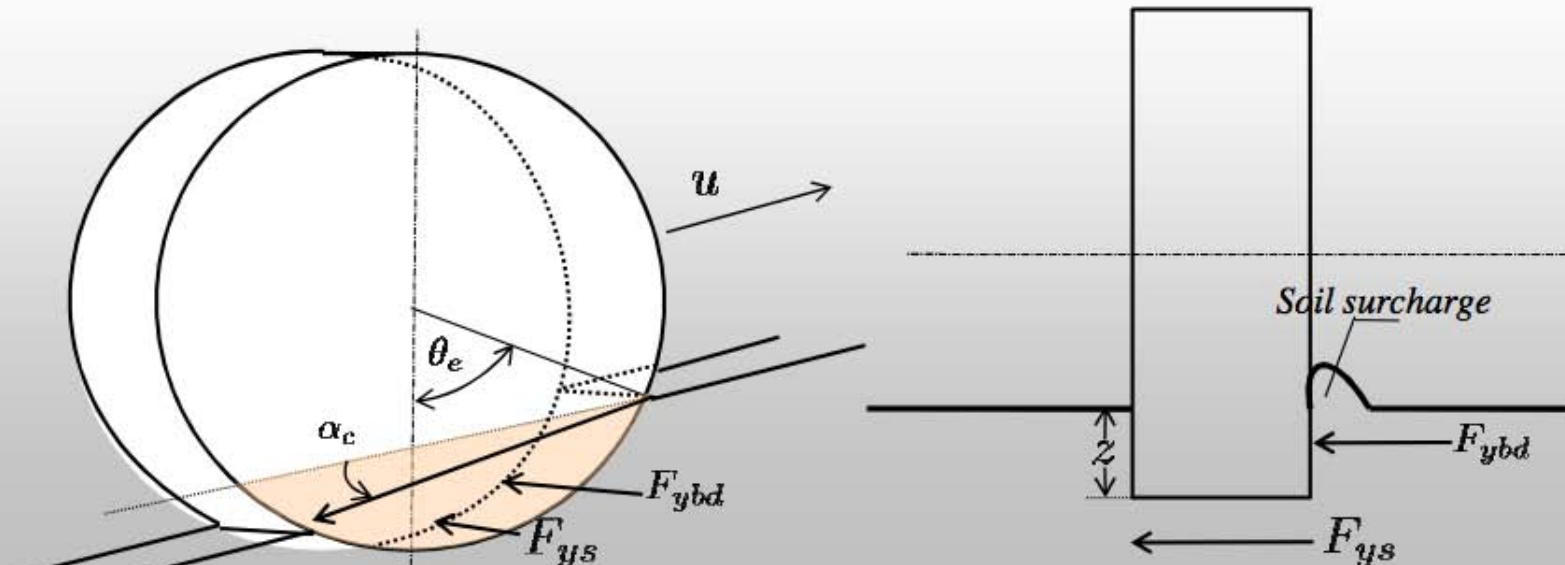


- Lateral forces act on wheel sidewall during turning
 - Forces arise from soil shearing and bulldozing

$$F_y = F_{ys} + F_{ybd}$$

$$F_{ybd} = w \int_{\theta_b}^{\theta_e} (\gamma_s z N_\gamma + c N_c + q N_q) \cos(\delta_f) d\theta$$

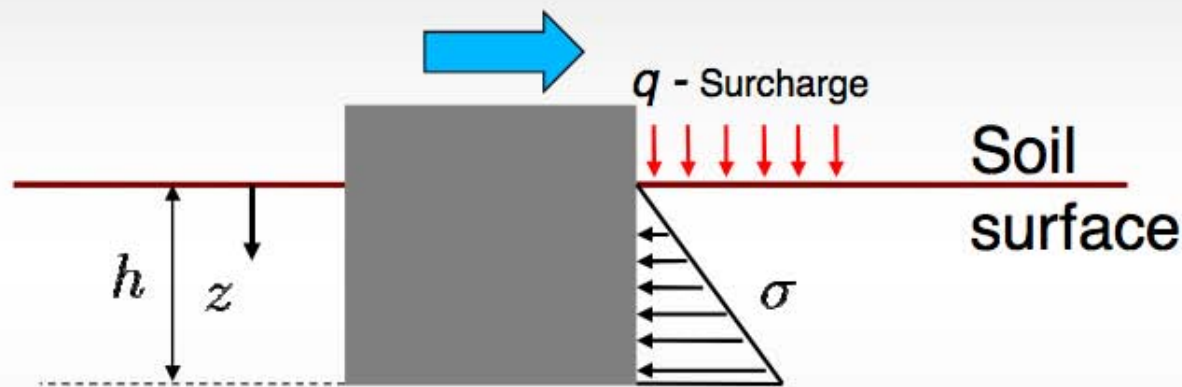
$$F_{ys} = b \int_{\theta_b}^{\theta_e} (c + \sigma_n(\theta) \tan(\phi)) \left(1 - e^{-\frac{j_y}{k_y}}\right) d\theta$$





Lateral Force - Bulldozing

- Like grouser effect, bulldozing is typically modeled through soil bearing capacity analysis



$$\sigma = \gamma z N_\gamma + c N_c + q N_q \text{ [Pa]}$$

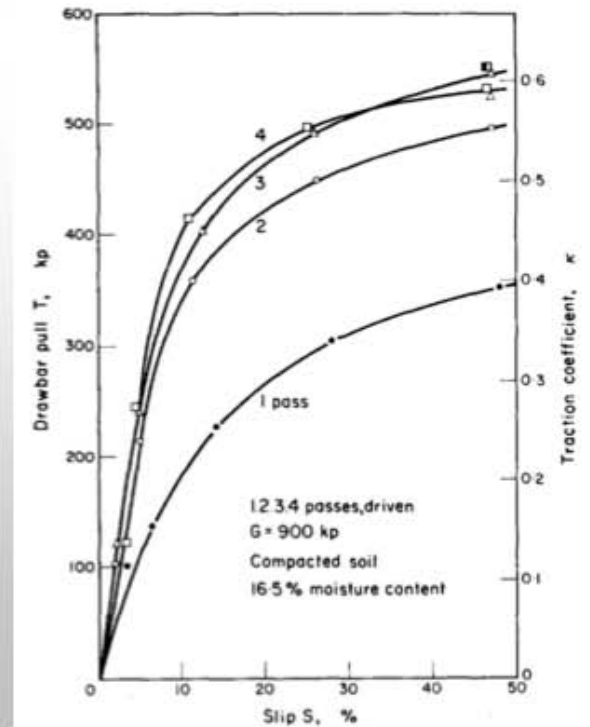
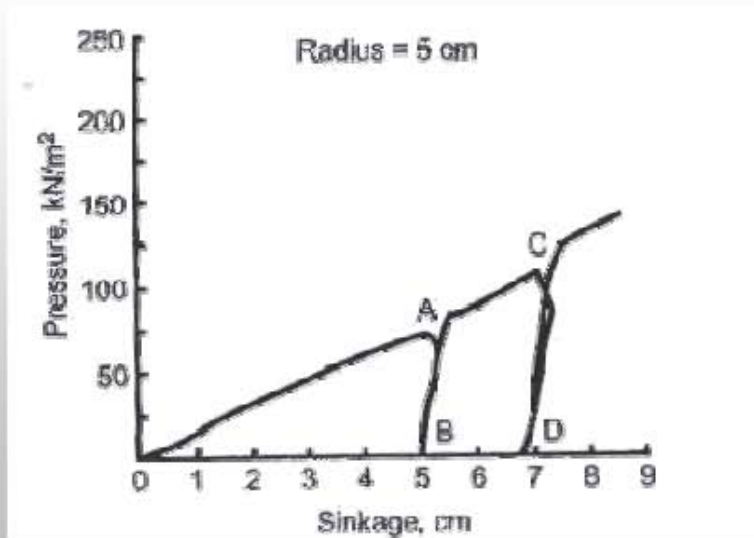
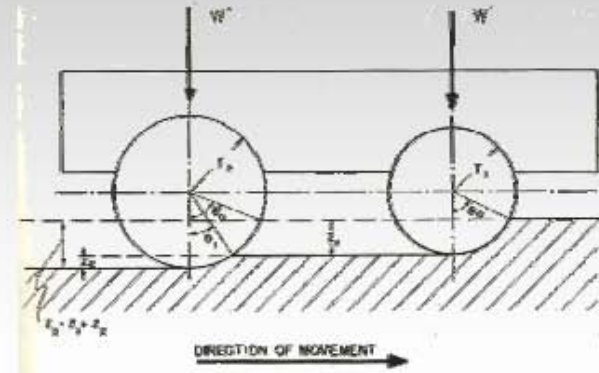
- N -factors are function of soil angle of internal friction

$$N_\gamma = \frac{2(N_q + 1) \tan \phi}{1 + 0.4 \sin 4\phi} \quad N_c = \frac{N_q - 1}{\tan \phi} \quad N_q = \frac{e^{(1.5\pi - \phi) \tan \phi}}{2 \cos^2(\pi/4 + \phi/2)}$$



Repetitive Loading

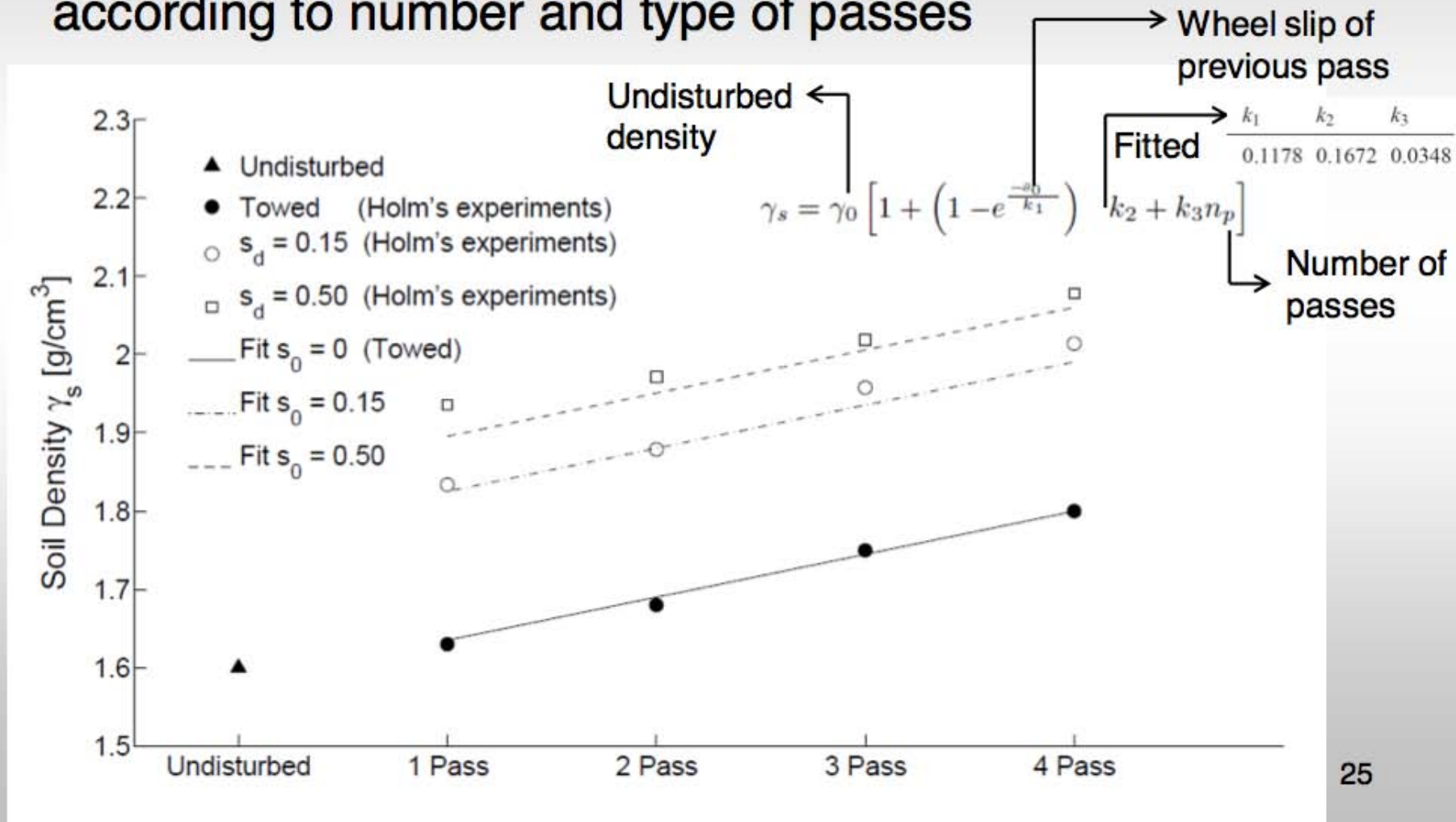
- Rover trailing wheels may pass through soil deformed by leading wheels
 - Repetitive loading alters soil behavior
 - Increases compaction (relative density)





Repetitive Loading

- Multi pass can be modeled by modifying soil parameters according to number and type of passes



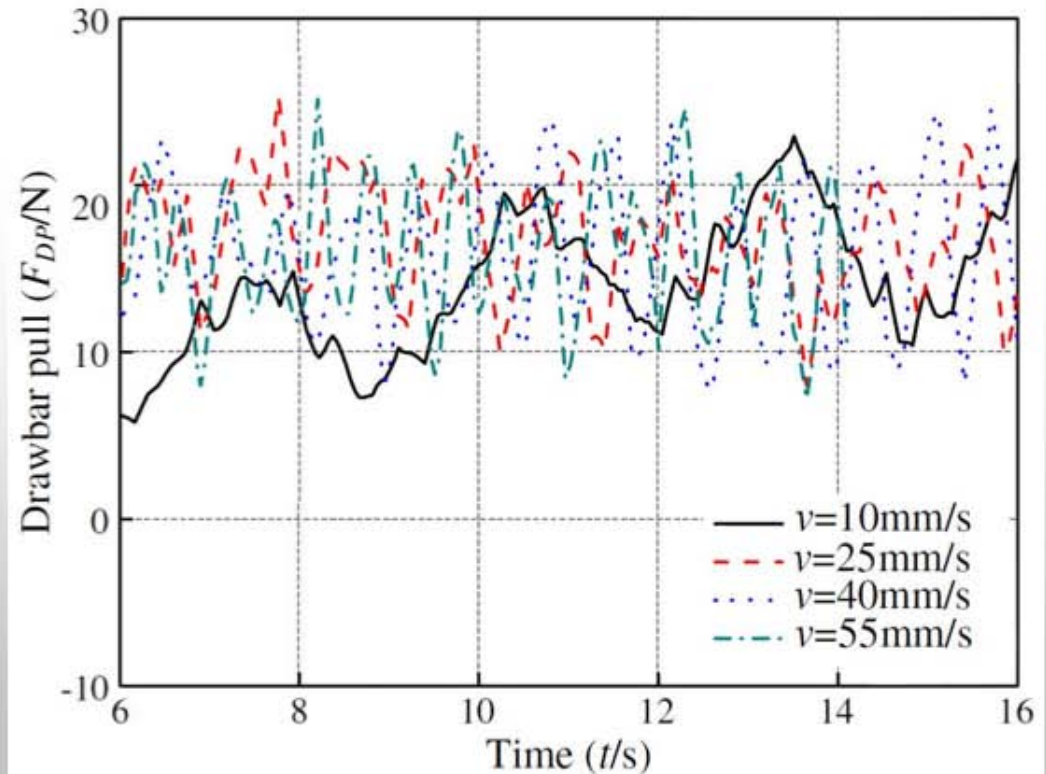
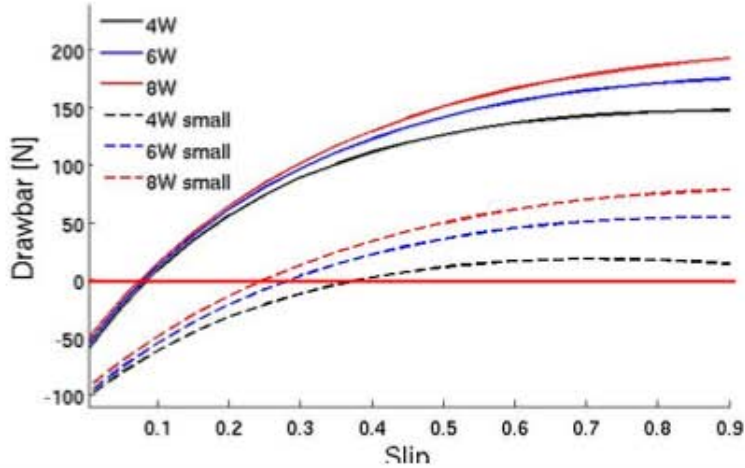


Classical Model Limitations

- Terramechanics developed in context of large vehicles, for design trade space analysis
 - Would like to apply to smaller, lighter systems, for dynamic sim
- Key limitations
 - Effect of terrain inhomogeneity
 - Soil condition dependence
 - Layering, relative density, moisture content
 - Scale effects
 - Parameter scale dependence (non-intrinsic soil properties)
 - Effects related to slipping and sinking
 - Slip ratio definition
 - Rate dependence



Terrain Inhomogeneity (1)





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- Terramechanics developed in context of large vehicles, for design trade space analysis
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Terrain Inhomogeneity

- Pressure-sinkage relation characterizes wide range of terrains with single equation
 - Loose, granular soils, crusty materials, clay

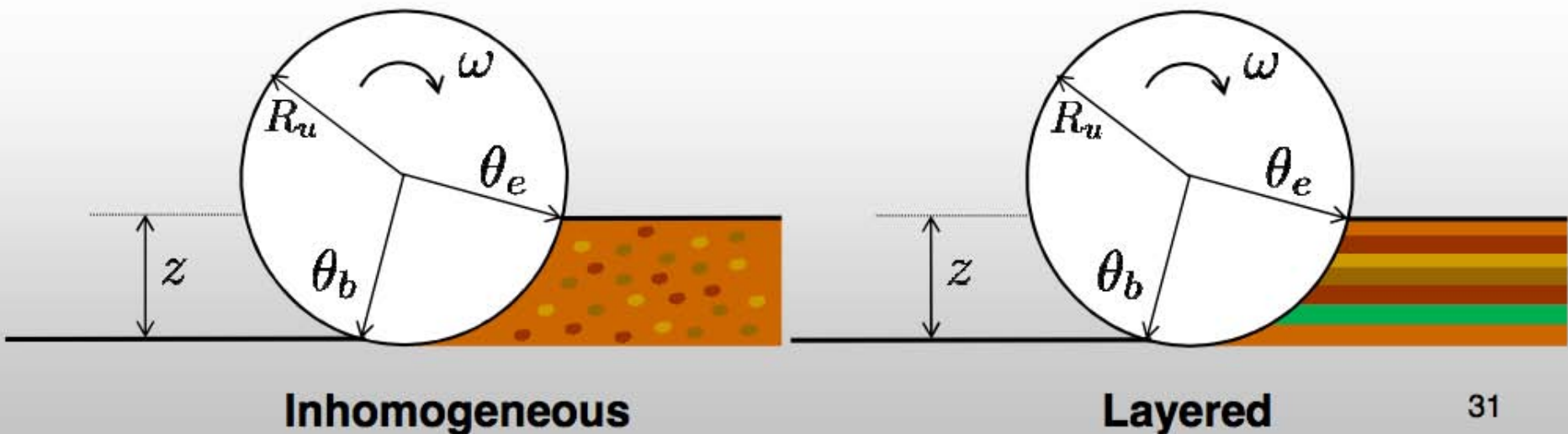
$$\sigma_n = \left(\frac{k_c}{b} + k_\phi \right) z^n$$

- Observations: significant experimental variation wrt soil condition
 - Layering
 - Relative density
 - Moisture content



Terrain Inhomogeneity (1)

- Bekker theory assumes homogenous soil
 - Soil is often layered, inhomogeneous
- Lack of analytical formulations for pressure-sinkage, shear stress-shear deformation





Terrain Inhomogeneity (1)

- Pressure-sinkage relations

$$\sigma_n = \left(\frac{k_c}{b} + k_\phi \right) z^n$$

$$\sigma_{nf} = \left(\frac{k_c}{b} + k_\phi \right) [R(\cos(\theta) - \cos(\theta_e))]^n$$

$$\sigma_{nr} = \left(\frac{k_c}{b} + k_\phi \right) \left[R \left(\cos \left(\theta_e - \left(\frac{\theta - \theta_r}{\theta_N - \theta_r} \right) (\theta_e - \theta_N) \right) - \cos(\theta_e) \right) \right]^n$$

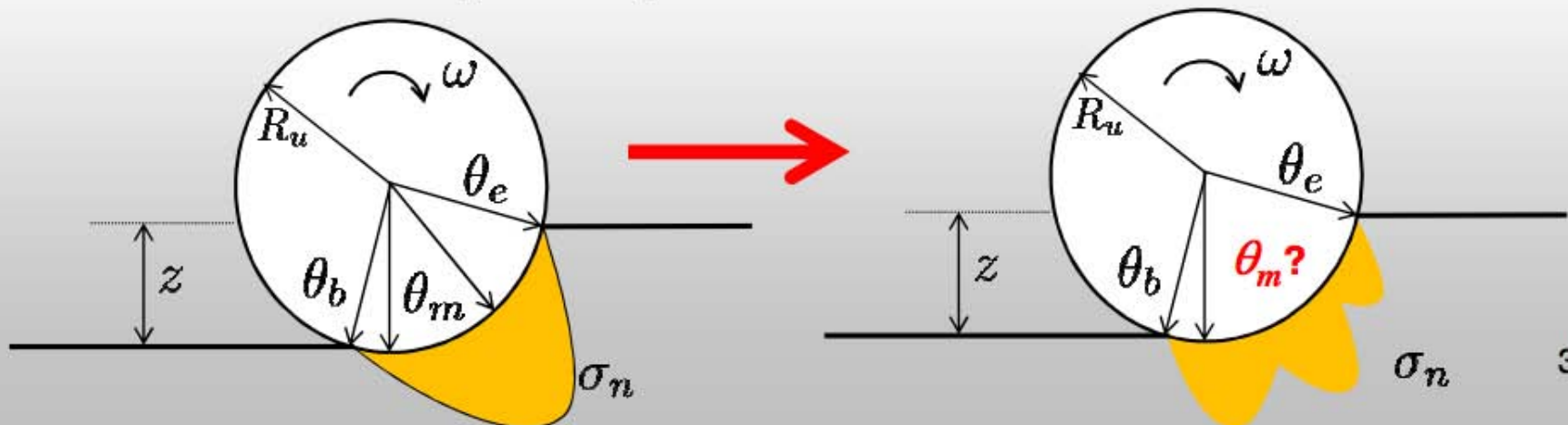
$$\theta_m < \theta \leq \theta_e$$

$$\theta_b \leq \theta \leq \theta_m$$

How to define?

- Shear stress-shear displacement

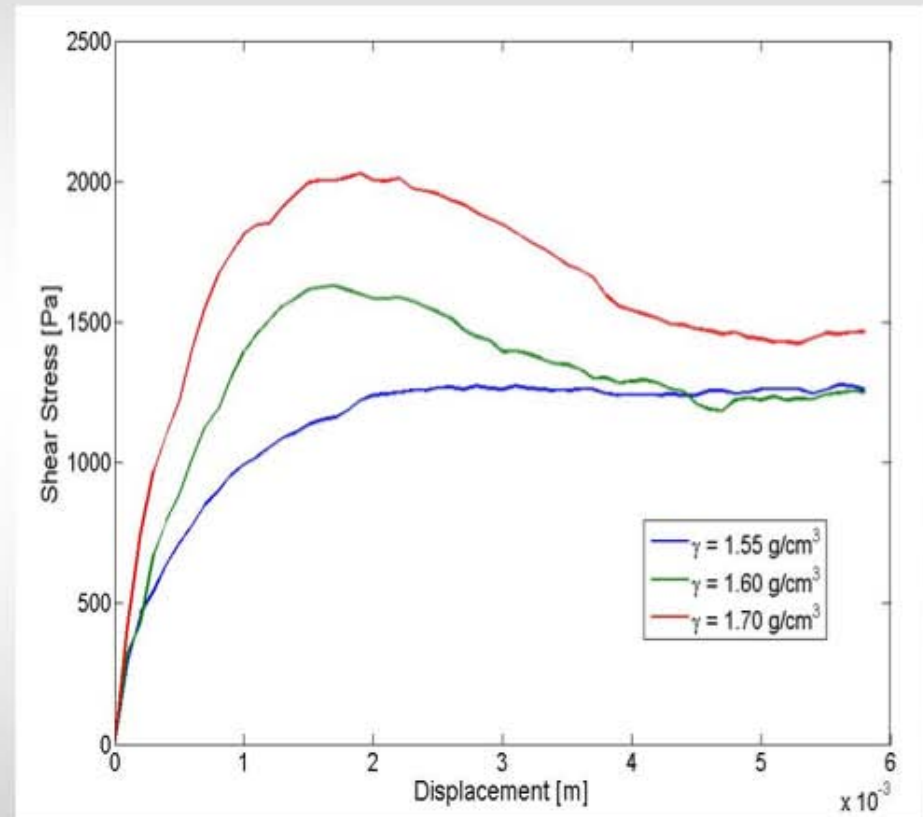
$$\tau_x(\theta) = \tau_{max} \left(1 - e^{\frac{-jx}{k_x}} \right) \quad \tau_{max} = c + \sigma_n(\theta) \tan \phi$$





Terrain Inhomogeneity (2)

- Bekker theory (generally) ignores soil state
- Large vehicles tend to compact terrain to dense state upon passage
 - For small rovers, weight is insufficient to compact soil
- Relative density can strongly influence shear stress at interface
 - Strong influence on thrust
 - Strong influence on torque during digging/scooping

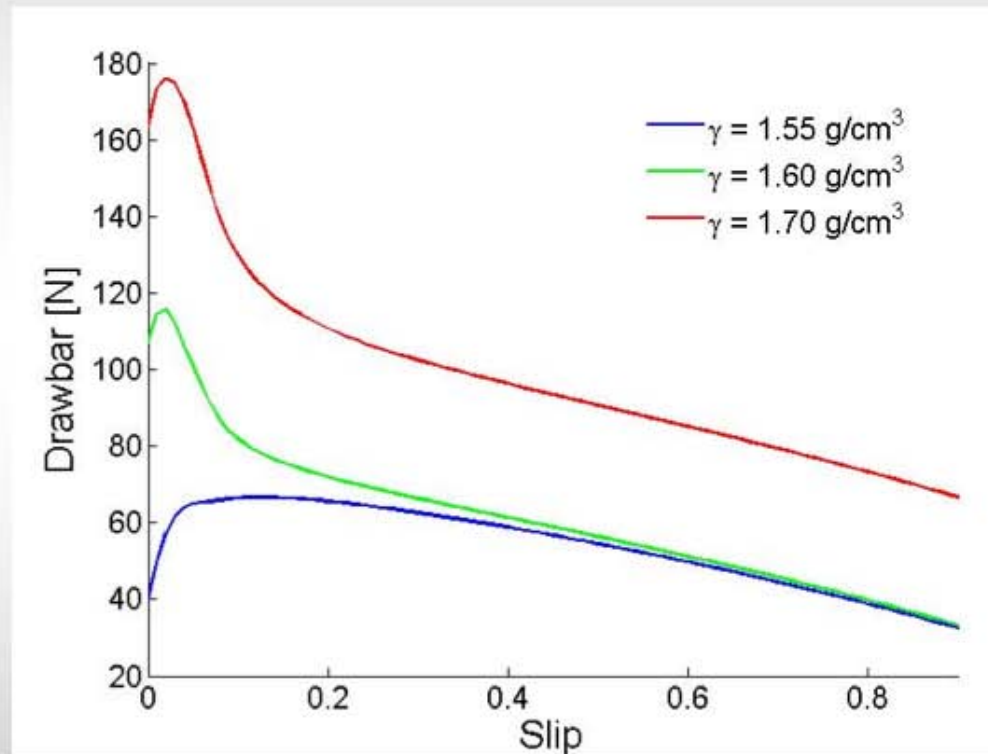


Shear box test of MMS



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Terrain Inhomogeneity

- Questions (Solutions?)

- How to compute sinkage in inhomogeneous soil?

- Express sinkage in integral form (layered)?

$$\sigma_n = \left(\frac{k_c}{b} + k_\phi \right) z^n$$

- Effective parameters for mixed soils?

- How to compute failure of layered (crusty) soil?

$$\tau_{max} = c + \sigma_n(\theta) \tan \phi$$

- Piecewise formulation?

- Smoothness of stress distribution?

- How to represent parameters?

- Intervals? Distributions?

- State dependent? (For all soils, or only some?)

- How to represent governing equations?

- Deterministic? Stochastic?



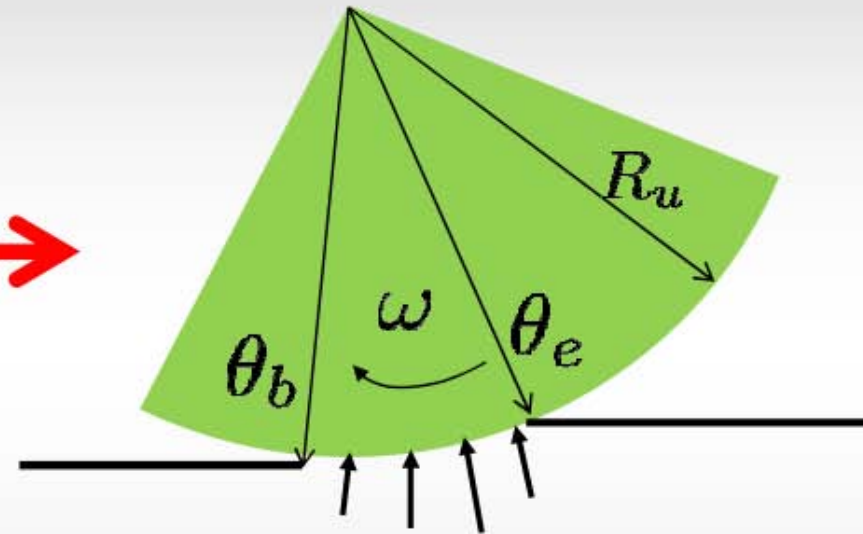
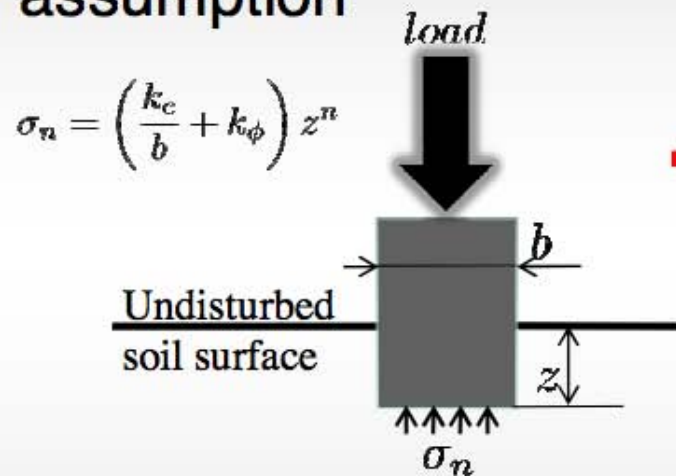
Classical Model Limitations

- Terramechanics developed in context of large vehicles, for design trade space analysis
 - Would like to apply to smaller, lighter systems, for dynamic sim
- **Key limitations**
 - Effect of terrain inhomogeneity
 - Soil condition dependence
 - Layering, relative density, moisture content
 - **Scale effects**
 - **Parameter scale dependence (non-intrinsic soil properties)**
 - Effects related to slipping and sinking
 - Slip ratio definition
 - Rate dependence



Scale Effects (1)

- Pressure-sinkage relations developed under flat plate assumption



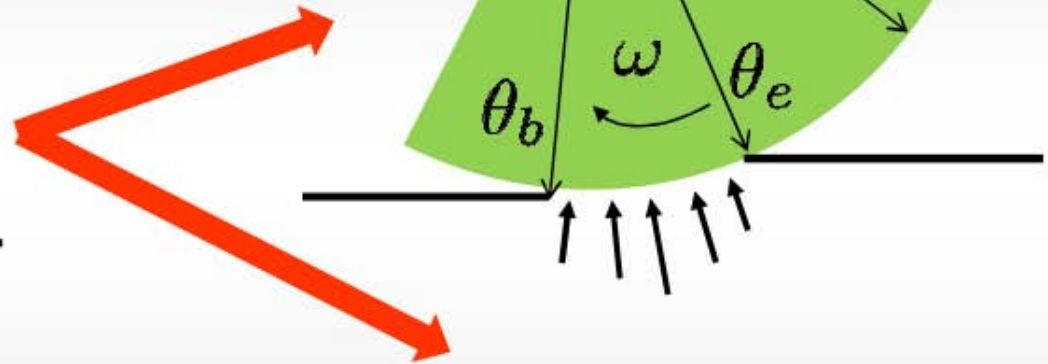
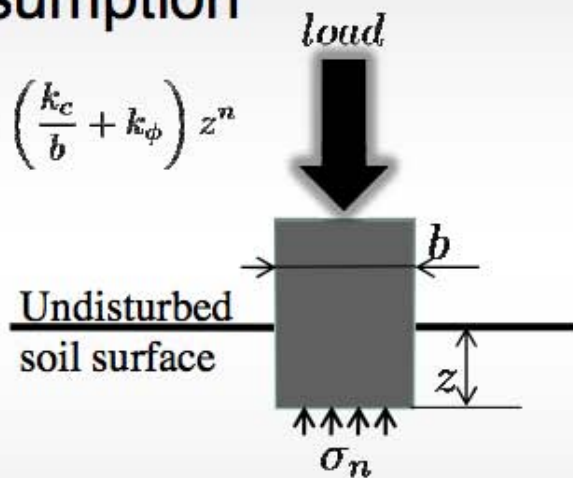
- Reasonable for large vehicles
 - Uniform stress distribution at interface



Scale Effects (1)

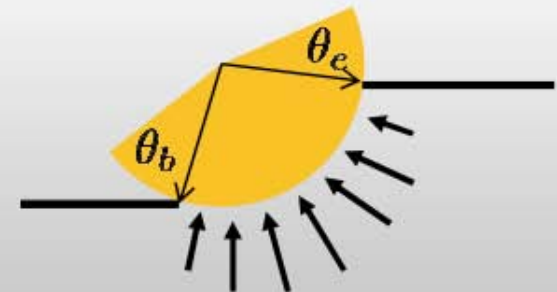
- Pressure-sinkage relations developed under flat plate assumption

$$\sigma_n = \left(\frac{k_c}{b} + k_\phi \right) z^n$$



- What about for small vehicle, with high wheel curvatures?

- Stress distribution at interface non-uniform
- Component of normal stress balances load

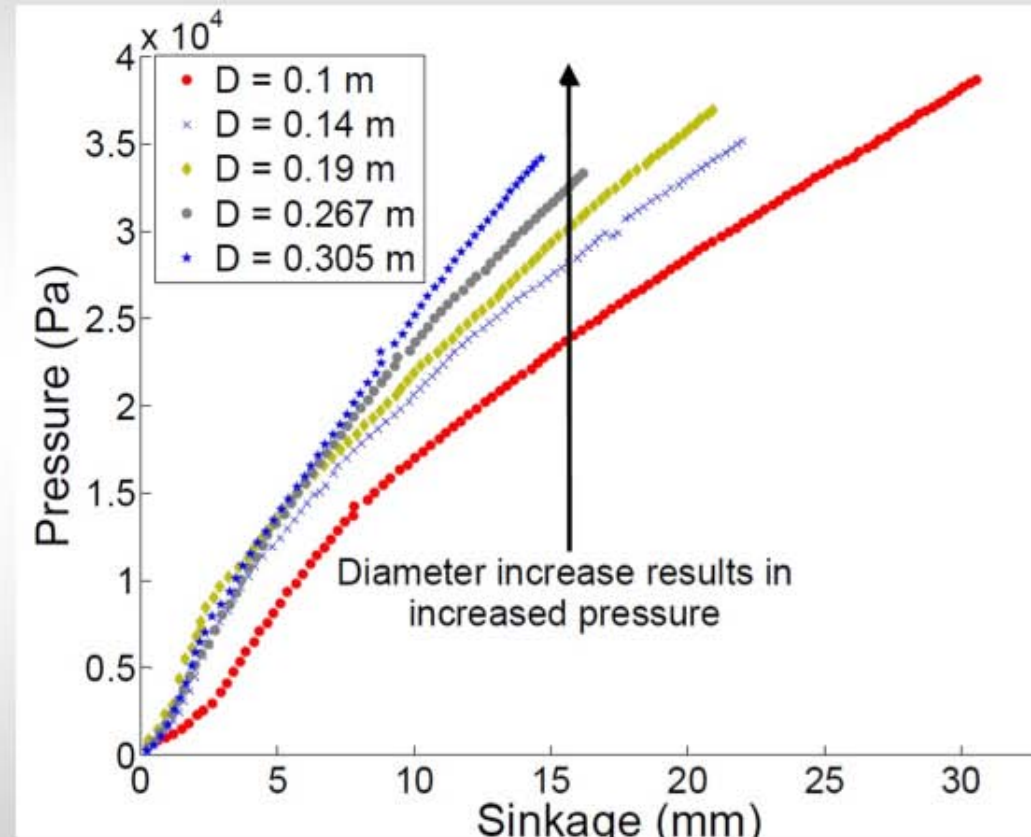




Scale Effects (1)

- Result: Poor prediction of sinkage
- Why is this?
 - Intrinsic parameters not really intrinsic

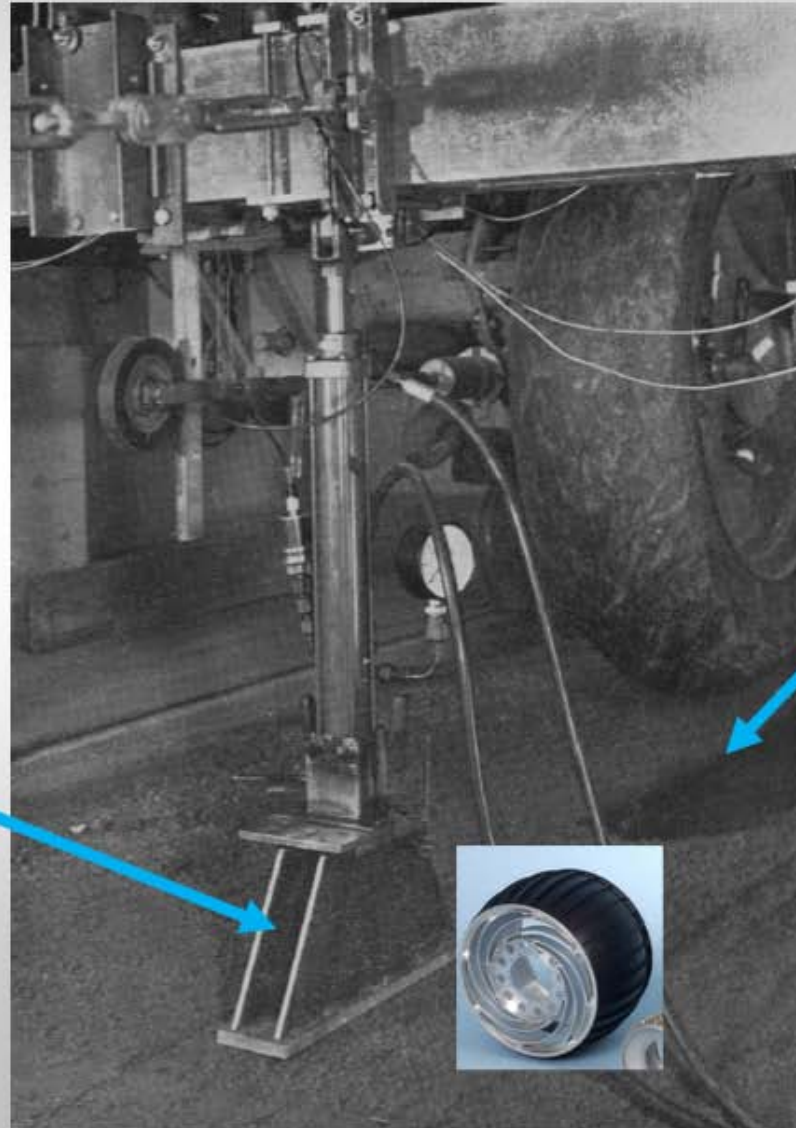
$$\sigma_n = \left(\frac{k_c}{b} + k_\phi \right) z^n$$





Scale Effects (1)

Beviameter
plate



Tire imprint

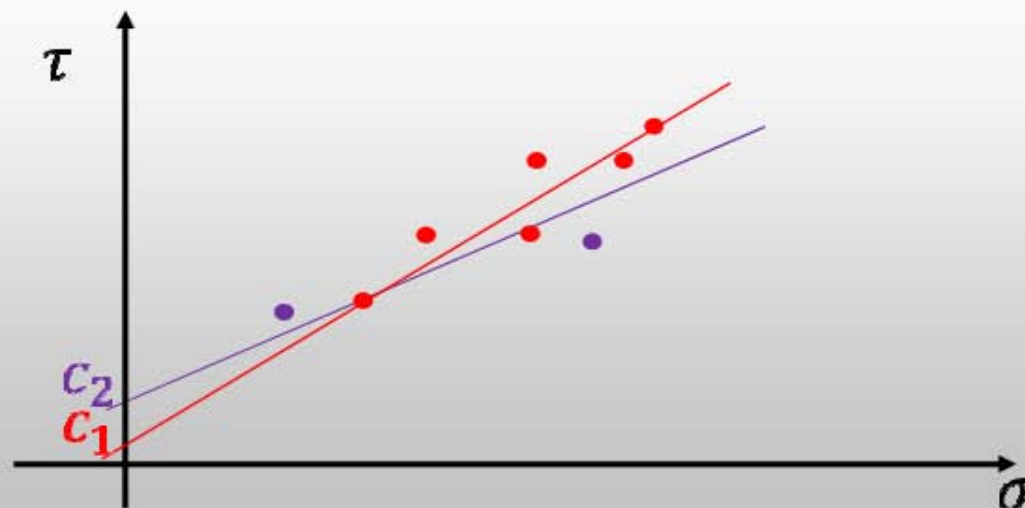


Scale Effects (2)

- Soil shear failure is governed by soil cohesion and internal friction angle

$$\tau_{max} = c + \sigma_n(\theta) \tan \phi$$

- Cohesion often measured at high normal stress
 - At low normal loads, effect of cohesion can dominate



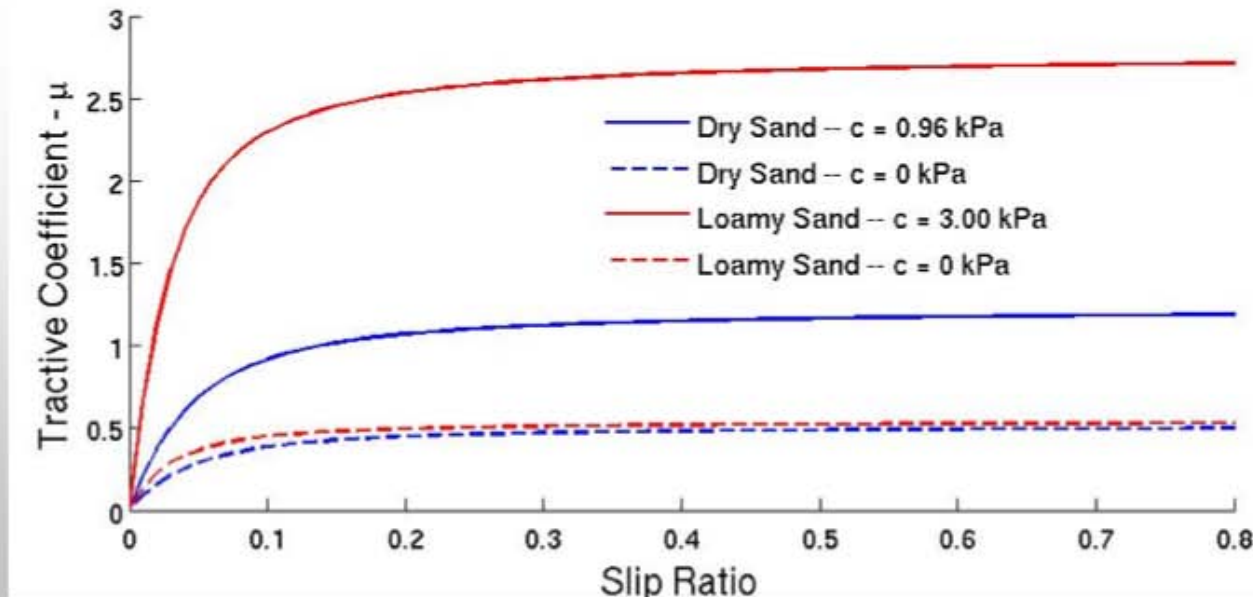


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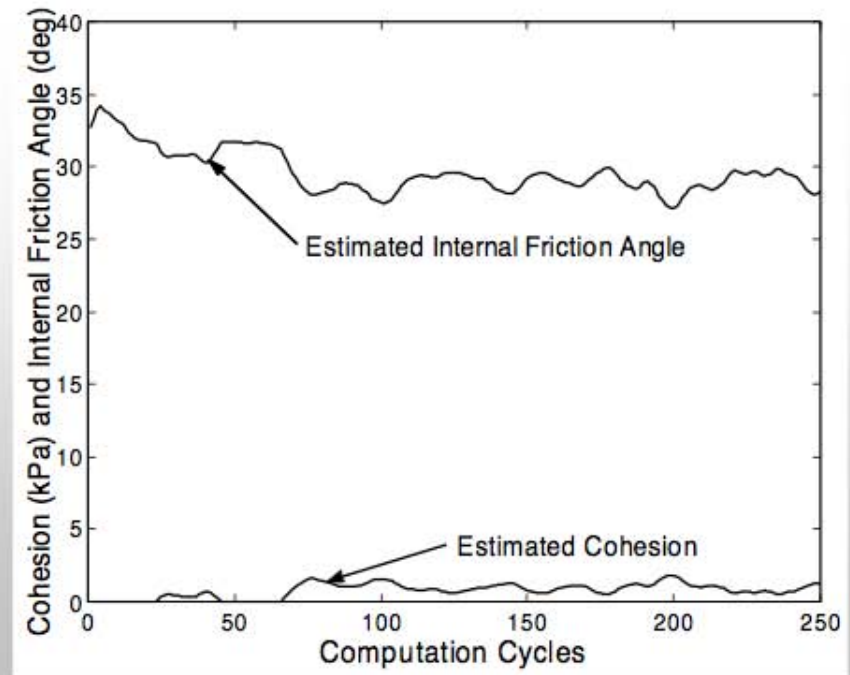
- Cohesion often measured at high normal stress
 - At low normal loads, effect of cohesion can dominate





Scale Effects

- Questions (Solutions?)
 - Can we formulate terramechanics relations with intrinsic parameters?
 - Consistent results across scales
 - Can we develop in situ measurement/estimation procedures for parameter estimation?
 - Can we develop lab test devices/procedures for measurement at low normal stress?





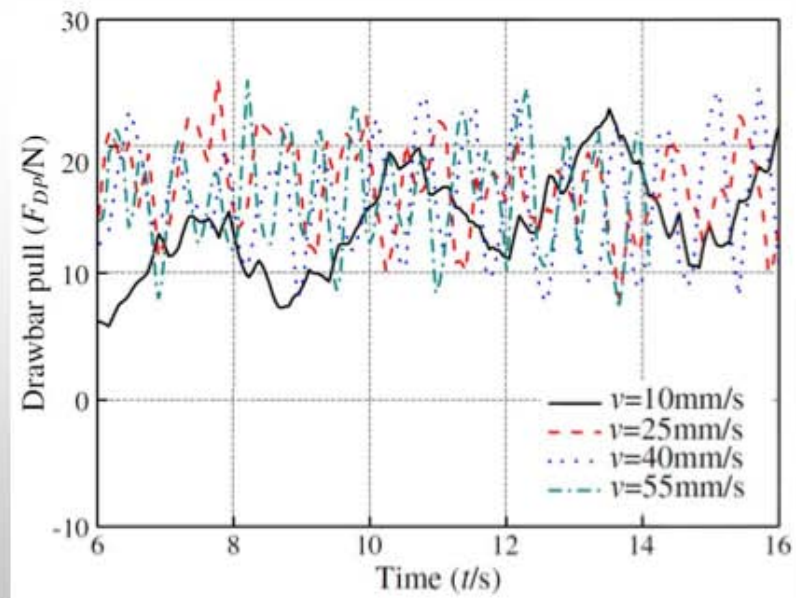
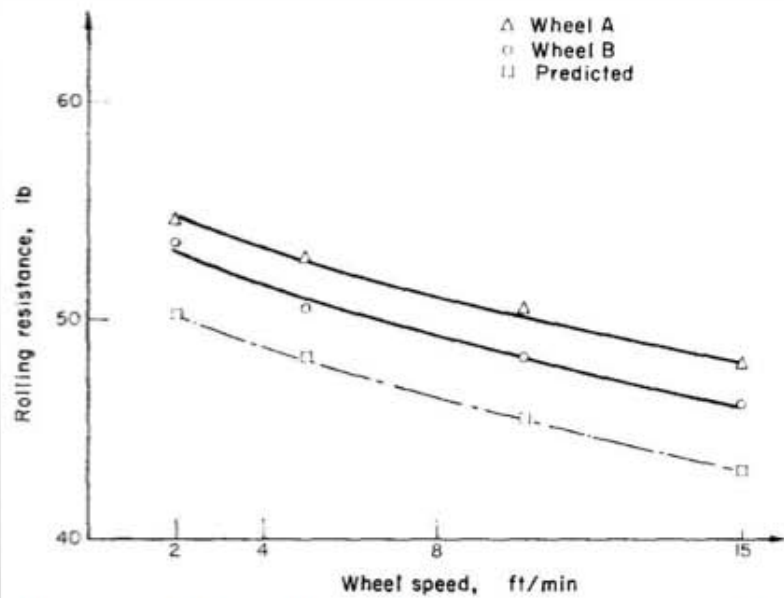
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 - Slip ratio definition
 - Rate dependence



Slipping and Sinking (1)

- Terramechanics models are not rate dependent
- Studies on large wheels show that at higher velocity^{1,2}:
 - Sinkage decreases
 - Traction improves
- Experiments³ on small wheels have suggested little influence

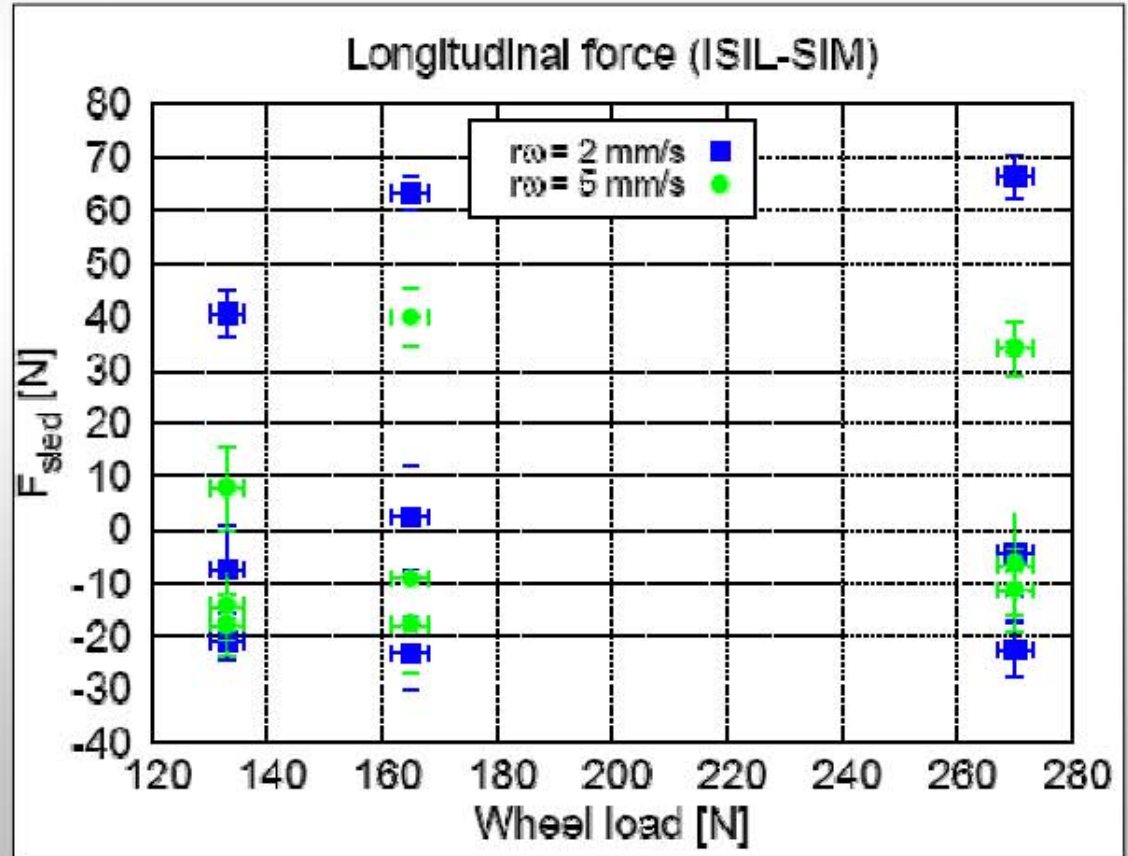


1. Shmulevic I. et al./Journal of Terramechanics 35,1998, 189-207
2. Pope R.G./ Journal of Terramechanics 8(1), 1971, 51-58
3. Ding L. et al./Journal of Terramechanics 48, 2011, 27-45



Slipping and Sinking (1)

- Experiments with MER wheels have shown significant velocity effect
 - Plot of thrust force vs. vertical wheel load

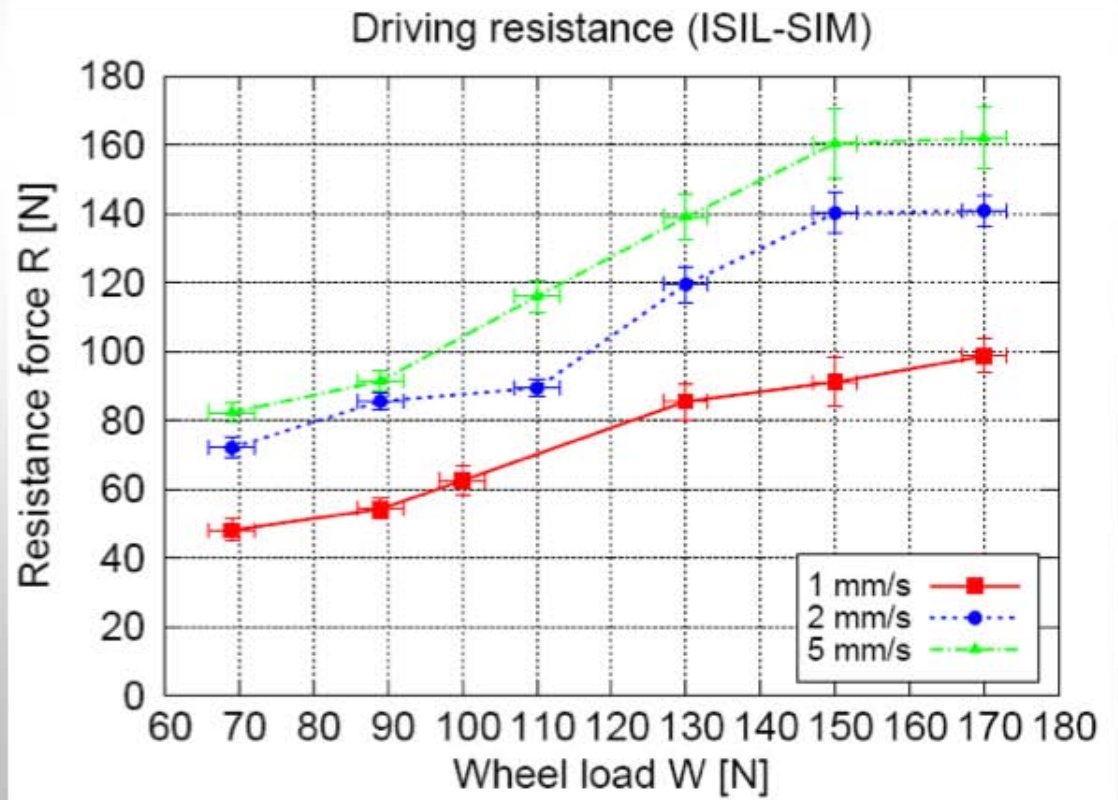


- Vertical array of same-color data points: slip increasing top to bottom (83 %, 92 %, 98 %)



Slipping and Sinking (1)

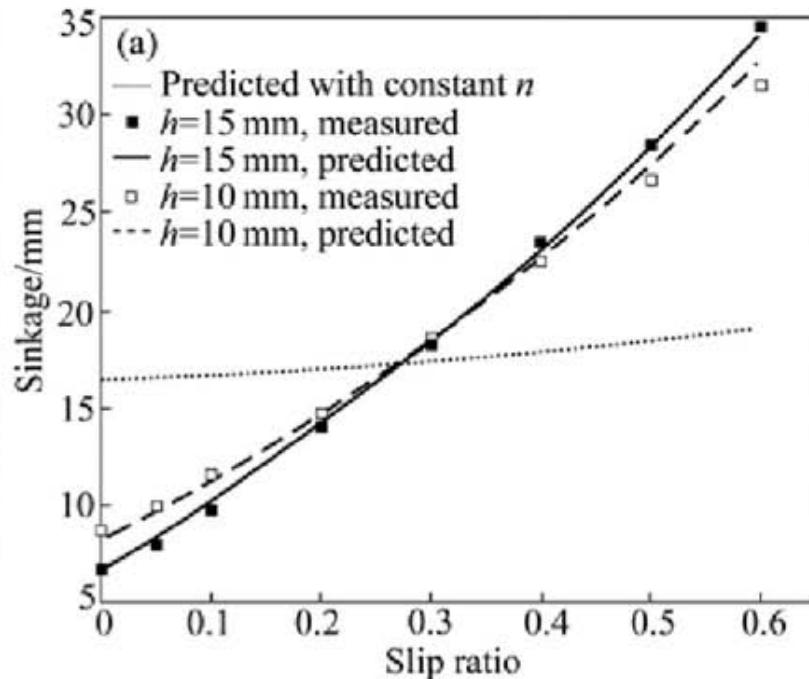
- Experiments with MER wheels have shown significant velocity effect
 - Resistance from blocked RF wheel vs wheel load and drag velocity





Slipping and Sinking (2)

- Terramechanics theory is not well suited for modeling motion with high slippage
 - No model of material transport
 - No temporal dependence



**Opportunity
Maneuvers
out of
Sand Trap**

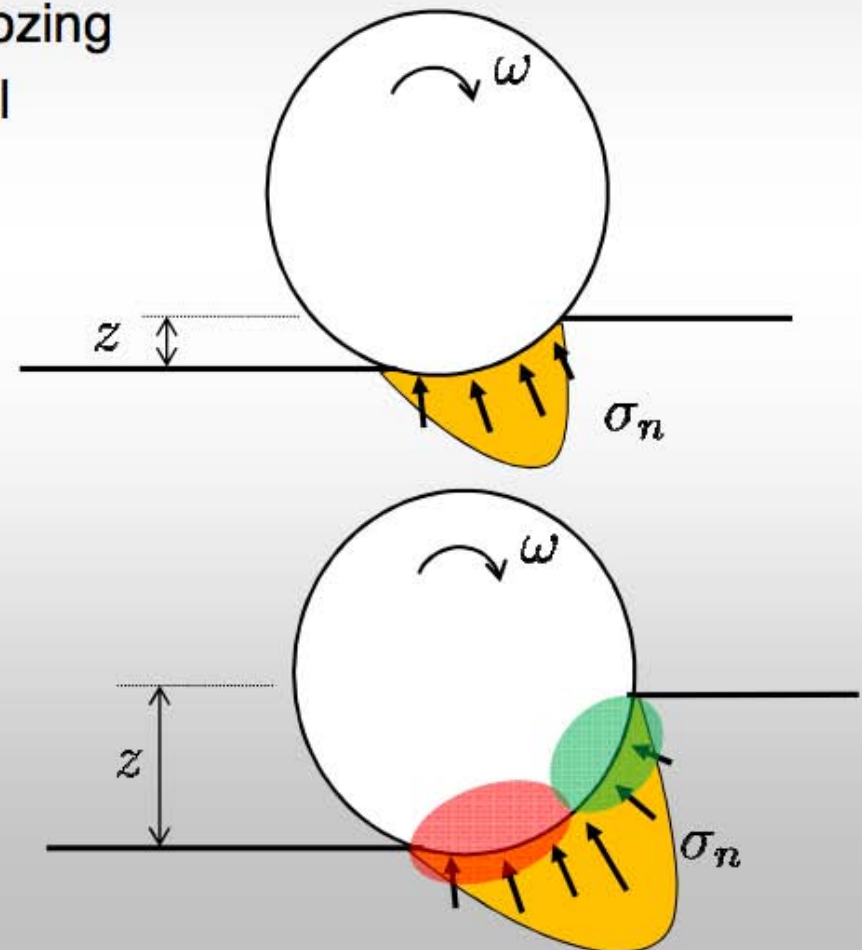
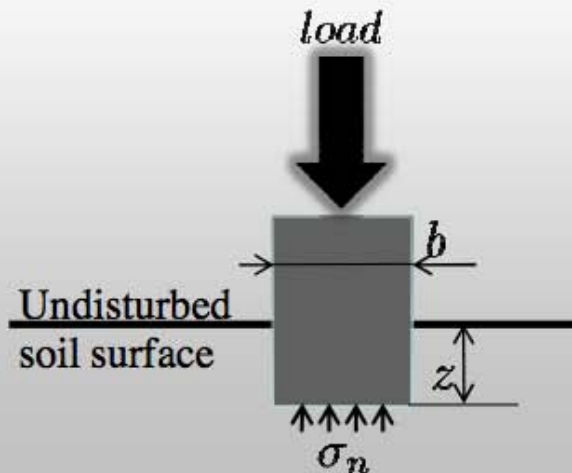


Slipping and Sinking (3)

- Terramechanics theory is not well suited for modeling motion with high sinkage
 - Compaction resistance vs. bulldozing
 - “Flattening” soil vs. “shoving” soil

$$F_x = bR \int_{\theta_b}^{\theta_c} \tau_x(\theta) \cos(\theta) - \sigma_n(\theta) \sin(\theta) d\theta$$

$$\sigma_n = \left(\frac{k_c}{b} + k_\phi \right) z^n$$

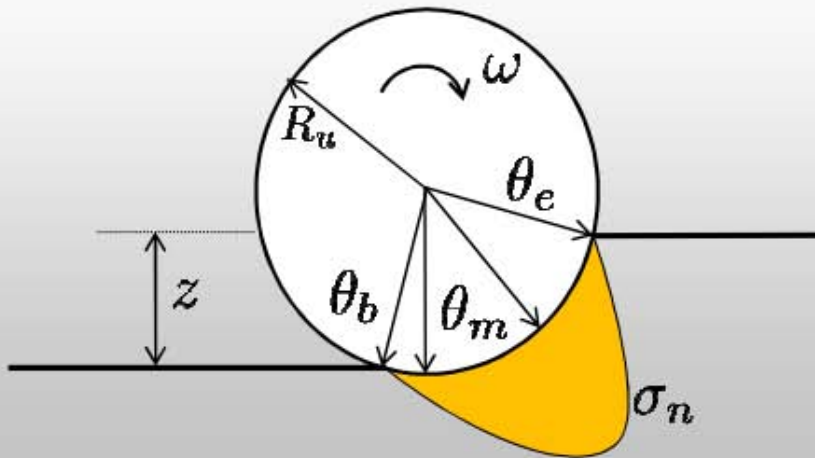




Slipping and Sinking (4)

- Slip ratio defines relative velocity between wheel and soil
 - Dictates shear stress, deformation

$$s_d = 1 - \frac{u}{\omega R}$$

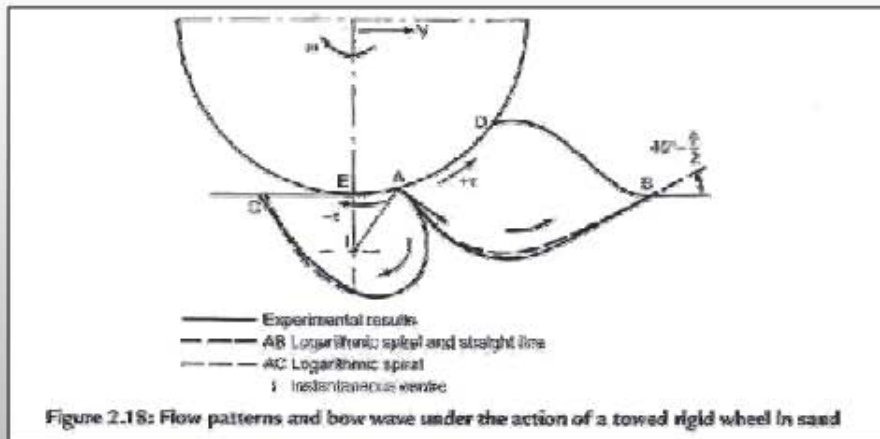




Slipping and Sinking (4)

- Problems with slip ratio
 - Undefined at zero angular velocity
 - Issue for simulation
 - Transition from positive to negative not handled by theory
 - Can occur during free rolling

$$s_d = 1 - \frac{u}{\omega R}$$





Slipping and Sinking (4)

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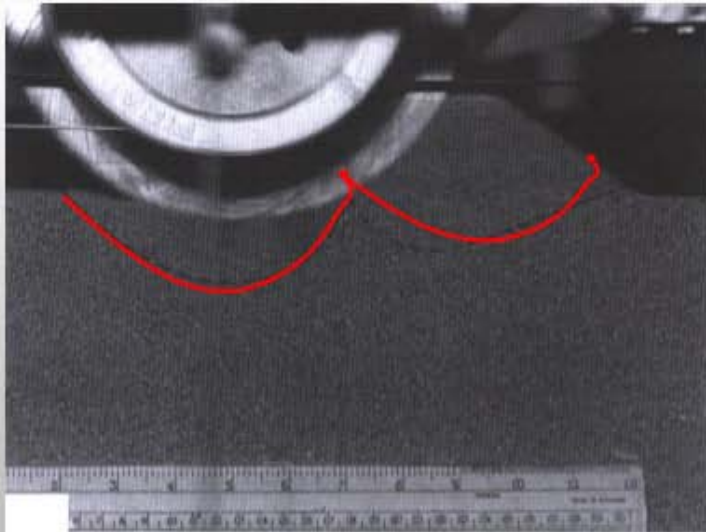


Figure 1.11: Soil flow patterns under a driven rigid wheel in sand



Slipping and Sinking

- Questions (Solutions?)
 - How to model rate dependence?
 - Effect on motion resistance, thrust
 - Momentum formulation of terramechanics relations?
 - How to model temporal effects?
 - Effect on sinkage
 - Model material transport based on grouser geometry?
 - For some soils? All?
 - How to model motion resistance due to high sinkage?
 - Piecewise formulation?
 - “Unified” model of wheel slip?
 - Analysis of particle motion under wheels



Conclusions

- Fundamental limitations of terramechanics modeling
 - Effect of terrain inhomogeneity
 - Soil condition dependence
 - Layering, relative density, moisture content
 - Scale effects
 - Parameter scale dependence (non-intrinsic soil properties)
 - Effects related to slipping and sinking
 - Slip ratio definition
 - Rate dependence
- Issues affect computation, simulation
- Tradeoff between generality and accuracy
- Tradeoff between measurement burden and accuracy

Terramechanics References

- Bekker, M.G, Introduction to Terrain-Vehicle Systems, Ann Arbor, University of Michigan, 1969
- Terzaghi, Theoretical Soil Mechanics, 1943
- Wong, J.Y. Theory of Ground Vehicles 2nd Edition, Canada

