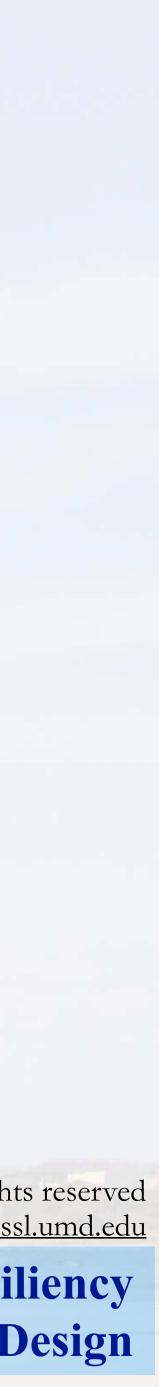
Reliability, Redundancy, and Resiliency

- Review of probability theory
- Component reliability
- Confidence
- Redundancy
- Reliability diagrams
- Intercorrelated failures
- System resiliency
- Resiliency in fixed fleets

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Review of Probability

- Probability that A occurs $0 \le P(A) \le 1$
- Probability that A does not occur $P(\overline{A})$
- Sum of all probable outcomes $P(A) + P(\overline{A}) = 1$



2



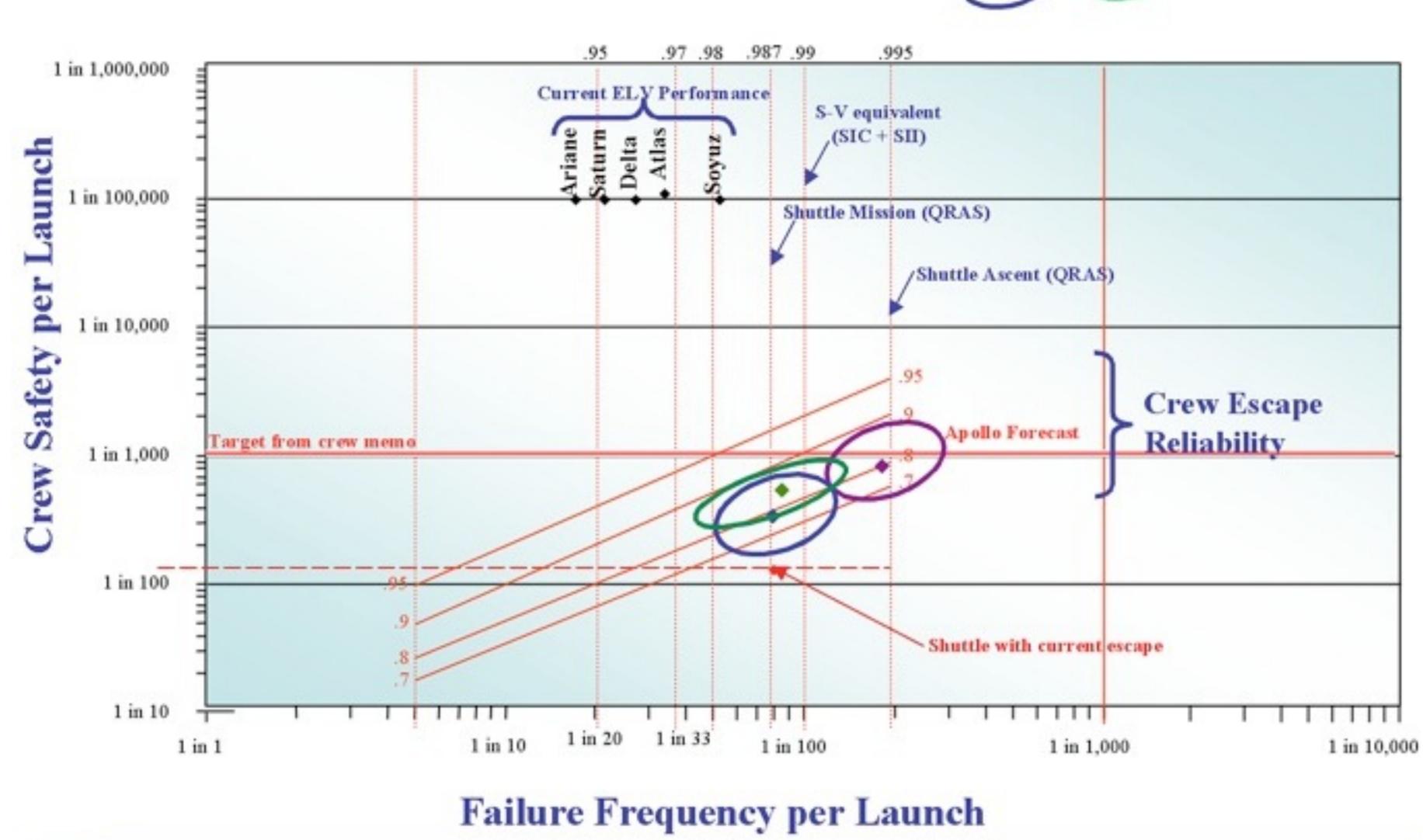
Review of Probability Probability of both A and B occurring $P(A) \cap P(B) = P(A)P(B)$ • Probability of either A or B occurring $P(A) \cup P(B) = 1 - P(\overline{A})P(\overline{B})$ = 1 - [1 - P(A)][1 - P(B)]= P(A) + P(B) - P(A)P(B)





Baseline Results

Results in the reliability / safety space





Simple Overview of Abort Reliability

 $P_{survival} = P_{launch} \cup P_{abort}$ $P_{abort} = 1 - \frac{1 - P_{survival}}{1 - P_{launch}}$ $P_{abort} = 1 - \frac{1 - 0.999}{1 - 0.97} = 0.9667$

 $P_{survival} = 1 - (P_{launch} \cap P_{abort})$ $P_{survival} = 1 - \left[\left(1 - P_{launch} \right) \left(1 - P_{abort} \right) \right]$ $P_{survival} = 0.999; P_{launch} = 0.97$

5





Expected Value Theory

- Probability of an outcome does not determine value of the outcome
- of outcome



Combine probabilities and values to determine expected value

$EV = P(A)U(A) + P(\overline{A})U(\overline{A})$

6



Expected Value Example

$$P(win) = 1 / \frac{4}{6!}$$

• Assume \$10,000,000 jackpot

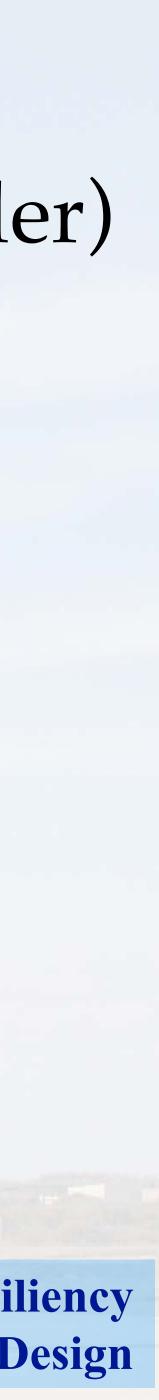
$EV = (7.151 \times 10^{-8})(10^{7}) + (1)(-1) = -\0.39

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• Maryland State Lottery - pick six numbers out of 49 (any order)

 $\frac{49!}{143!} = \frac{1}{13,983,816}$



Utility Theory

- fully quantify utility
- exceeds negative utility of small investment: *risk proverse*
- Imagine lottery where \$1000 buys 1:500 chance at \$1M -EV=(.998)(-\$1000)+(.002)(\$.999M)=\$1000 risk adverse

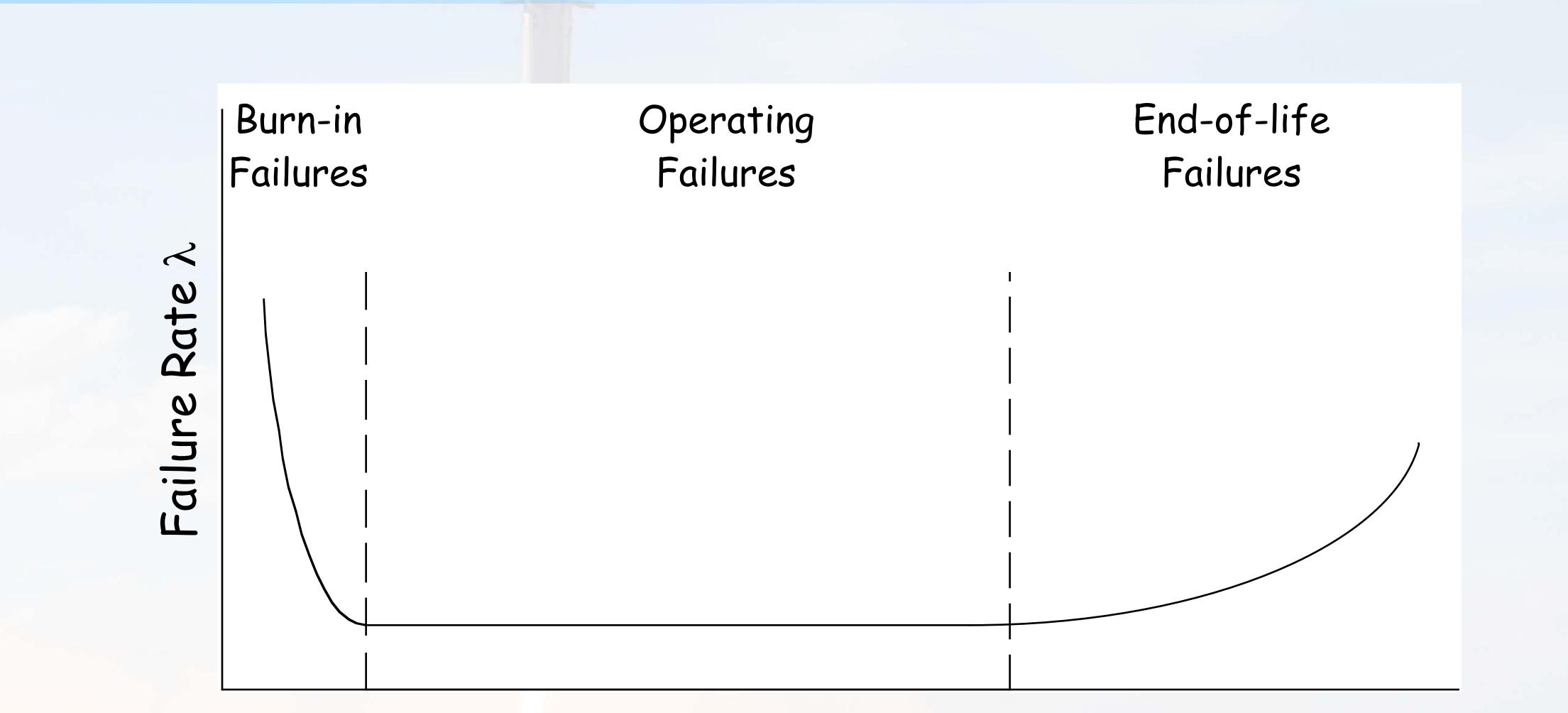


• Numerical rating from expected value calculations does not

• Lottery example previously: utility of (highly unlikely) win



Component Reliability





Time



Reliability Analysis

failing per unit time

The trend of operating units with time is then

 $\int_0^t \lambda(\tau) \, d\tau = -\int_1^{R(t)} \frac{dR(\tau)}{R(\tau)}$



Failure rate is defined as fraction of currently operating units

 $\lambda(t) = -\frac{1}{R(t)}\frac{d}{dt}R(t)$

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Reliability Analysis (continued)

- Evaluation of the definite integrals gives
- Assuming that λ is constant over the operating lifetime,
 - $R(t) = \exp\left|-\right|$
- as mean time between failures)



$\int_0^t \lambda(\tau) \, d\tau = -\ln[R(t)]$

$$\int_0^t \lambda(\tau) d\tau = e^{-\lambda t}$$

Ш

• At t=1/ λ , 1/e of the original units are still operating (defined



Reliability Analysis (continued)

- failure rate λ :
 - $R(t) = e^{-\frac{t}{MTBF}}$
- where MTBF=mean time between failures • For a mission duration of N hours, estimate of component reliability becomes

R(mission)



• Frequently assess component reliability based on reciprocal of

$$=e^{-\frac{N}{MTBF}}$$





Verifying a Reliability Estimate

- it 20 times without a failure?
- What is the probability Q that you will see one or more failures?
 - R=.99 P=.8179 Q=.1821
 - R=.95 P=.3584 Q=.6416
 - -R=.90 P=.1216 Q=.8784



• Given a unit reliability of R, what is the probability P of testing





Confidence

you should have seen worse results than you did

P(observed and better outcomes) + C = 1



• The confidence C in a test result is equal to the probability that





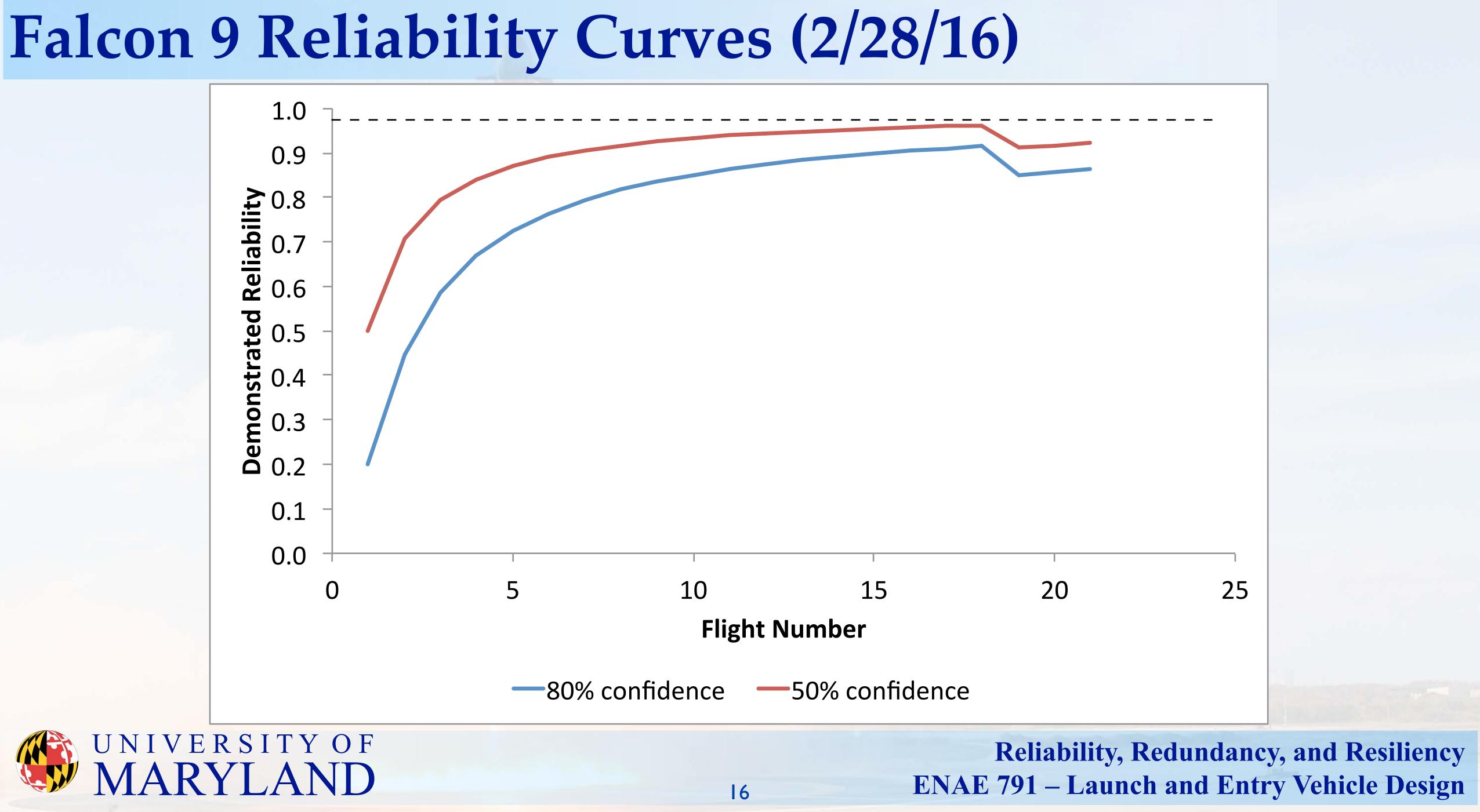
Example of Confidence - Saturn V • 13 vehicle flights without a failure • Assume a reliability value of R

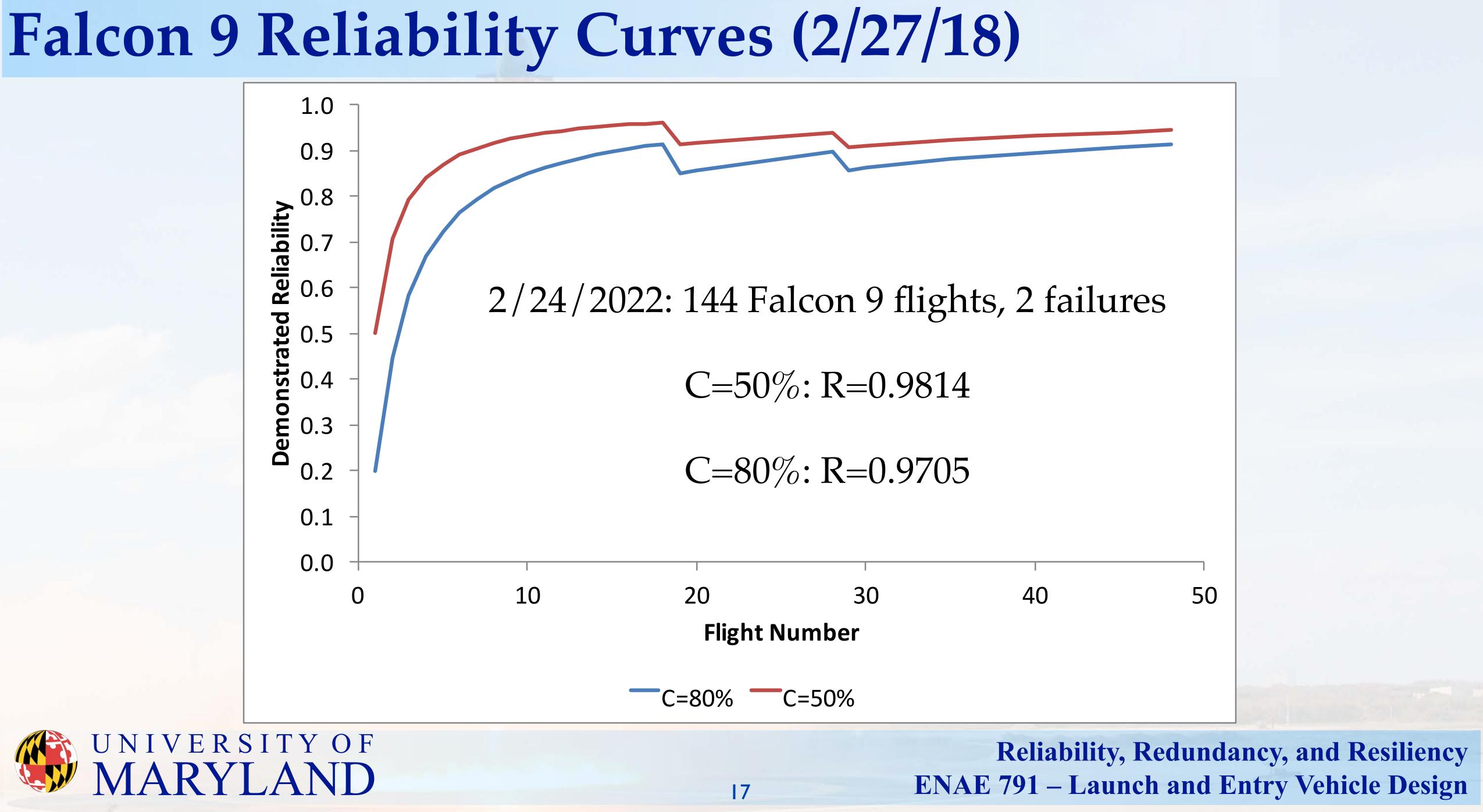
- Valador report (slide 4) listed 95% reliability
 - $C = 1 R^{13} = 1 0.95^{13} = 48.7\%$
- What reliability could we cite with 80% confidence? $R = (1 - C)^{1/13} = 0.2^{0.07692} = 88.4\%$



- $R^{13} + C = 1$

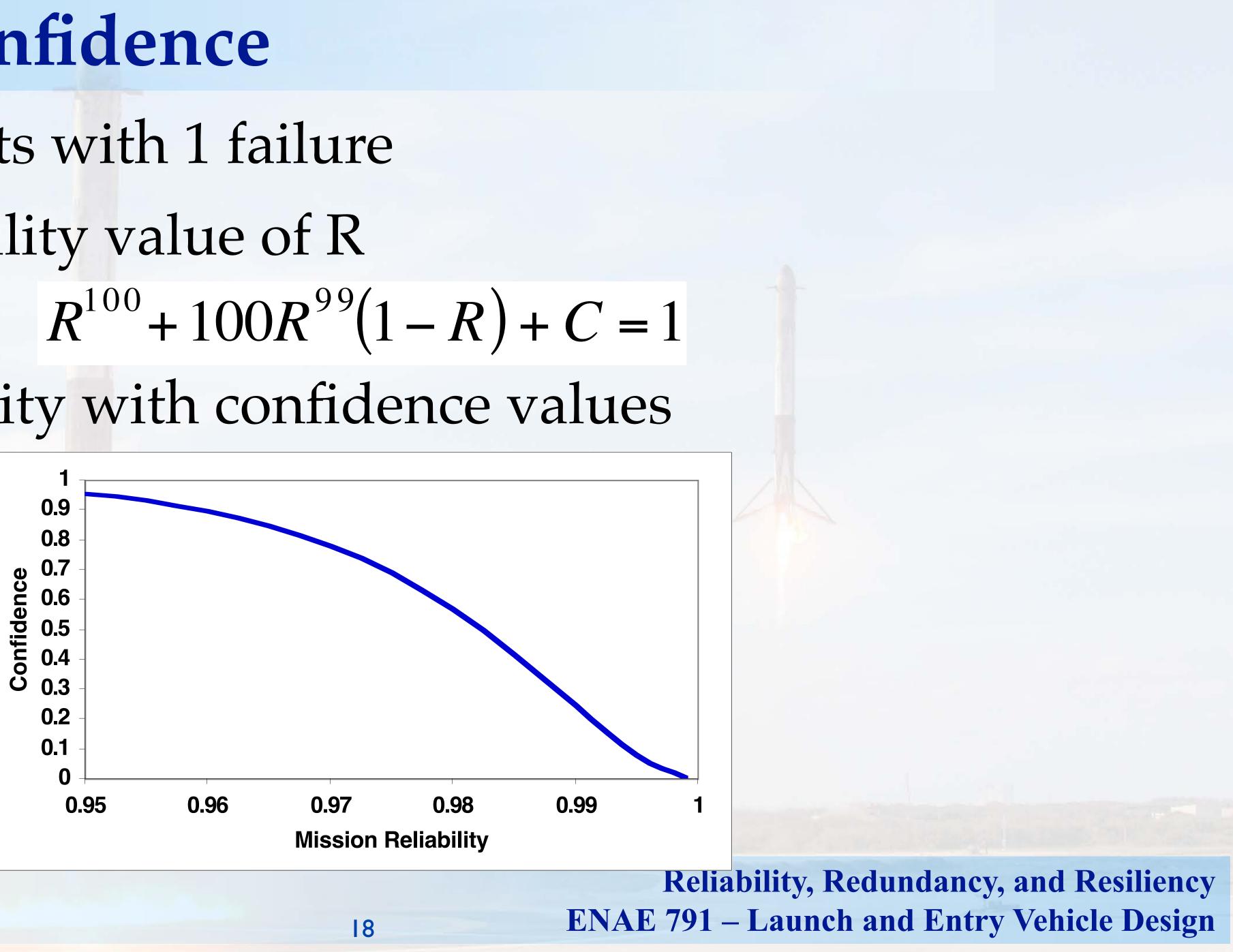






Example of Confidence

- 100 vehicle flights with 1 failure
- Assume a reliability value of R
- Trade off reliability with confidence values





Definition of Redundancy

• Probability of k out of n units working = (number of combinations of k out of n) x P(k units work) x P(n-k units fail)

 $P\binom{k}{n} = \frac{n!}{k!(n-k)!} P^{k} (1-P)^{n-k}$





Redundancy Example 3 parallel computers, each has reliability of 95%: • Probability all three work $P(3) = P^3 = (.95)^3 = .8574$ • Probability exactly two work $P(2) = 3P^2(1-P) = 3(.95)^2(.05) = .1354$ Probability exactly one works $P(1) = 3P(1-P)^2 = 3(.95)(.05)^2 = .0071$ Probability that none work $P(0) = (1 - P)^3 = (.05)^3 = .0001$ UNIVERSITY OF 20



Redundancy Example 3 parallel computers, each has reliability of 95%: • Probability all three work P(3) = .8574 Probability at least two work P(3) + P(2) = .8574 + .1354 = .9928• Probability at least one works P(3) + P(2) + P(1) = .9928 + .0071 = .99999

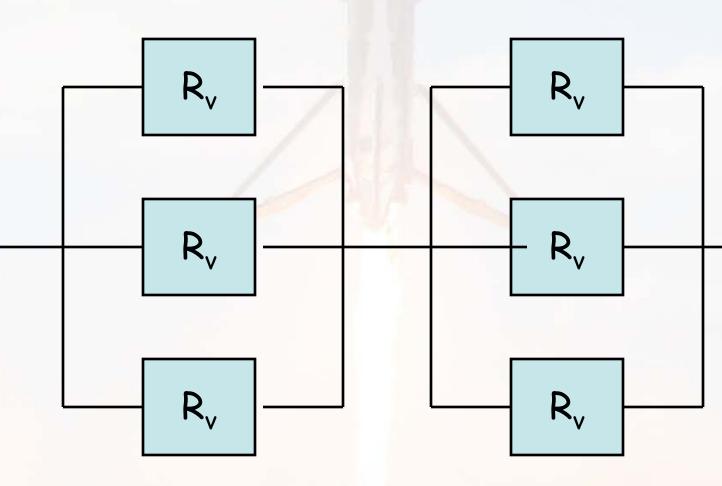
 Probability that none work $P(0) = (1 - P)^3 = (.05)^3 = .0001$

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Reliability Diagrams

- Example of Apollo Lunar Module ascent engine
- Three valves in each of oxidizer and fuel lines
- One in each set of three must work
- $R_v = 0.9 R_{system} = .998$



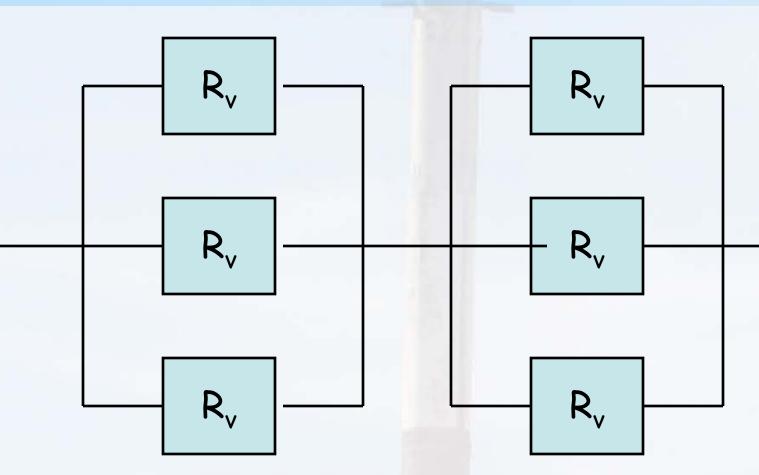


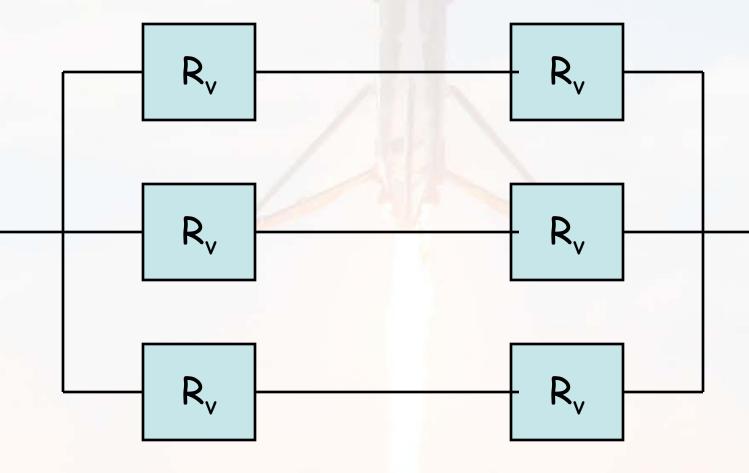
ent engine 1el lines

$R_{system} = \left[1 - (1 - R_v)^3\right]^2$



Reliability Diagrams (how not to...)







$$R_{system} = \left[1 - (1 - R_v)^3\right]^2$$
$$R_v = 0.9 - R_{system} = .998$$

 $R_{system} = \left[1 - (1 - R_v^2)^3\right]$

 $R_v = 0.9 - R_{system} = .993$

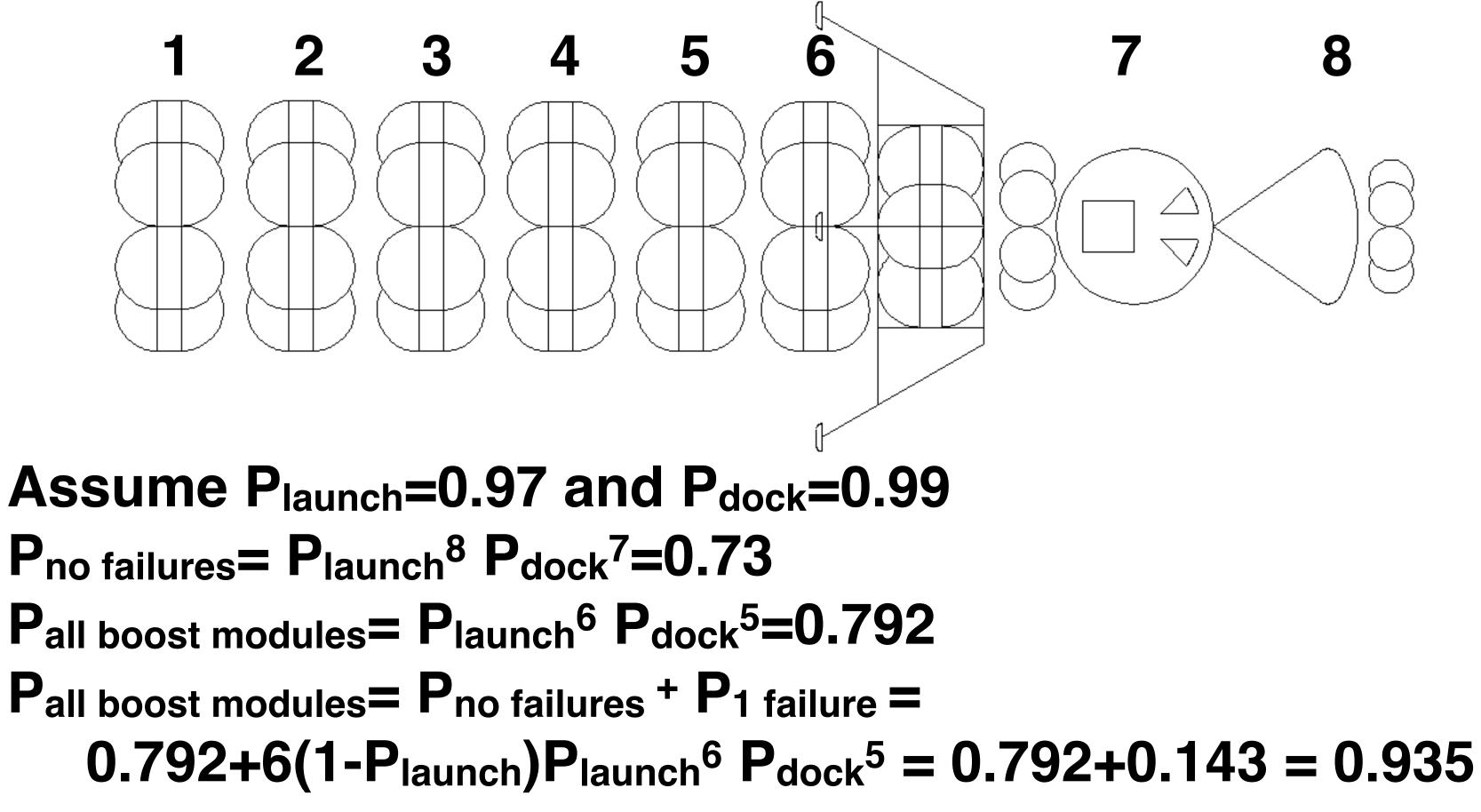




Moon the Return to ow-Cost

Earth Departure Configuration

8 launches and 7 dockings required to start mission



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Moon the to Return Low-Cost

Spares - The Big Picture

- each of 10 missions
- crew module for each mission
- Assume composite reliability =0.97(0.99)=0.96
 - $P(n \mid n) = p^n$
 - $P(n \mid n+1) = r$
 - $P(n \mid n+2) = -$

 $P(n \mid n+m) =$

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Have to get 6 functional boost modules for

Have to get functional lunar vehicle and

$$\frac{n(p^{n-1})(1-p)(p)}{2}$$

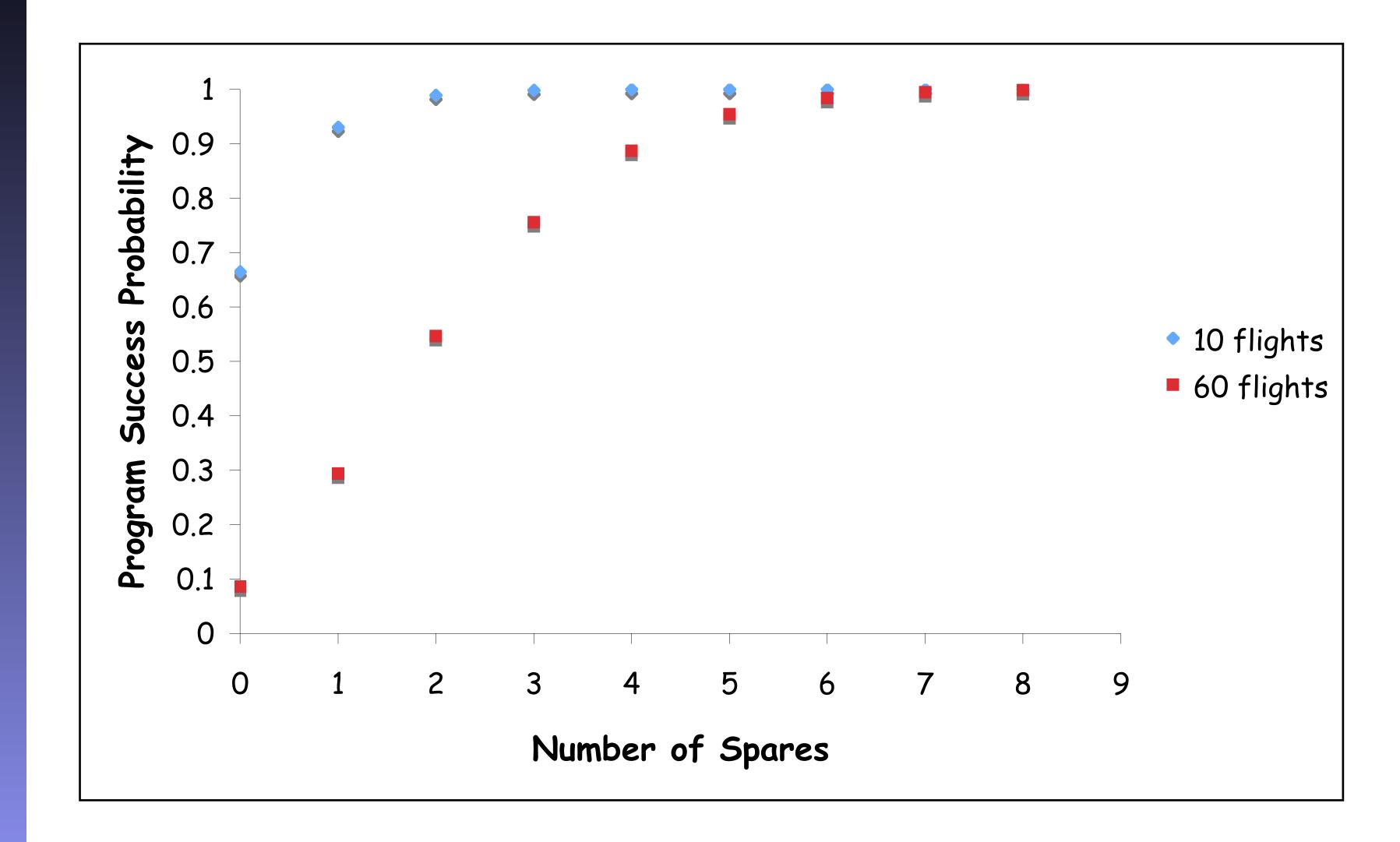
$$\frac{n(n-1)}{2}(p^{n-2})(1-p)^2(p)$$

$$\frac{n!}{(n-m)!m!}(p^{n-m})(1-p)^m(p)$$



Moon Return to the Low-Cost

Effect of Fleet Spares on Program



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Moon the to Return Low-Cost

Spares Strategy Selection

- VSE approach:
 - 2 launches and 1 dock: P=(0.97)²(0.99)=0.931 – Program reliability over 10 missions:
- $0.931^{10} = 0.492$
- Goal: meet VSE program reliability
 - 1 lander and 1 CEV spare p=0.9308 each
 - 2 boost module spares p=0.5464
 - Program reliability: (0.9308)²(0.5464)=0.473
- Alternate goal: 85% program reliability
 - 2 lander, 2 CEV, 4 BM spares: $(0.9893)^2(0.8871)=0.868$
 - 1 lander, 1 CEV, 6 BM spares: $(0.9308)^2(0.9838)=0.852$

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Intercorrelated Failures

- Some failures in redundant systems are common to all units
 - Software failures
 - "Daisy-chain" failures
 - Design defects
- Following a failure, there is a probability f that the failure causes a total system failure





Intercorrelated Failure Example 3 parallel computers, each has reliability of 95%, and a 30%

- intercorrelated failure rate:
- Probability all three work
 - $P(3) = P^3 = (.95)^3 = .8574$
- Probability exactly two work (one failure)
 - Probability the failure is benign (system works)
 - $P(2_{safely}) = .7(.1354) = .0948$ – Probability of intercorrelated failure (system dies)

UNIVERSITY OF MARYLAND $P(2_{system \ failure}) = .3(.1354) = .0406_{ity, Redundancy, and Resiliency}$

 $P(2) = 3P^2(1-P) = 3(.95)^2(.05) = .1354$



Intercorrelated Failure Example (continued from previous slide) • Probability exactly one works (2 failures) $P(1) = 3P(1-P)^2 = 3(.95)(.05)^2 = .0071$ – Probability that both failures are benign $P(1_{safely}) = .7^2(.0071) = .0035$ Probability that a failure is intercorrelated



- $P(1_{system \ failure}) = (1 .7^2)(.0071) = .0036$



Redundancy Example with Intercorrelation

- 3 parallel computers, each has reliability of 95%, and a 30%intercorrelated failure rate:
- Probability all three work

P(3) = .8574

- Probability at least two work
- Probability at least one works



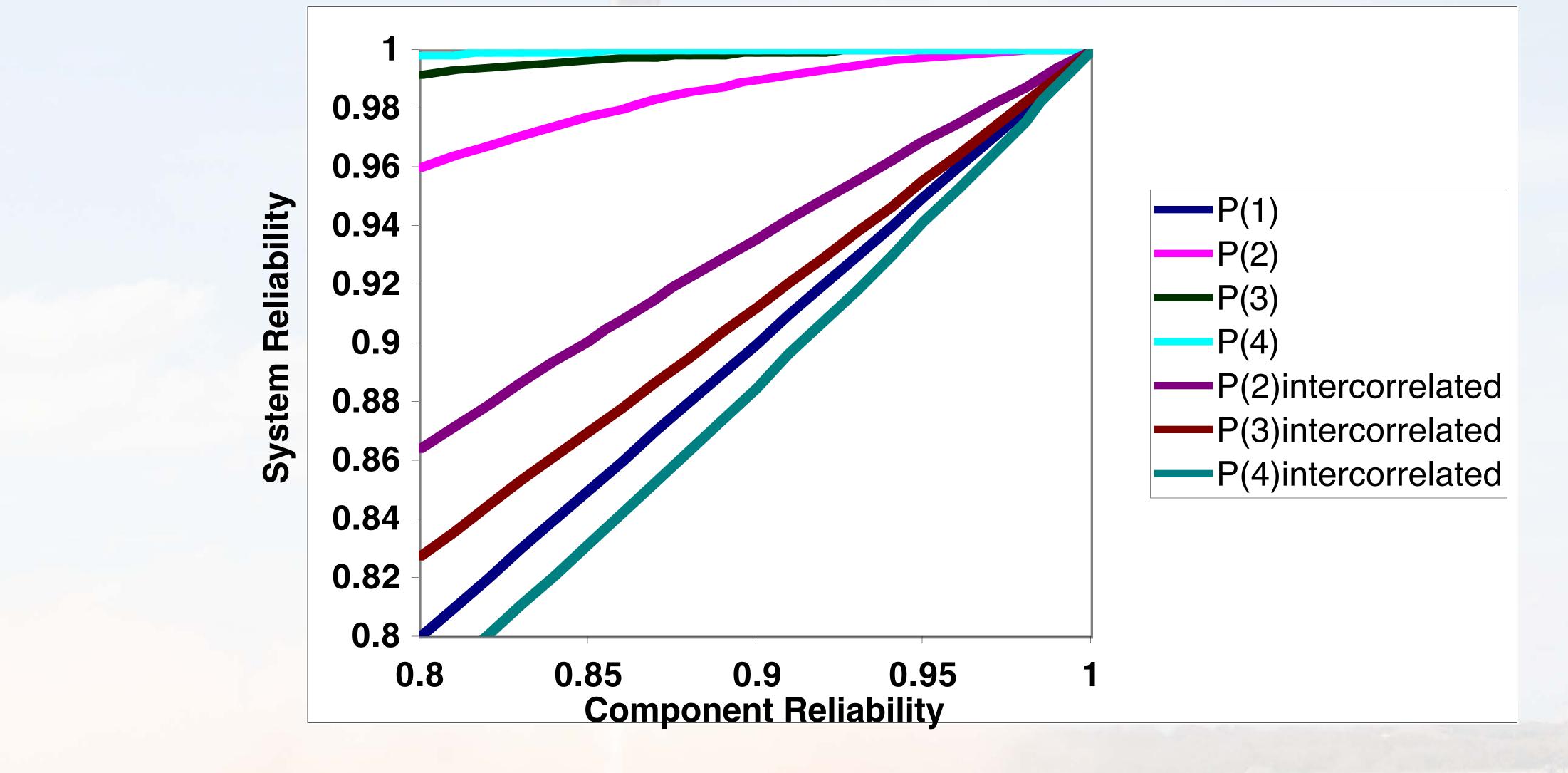
= .8574 + .0948 = .9522 (*was* .9928)

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= .9522 + .0035 = .9557 (*was* .9999)



System Reliability with 30% Intercorrelation







Probabilistic Risk Assessment

- event)
- Estimation of the consequences associated with each combination.

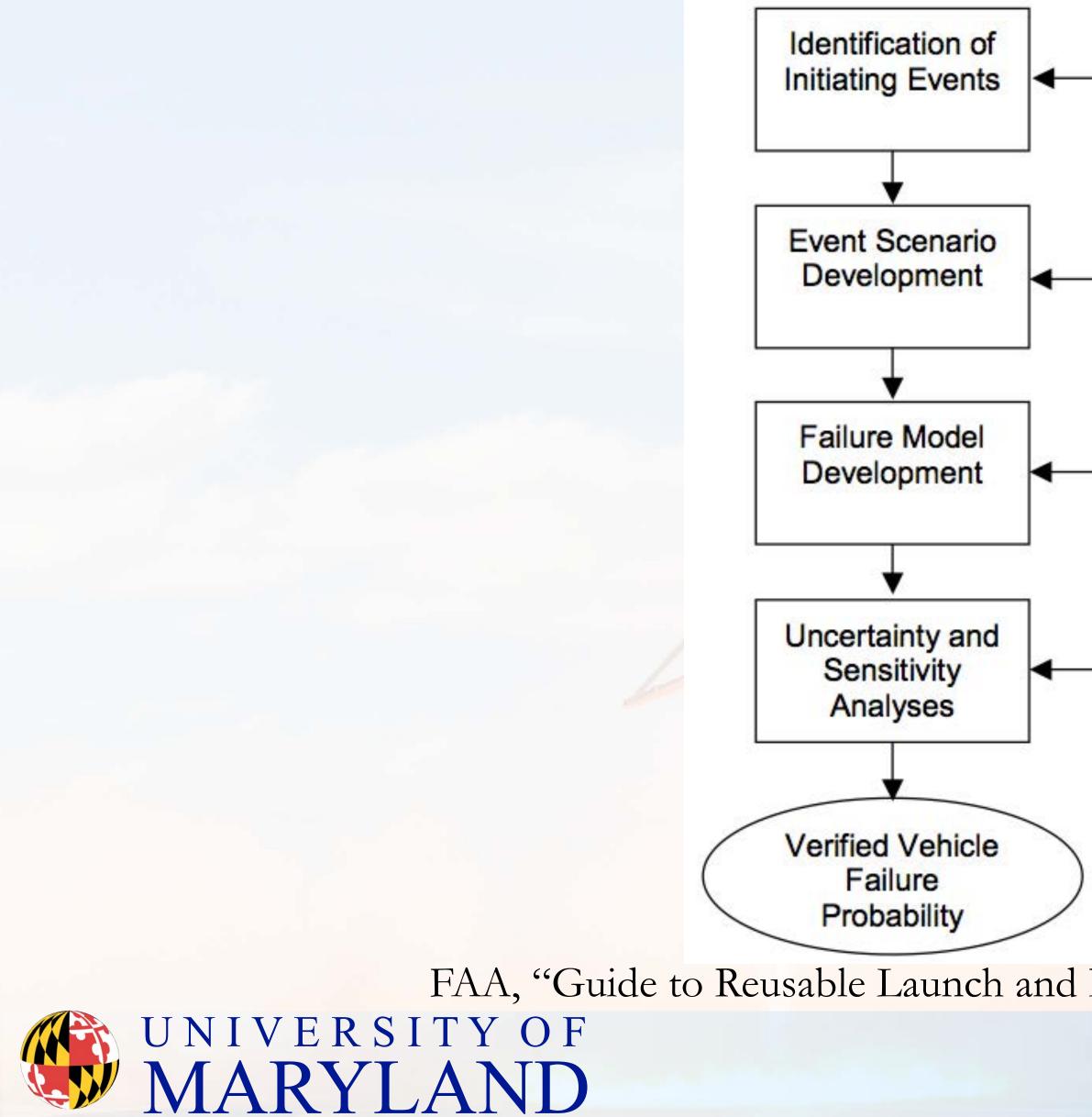


• Identification and delineation of the combinations of events that, if they occur, could lead to an accident (or other undesired

• Estimation of the chance of occurrence for each combination



PRA Process Flowchart



Mission and System Descriptions, Hazard Analyses

System Reliability Analyses, Historical Data

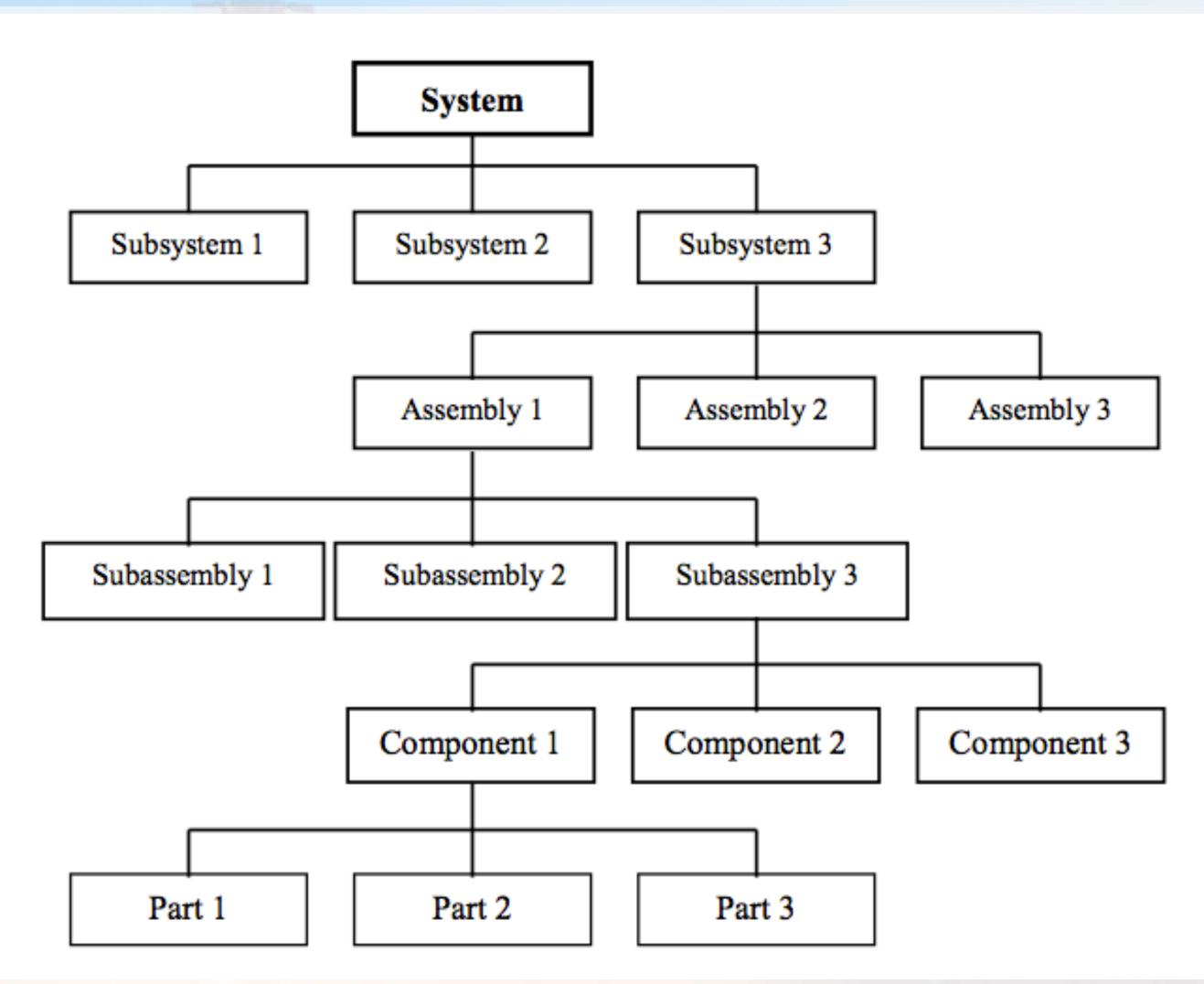
System and Subsystem Reliability Analyses, Historical & Verification Data

Monte Carlo Simulation, Historical & Verification Data

FAA, "Guide to Reusable Launch and Reentry Vehicle Reliability Analysis" April 2005



System Breakdown Chart



FAA, "Guide to Reusable Launch and Reentry Vehicle Reliability Analysis" April 2005 UNIVERSITY OF MARYLAND 35 ENAE 791 – Launch and Entry Vehicle Design



Failure Modes and Effects Analysis

System: Upper Stage Propulsion System

Mission: Satellite Delivery to GEO

Phase: Orbital Insertion

Ref. Drawing: GTYD-1002B008

ID	Item	Failure Modes	Failure Causes	Failure Effects	Risk Assessment Sev. Prob. Risk			Detection Methods and Controls
2.0	Combustion Chamber	a. Coolant loss b. Seal failure	 a. Manufact. process problem b. Cyclic fatigue 	 a. Reduced performance, burn-through, possible crash and injury to involved public b. Reduced performance 	a.II b.III	a.C b.D	a.6 b.14	a. Inspect welds b. Seal redundancy

FAA, "Guide to Reusable Launch and Reentry Vehicle Reliability Analysis" April 2005 UNIVERSITY OF MARYLAND **Reliability, Redundancy, and Resiliency ENAE 791 – Launch and Entry Vehicle Design** 36

FAILURE MODES, EFFECTS, AND CRITICALITY ANALYSIS WORKSHEET

Sheet 1 of 20

Prepared by: John Smith

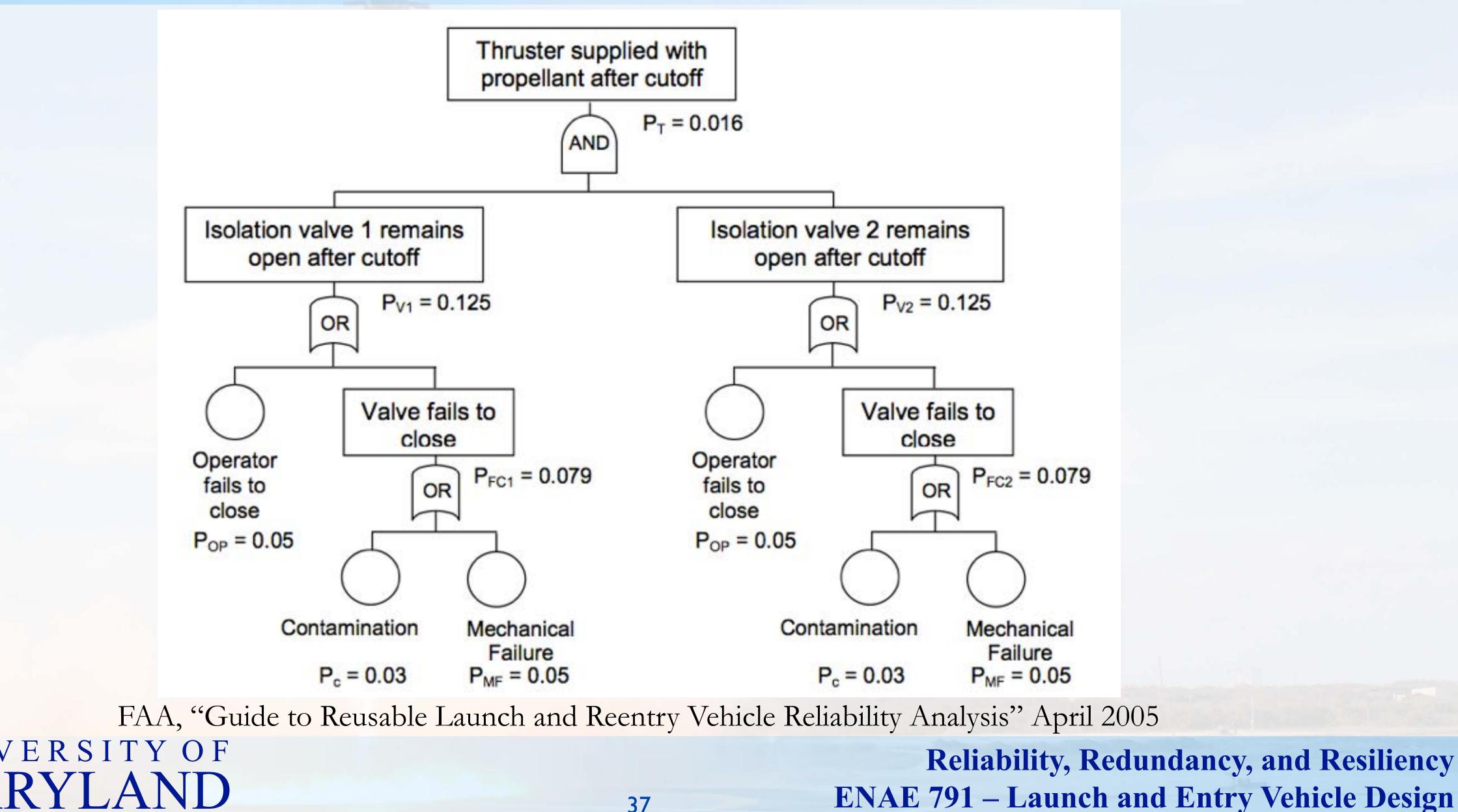
Reviewed by: Janet Jones

Approved by: Sharon Jackson

Date: January 2, 2004



Fault Tree Analysis

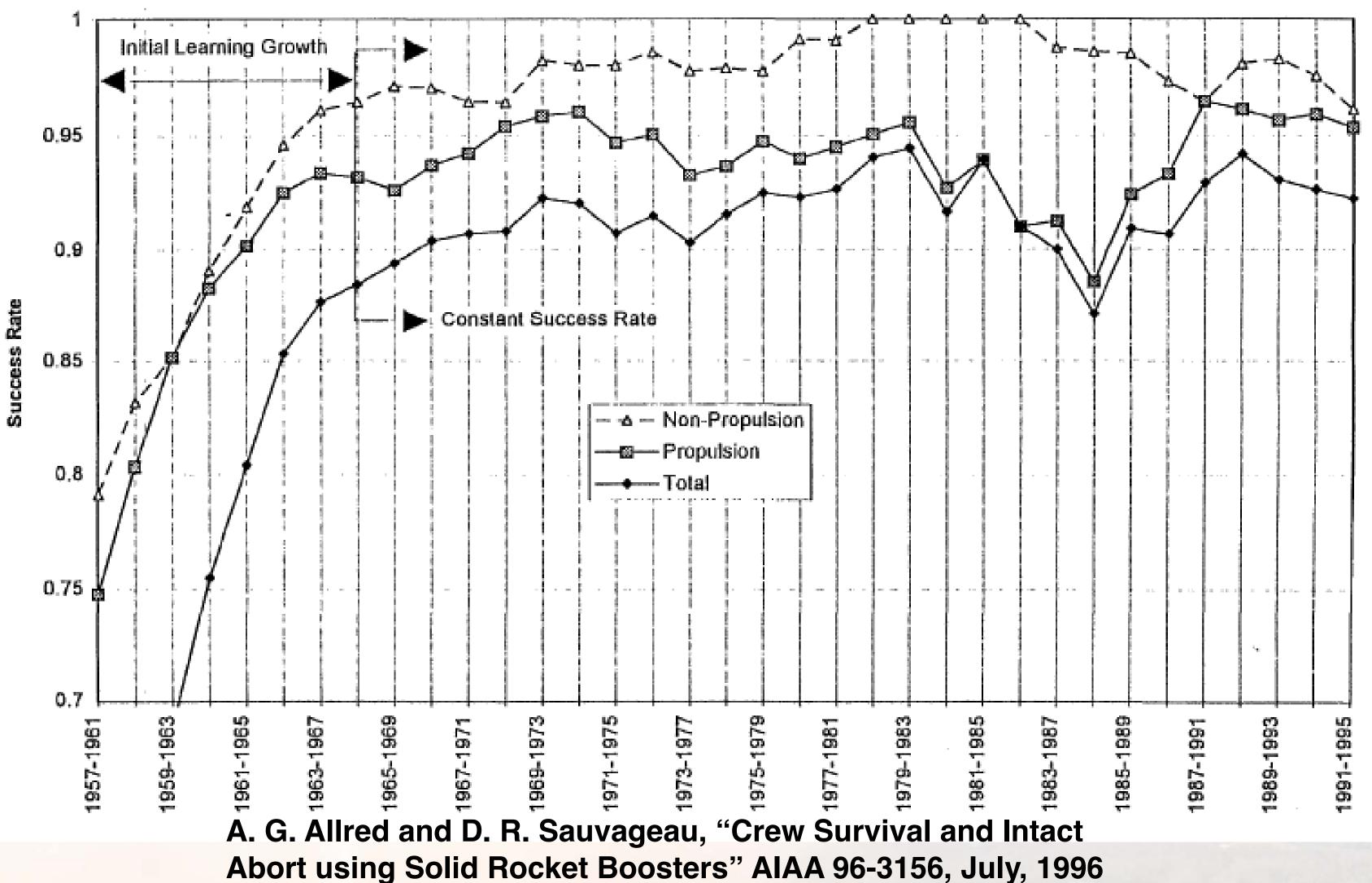


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U.S. Launch Reliability - 5 yr. rolling avgs.







LV Subsystem Failures 1984-2004

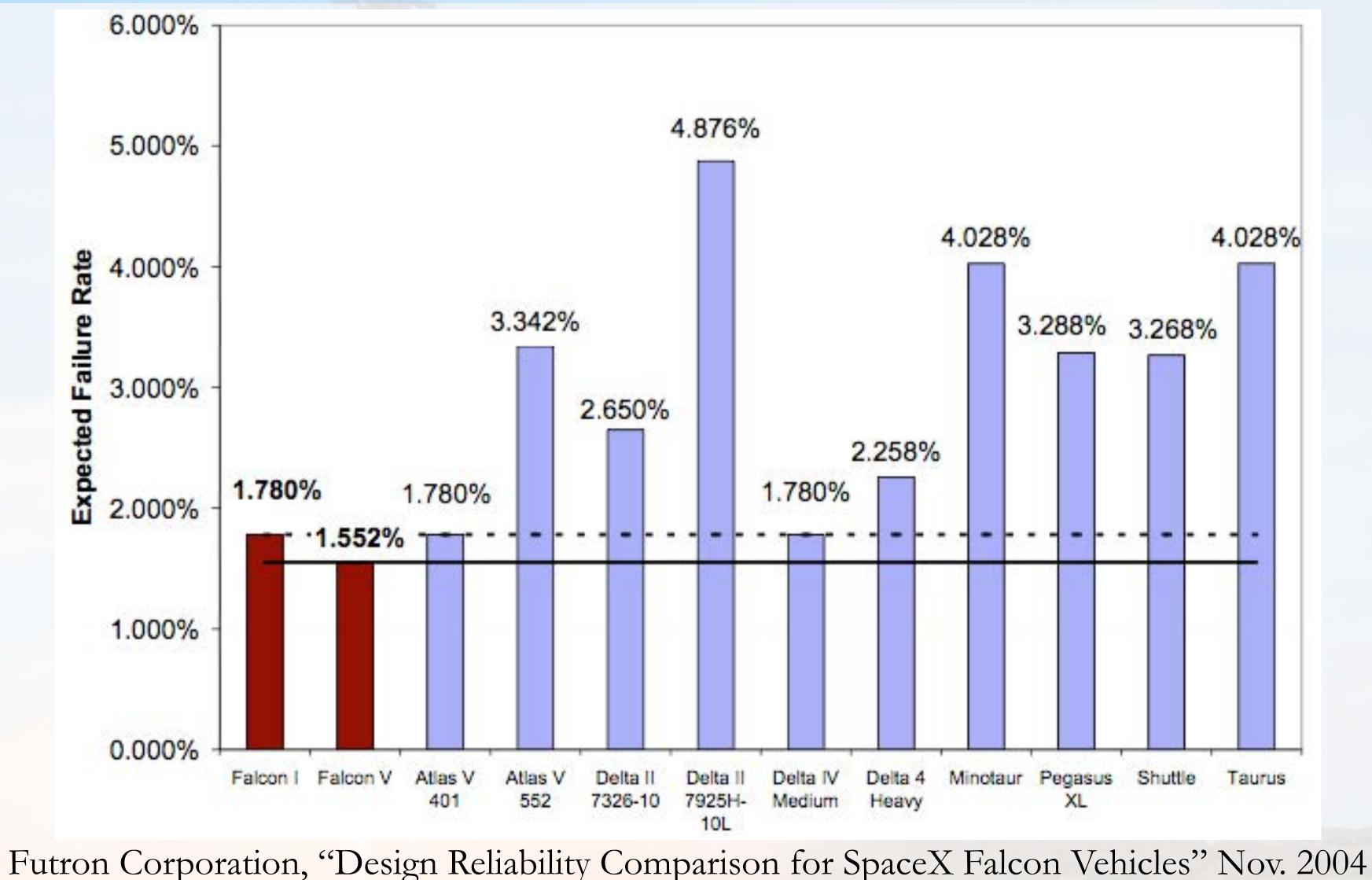
Failure Type	Failures	Total Events	Individual Percent Failure Rate	
Liquid Propulsion (Start)	3	1255	0.239%	
Liquid Propulsion (In-flight)	3	1255	0.239%	
Total Liquid Failure	6	1255	0.478%	
Solid Propulsion (Shell)	4	1831 (all solids)	0.218%	
Solid Propulsion (TVC)	3	571 (TVC only)	0.525%	
Solid Propulsion with TVC (TVC and			0 74004	
Shell Failure Modes)			0.743%	
Stage, Booster, and Payload Separations	6	2577	0.233%	
Fairing Separation	1	357	0.280%	
Small Solid Booster Separations	1*	1165	0.086%	
Electrical	2	470	0.426%	
Avionics	2	470	0.426%	
Other	1	470	0.213%	

Futron Corporation, "Design Reliability Comparison for SpaceX Falcon Vehicles" Nov. 2004





Expected Failure Rates from Prop/Sep

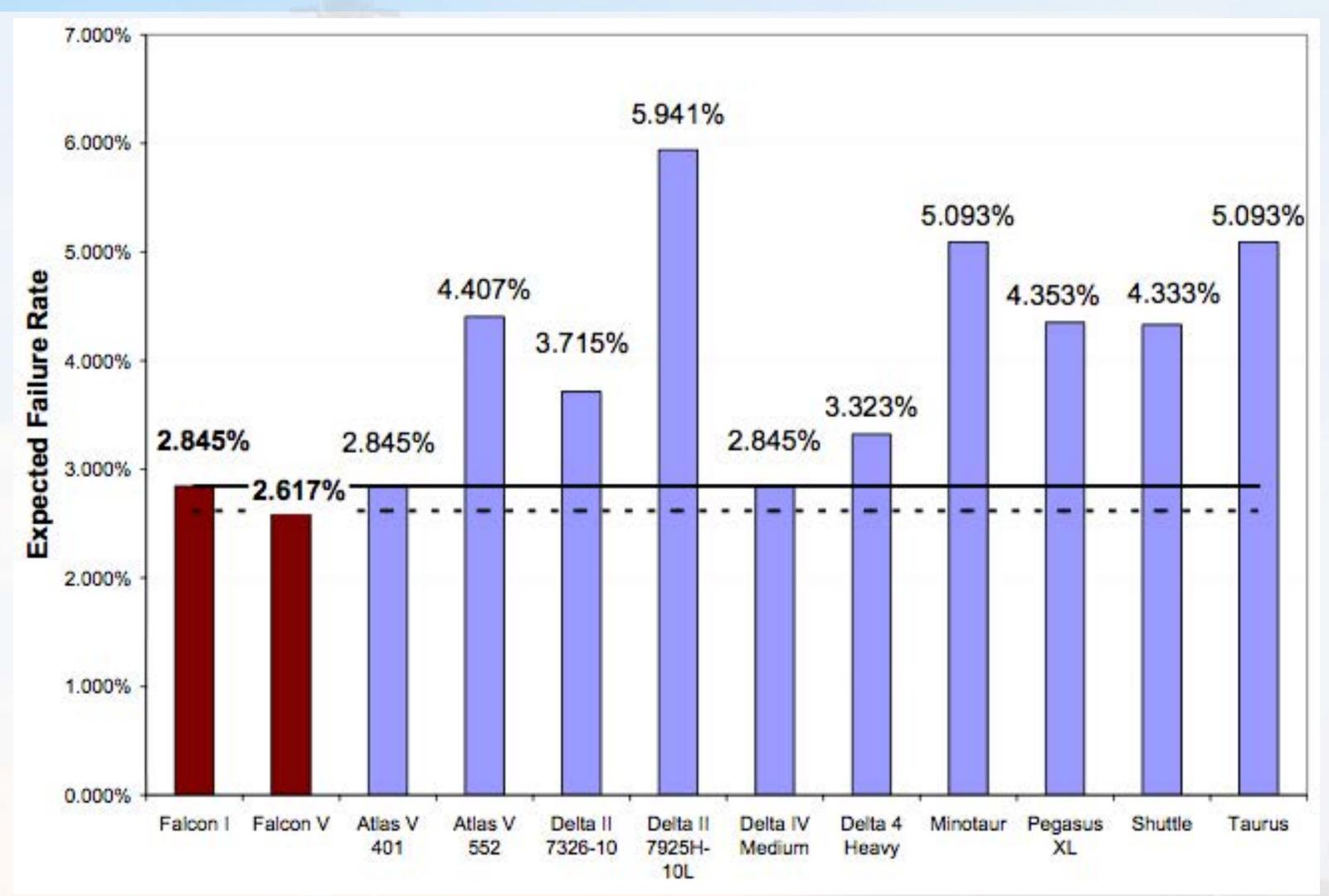


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Futron Corporation, "Design Reliability C UNIVERSITY OF MARYLAND



Failure Rates from All Causes



Futron Corporation, "Design Reliability Comparison for SpaceX Falcon Vehicles" Nov. 2004 UNIVERSITY OF MARYLAND **Reliability, Redundancy, and Resiliency ENAE 791 – Launch and Entry Vehicle Design** 41



Concept of System Resiliency

- Initial flight schedule + + + + + + + + +
- Hiatus period following a failure + H
- Backlog of payloads not flown in hiatus + + +
- Surge to fly off backlog + ₩
- Resilient if backlog is cleared before next failure occurs (on average)







Resiliency Variables

- r nominal flight rate, flts/yr
- d down time following failure (yrs)
- k fraction of flights in backlog retained
- S surge flight rate / nominal flight rate
- m average/expected flights between failures
- rd number of missed flights
- krd number of flights in backlog
- (S-1)r backlog flight rate





Definition of Resiliency

- Example for Delta launch vehicle
- r = 12 flts/yr
- d = 0.5 yrs
- k = 0.8
- S = 1.5
- m = 30
- Srkd/(S-1) = 14.4 < 30 system is resilient!



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Srkd $\frac{1}{S-1} \le m$



Shuttle Resiliency (post-Challenger)

- r = 9 flts/yr
- d = 2.5 yrs
- k = 0.8
- S = .67 (6 flts/yr)
- m = 25
- System has negative surge capacity due to reduction in fleet measures



size - cannot ever recover from hiatus without more extreme



Modified Resiliency

- k' retention rate of all future payloads $(k' \leq S \text{ for } S < 1)$
- New governing equation for resiliency:

• Implication for shuttle case: ✓ k<.417 to achieve modified resiliency



$\frac{Srk'd}{S-k'} \le m$

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Shuttle Resiliency (post-Columbia)

- r = 5 flts/yr
- d = 2 yrs
- S = .8 (4 flts/yr)
- m = 56 (average missions/failure)
- Modified resiliency requires $k' \le 0.7$ for all future payloads



