Thermal Systems Design

- Fundamentals of heat transfer
- Radiative equilibrium
- Surface properties
- Non-ideal effects
  - Internal power generation
  - Environmental temperatures
- Conduction
- Thermal system components

Classical Methods of Heat Transfer

- Convection
  - Heat transferred to cooler surrounding gas, which creates currents to remove hot gas and supply new cool gas
  - Don't (in general) have surrounding gas or gravity for convective currents
- Conduction
  - Direct heat transfer between touching components
  - Primary heat flow mechanism internal to vehicle
- Radiation
  - Heat transferred by infrared radiation
  - Only mechanism for dumping heat external to vehicle

Ideal Radiative Heat Transfer

Planck's equation gives energy emitted in a specific frequency by a black body as a function of temperature

$$e_{\lambda b} = \frac{2\pi h C_0^2}{\lambda^5 \left[\exp\left(\frac{-hC_0}{\lambda k T}\right) - 1\right]}$$

(Don't worry, we won't actually use this equation for anything…)

- Stefan-Boltzmann equation integrates Planck's equation over entire spectrum

$$P_{rad} = \sigma T^4$$

$$\sigma = 5.67x10^{-8} \frac{W}{m^2 \, {}^\circ K^4}$$

("Stefan-Boltzmann Constant")

Thermodynamic Equilibrium

- First Law of Thermodynamics

$$Q - W = \frac{dU}{dt}$$

heat in -heat out = work done internally

- Heat in = incident energy absorbed
- Heat out = radiated energy
- Work done internally = internal power used (negative work in this sense - adds to total heat in the system)

Radiative Equilibrium Temperature

- Assume a spherical black body of radius r
- Heat in due to intercepted solar flux

$$Q_{in} = I_s \pi r^2$$

- Heat out due to radiation (from total surface area)

$$Q_{out} = 4\pi r^2 \sigma T^4$$

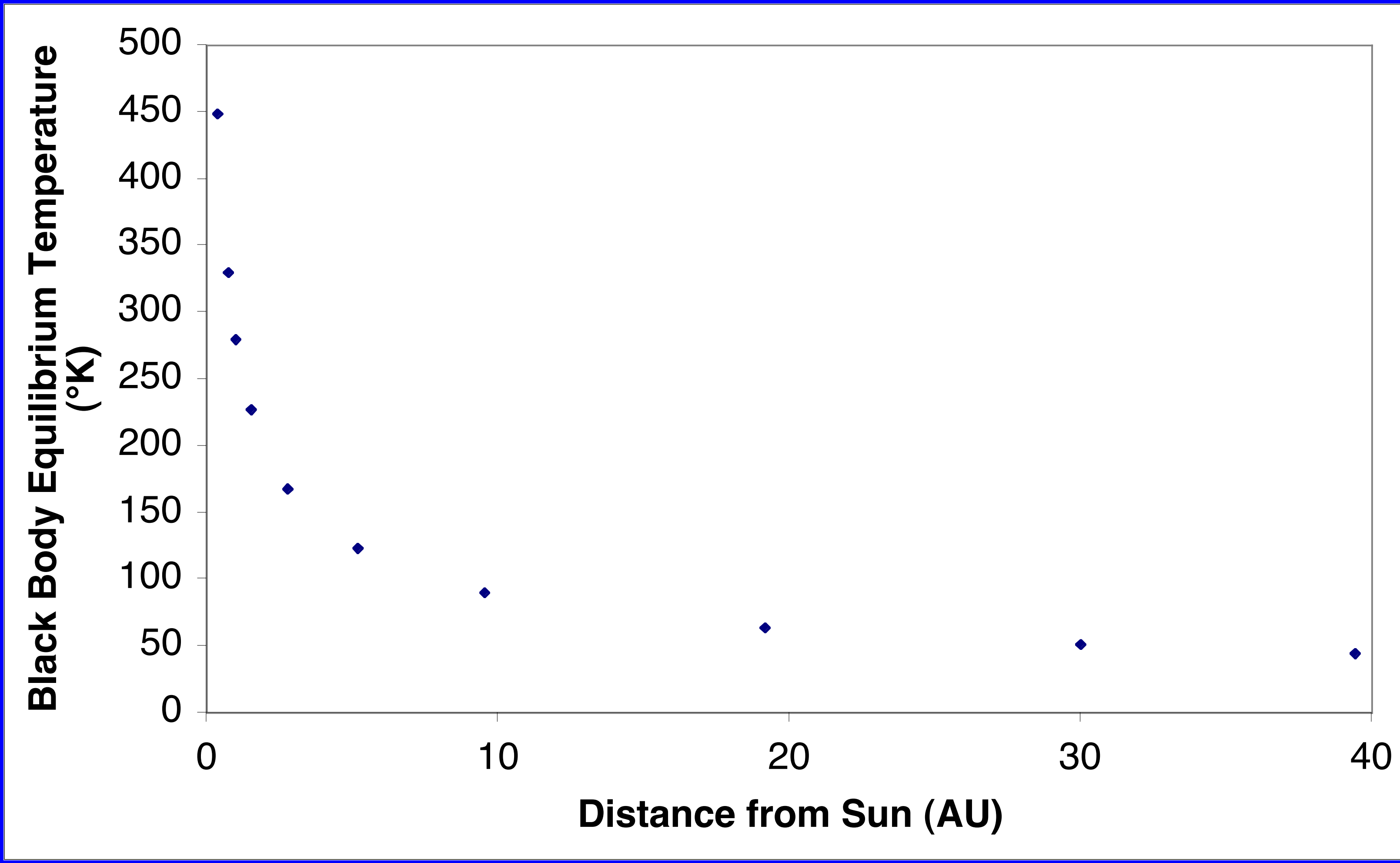
- For equilibrium, set equal

$$I_s \pi r^2 = 4\pi r^2 \sigma T^4 \Rightarrow I_s = 4\sigma T^4$$

- 1 AU: I_s=1394 W/m^2; T_{eq}=280°K

$$T_{eq} = \left(\frac{I_s}{4\sigma}\right)^{1/4}$$

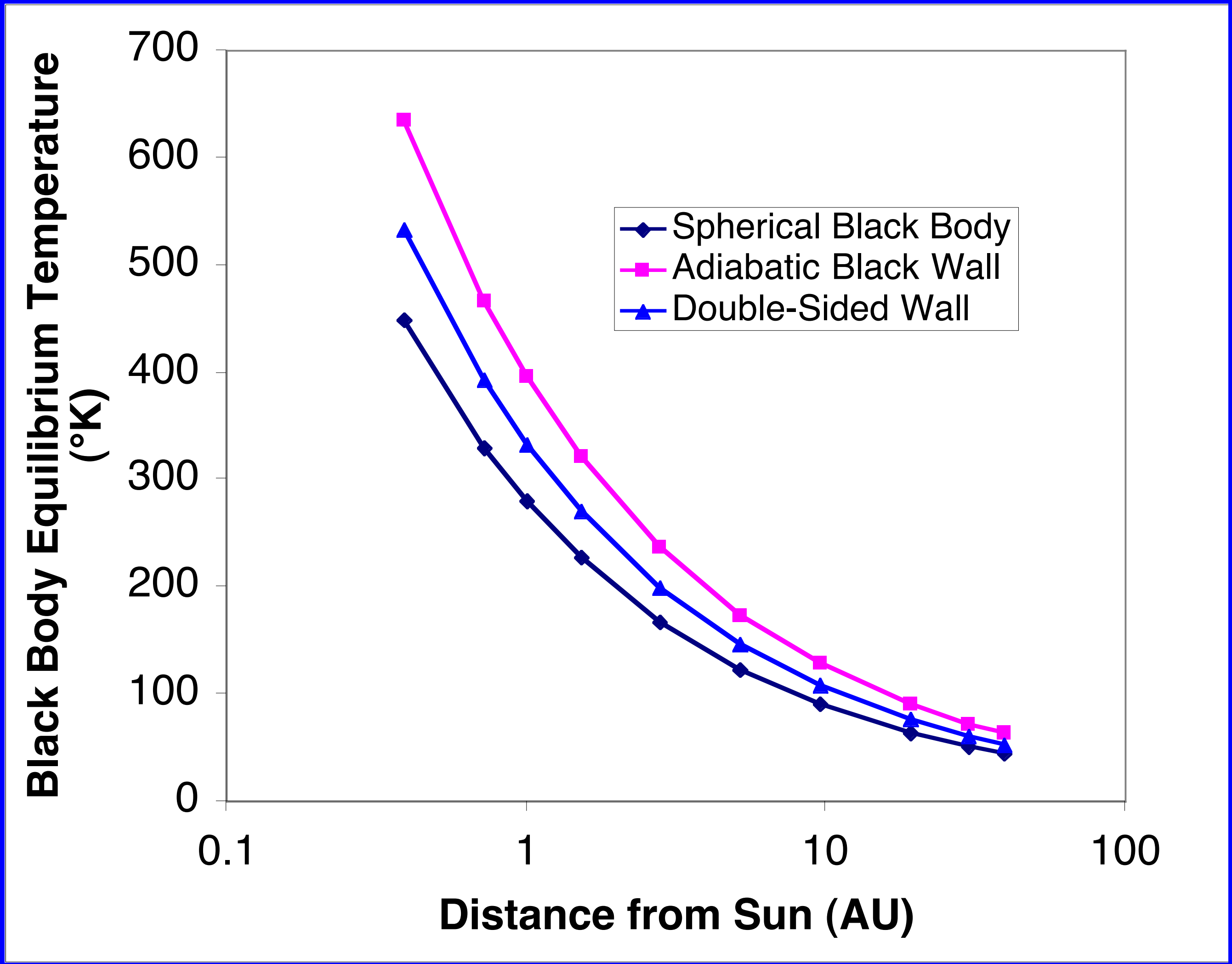
Effect of Distance on Equilibrium Temp



Shape and Radiative Equilibrium

- A shape absorbs energy only via illuminated faces
- A shape radiates energy via all surface area
- Basic assumption made is that black bodies are intrinsically isothermal (perfect and instantaneous conduction of heat internally to all faces)

Effect of Shape on Black Body Temps



Incident Radiation on Non-Ideal Bodies

Kirchkoff's Law for total incident energy flux on solid bodies:

$$Q_{Incident} = Q_{absorbed} + Q_{reflected} + Q_{transmitted}$$

$$\frac{Q_{absorbed}}{Q_{Incident}} + \frac{Q_{reflected}}{Q_{Incident}} + \frac{Q_{transmitted}}{Q_{Incident}} = 1$$

$$\alpha \equiv \frac{Q_{absorbed}}{Q_{Incident}}; \quad \rho \equiv \frac{Q_{reflected}}{Q_{Incident}}; \quad \tau \equiv \frac{Q_{transmitted}}{Q_{Incident}}$$

where

- α =absorptance (or absorptivity)
- ρ =reflectance (or reflectivity)
- τ =transmittance (or transmissivity)

Non-Ideal Radiative Equilibrium Temp

- Assume a spherical black body of radius r
- Heat in due to intercepted solar flux

$$Q_{in} = I_s \alpha \pi r^2$$

- Heat out due to radiation (from total surface area)

$$Q_{out} = 4 \pi r^2 \varepsilon \sigma T^4$$

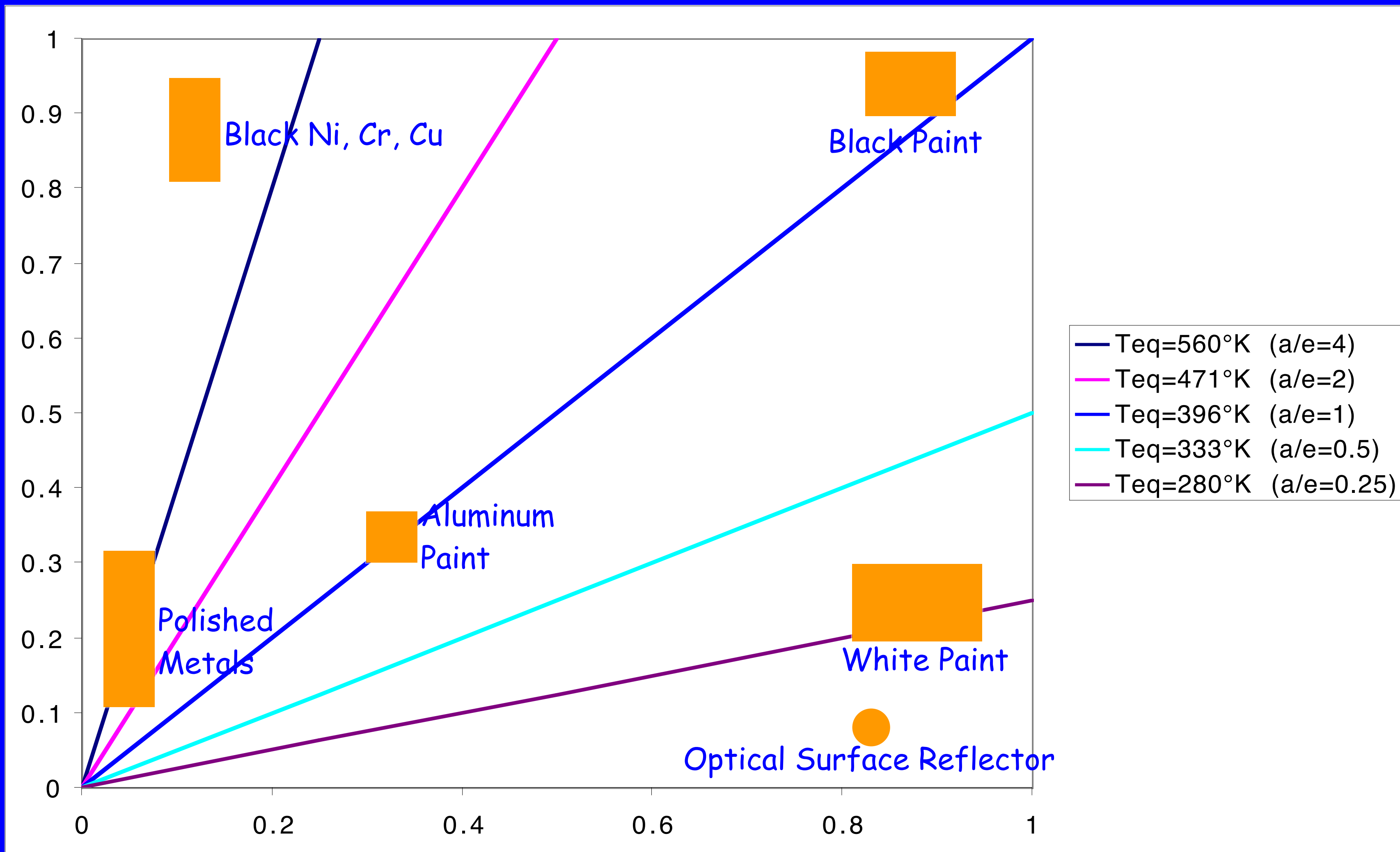
(ε = "emissivity" - efficiency of surface at radiating heat)

- For equilibrium, set equal

$$I_s \alpha \pi r^2 = 4 \pi r^2 \varepsilon \sigma T^4 \Rightarrow I_s = 4 \frac{\varepsilon}{\alpha} \sigma T^4$$

$$T_{eq} = \left(\frac{\alpha}{\varepsilon} \frac{I_s}{4\sigma} \right)^{1/4}$$

Effect of Surface Coating on Temperature



Non-Ideal Radiative Heat Transfer

- Full form of the Stefan-Boltzmann equation

$$P_{rad} = \varepsilon\sigma A\left(T^4 - T_{env}^4\right)$$

where T_{env}=environmental temperature (=4°K for space)

- Also take into account power used internally

$$I_s \alpha A_s + P_{\text{int}} = \varepsilon\sigma A_{rad}\left(T^4 - T_{env}^4\right)$$

Example: AERCam/SPRINT

- 30 cm diameter sphere
- $\alpha=0.2$; $\varepsilon=0.8$
- $P_{int}=200W$
- $T_{env}=280°K$ (cargo bay below; Earth above)
- Analysis cases:
  - Free space w/o sun
  - Free space w/sun
  - Earth orbit w/o sun
  - Earth orbit w/sun

AERCam/SPRINT Analysis (Free Space)

- A_s=0.0707 m^2; A_{rad}=0.2827 m^2
- Free space, no sun

$$P_{\text{int}} = \varepsilon\sigma A_{rad} T^4 \Rightarrow T = \left(\frac{200W}{0.8\left(5.67\times10^{-8}\frac{W}{m^2{}^\circ K^4}\right)\left(0.2827m^2\right)} \right)^{1/4} = 354^\circ K$$

AERCam/SPRINT Analysis (Free Space)

- A_s=0.0707 m^2; A_{rad}=0.2827 m^2
- Free space with sun

$$I_s \alpha A_s + P_{\text{int}} = \varepsilon \sigma A_{rad} T^4 \Rightarrow T = \left(\frac{I_s \alpha A_s + P_{\text{int}}}{\varepsilon \sigma A_{rad}} \right)^{1/4} = 362°K$$

AERCam/SPRINT Analysis (LEO Cargo Bay)

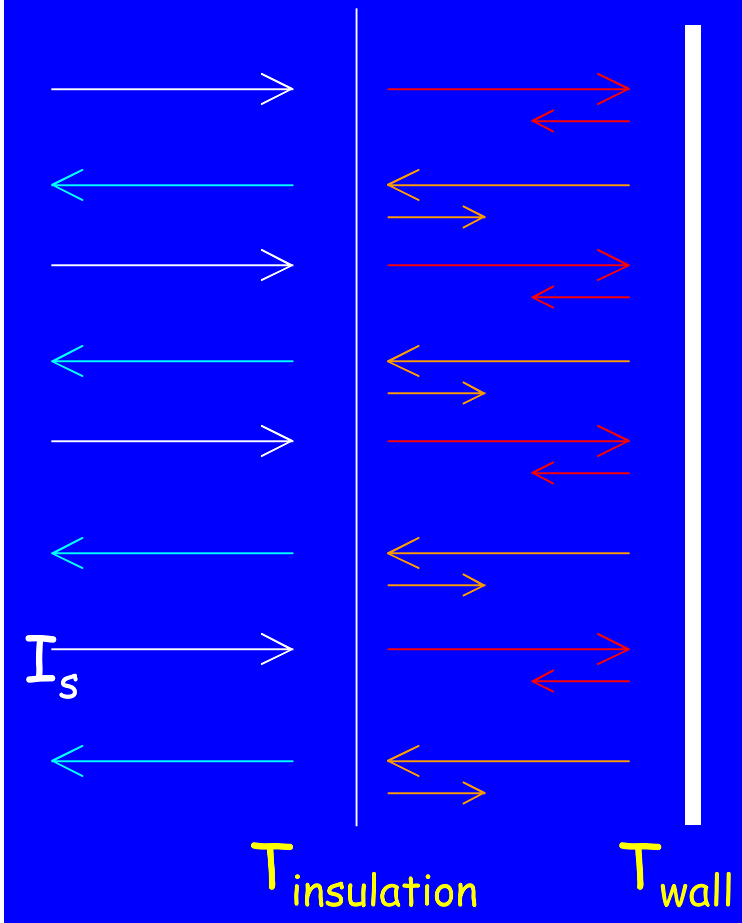
- T_{env}=280°K
- LEO cargo bay, no sun

$$P_{\text{int}} = \varepsilon\sigma A_{rad}\left(T^4 - T_{env}^4\right) \Rightarrow T = \left(\frac{200W}{0.8\left(5.67\times10^{-8}\dfrac{W}{m^2{}^\circ K^4}\right)\left(0.2827m^2\right)} + (280^\circ K)^4\right)^{1/4} = 384^\circ K$$

- LEO cargo bay with sun

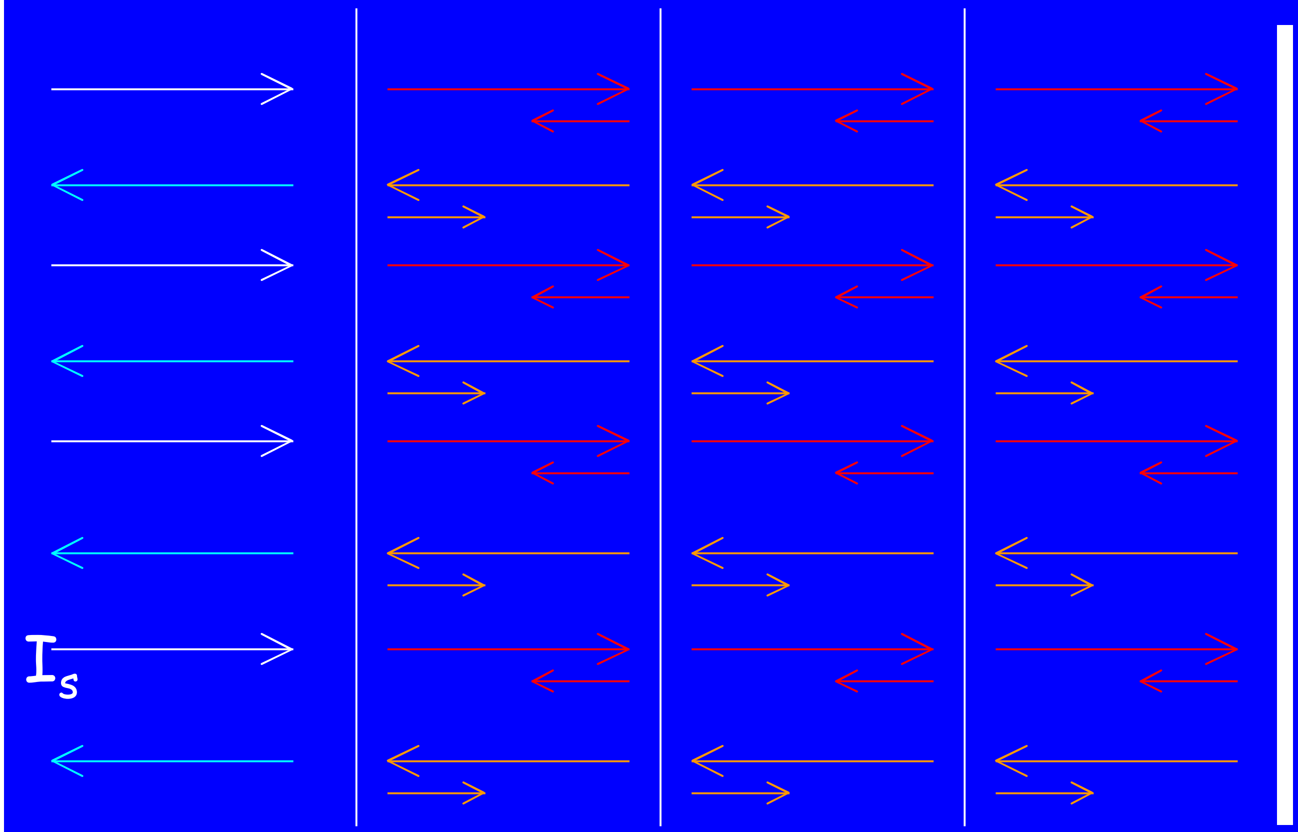
$$I_s\alpha A_s + P_{\text{int}} = \varepsilon\sigma A_{rad}\left(T^4 - T_{env}^4\right) \Rightarrow T = \left(\frac{I_s\alpha A_s + P_{\text{int}}}{\varepsilon\sigma A_{rad}} + T_{env}^4\right)^{1/4} = 391^\circ K$$

Radiative Insulation



- Thin sheet (mylar/kapton with surface coatings) used to isolate panel from solar flux
- Panel reaches equilibrium with radiation from sheet and from itself reflected from sheet
- Sheet reaches equilibrium with radiation from sun and panel, and from itself reflected off panel

Multi-Layer Insulation (MLI)



- Multiple insulation layers to cut down on radiative transfer
- Gets computationally intensive quickly
- Highly effective means of insulation
- Biggest problem is existence of conductive leak paths (physical connections to insulated components)

1D Conduction

- Basic law of one-dimensional heat conduction (Fourier 1822)

$$Q = -KA\frac{dT}{dx}$$

where

K=thermal conductivity (W/m°K)

A=area

dT/dx=thermal gradient

3D Conduction

General differential equation for heat flow in a solid

$$\nabla^2 T(\vec{r},t) + \frac{g(\vec{r},t)}{K} = \frac{\rho c}{K}\frac{\partial T(\vec{r},t)}{\partial t}$$

where

g(r,t)=internally generated heat

ρ=density (kg/m^3)

c=specific heat (J/kg°K)

K/ρc=thermal diffusivity

Simple Analytical Conduction Model

…	T_{i-1}	T_i	T_{i+1}	…

- Heat flowing from (i-1) into (i)

$$Q_{in} = -KA\frac{T_i - T_{i-1}}{\Delta x}$$

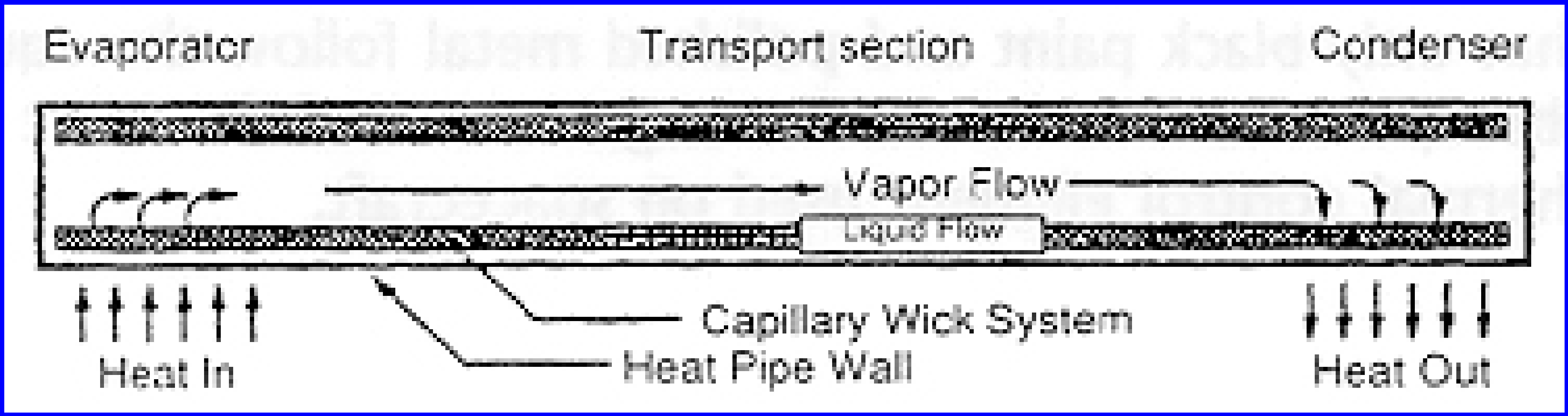
- Heat flowing from (i) into (i+1)

$$Q_{out} = -KA\frac{T_{i+1} - T_i}{\Delta x}$$

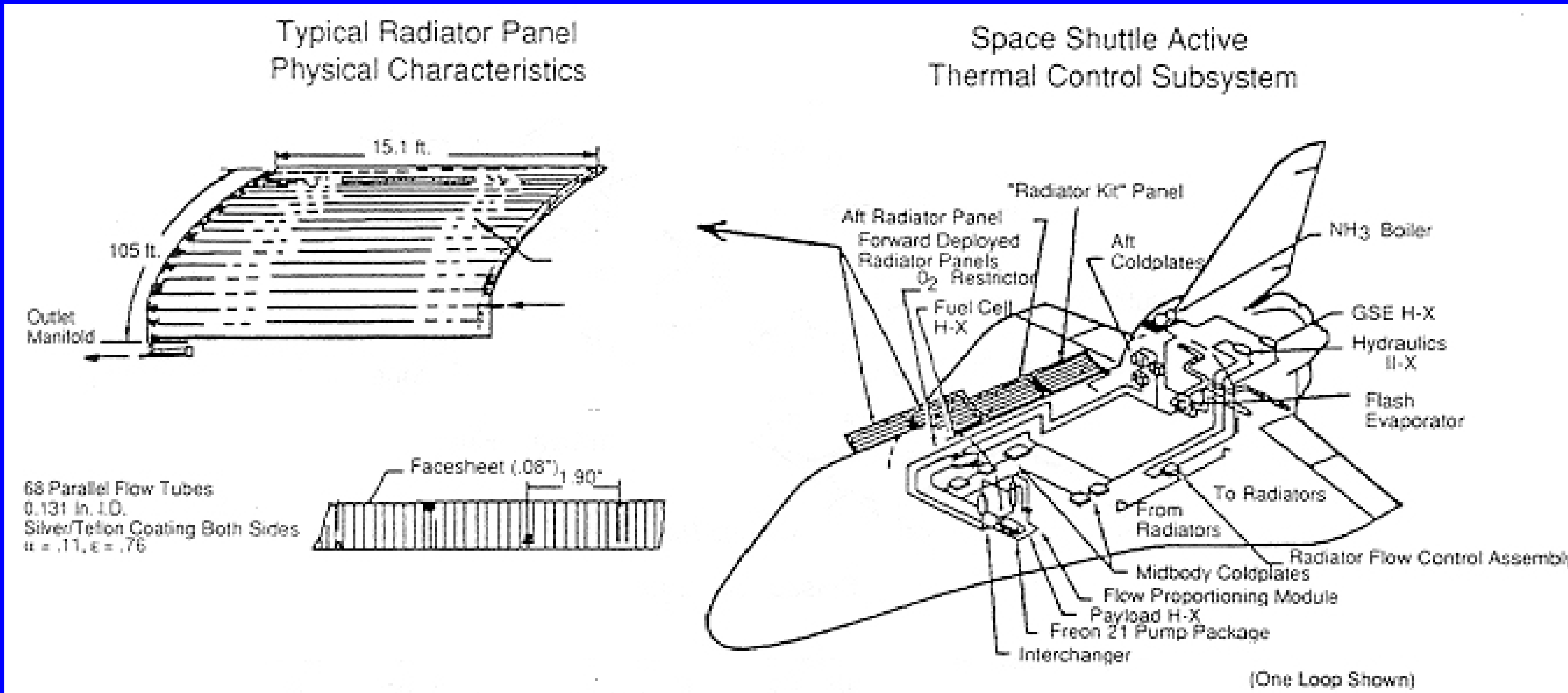
- Heat remaining in cell

$$Q_{out} - Q_{in} = \frac{\rho c}{K}\frac{T_i(j+1) - T_i(j)}{\Delta t}$$

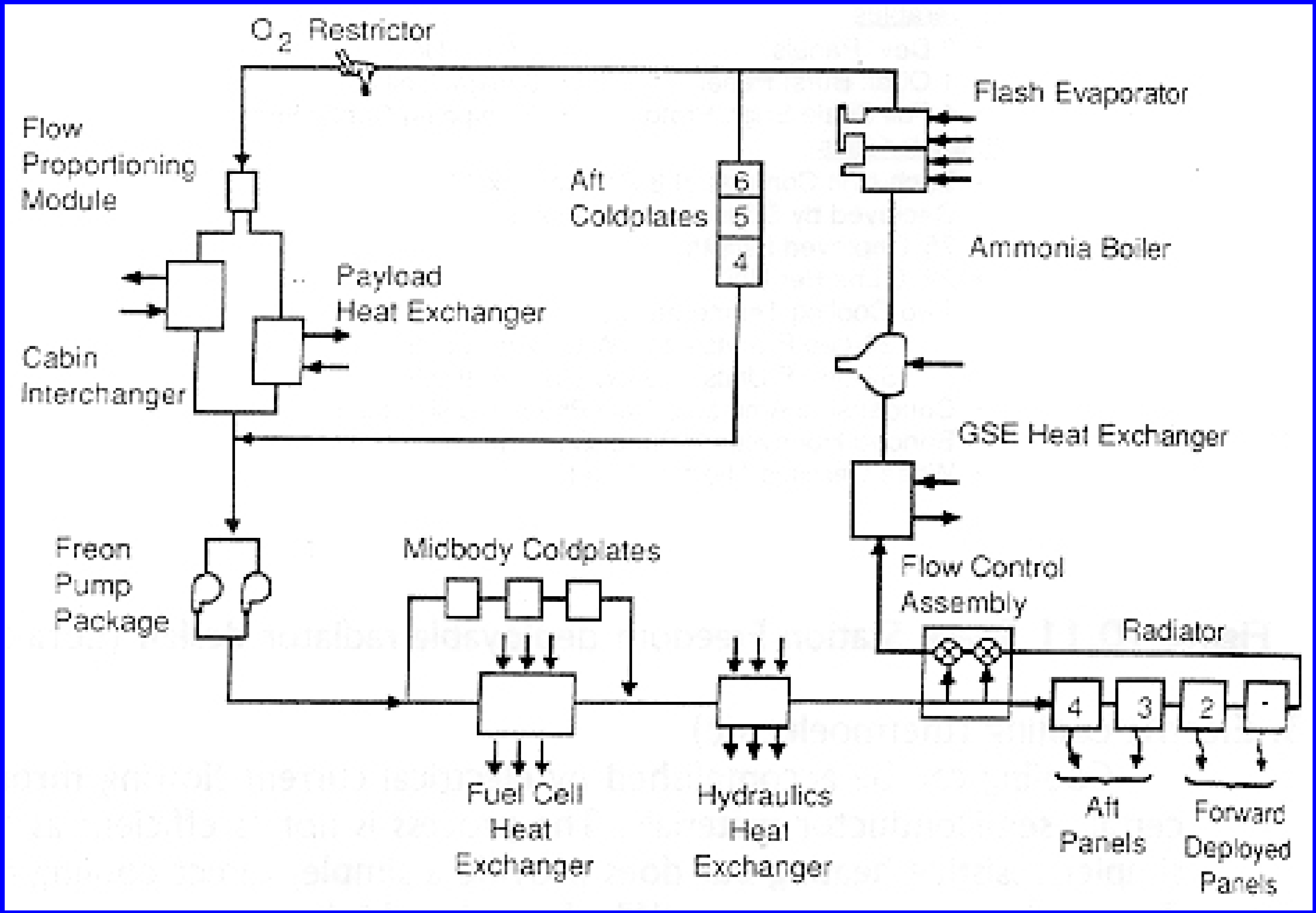
Heat Pipe Schematic



Shuttle Thermal Control Components



Shuttle Thermal Control System Schematic



ISS Radiator Assembly