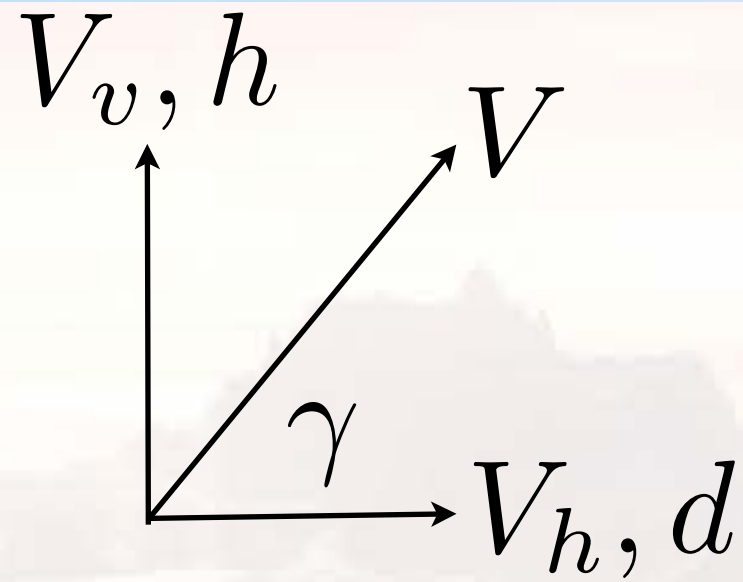


# Gaits and Locomotion

- Locomotion
- Metabolic energy
- Gaits
- Partial gravity simulation

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# Hopping (Airless Flat Planet)



Use  $F=ma$  for vertical motion

$$\dot{V}_v = -g \quad h = V_v t - \frac{1}{2}gt^2$$

$$t_{flt} = 2V_v/g$$

Constant velocity in horizontal direction produces

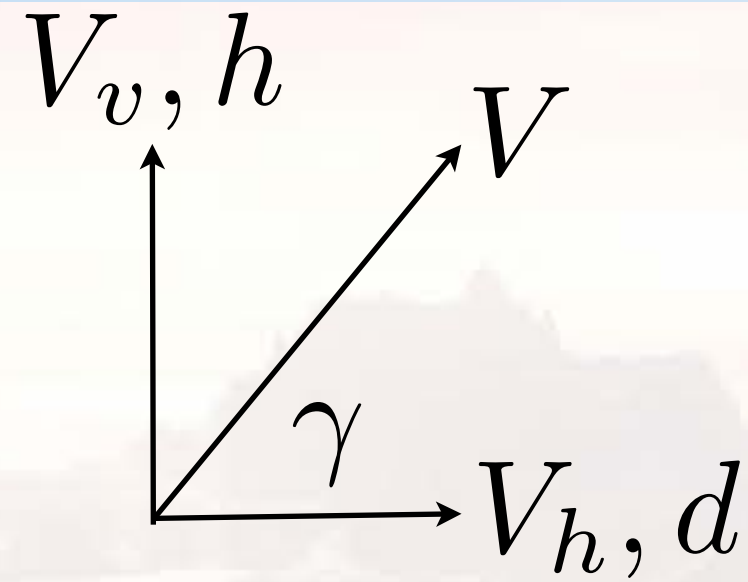
$$d = V_h t_{flt} = 2 \frac{V_h V_v}{g}$$

$$V_h = V \cos \gamma; V_v = V \sin \gamma$$

$$d = 2 \frac{V^2 \sin \gamma \cos \gamma}{g} = \frac{V^2}{g} \sin (2\gamma)$$



# Hopping (Airless Flat Planet)



Horizontal distance is maximized when  $\sin(2\gamma) = 1$

$$\gamma_{opt} = \frac{\pi}{2} = 45^\circ \quad d_{max} = \frac{V^2}{g}$$

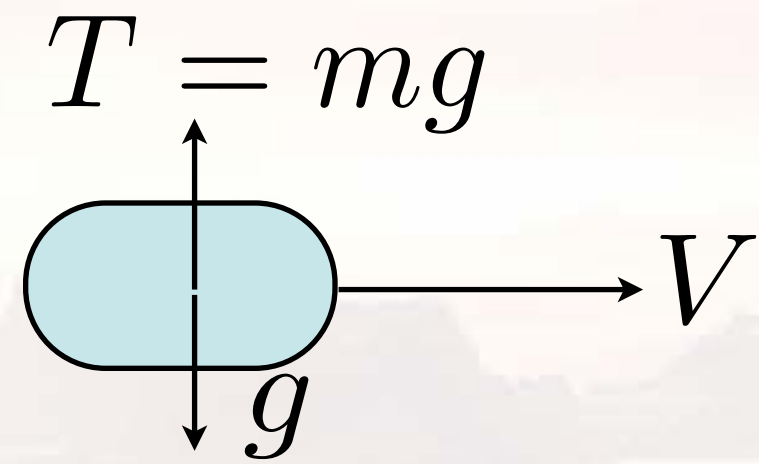
$$V = \sqrt{gd} \quad \Delta V_{total} = 2V = 2\sqrt{gd}$$

$$h_{max} = V_v \frac{V_v}{g} - \frac{1}{2}g \left( \frac{V_v}{g} \right)^2 \quad V_v = \frac{V}{\sqrt{2}}$$

$$h_{max} = \frac{V^2}{4g} = \frac{\sqrt{gd}^2}{4g} = \frac{d}{4}$$



# Propulsive Gliding (Airless Flat Planet)



Assume horizontal velocity is  $V$

$$\Delta V_h = 2V$$

(includes acceleration and deceleration)

$$t_{flt} = d/V$$

$$\Delta V_v = gt_{flt} = \frac{gd}{V}$$

Total  $\Delta V$  becomes

$$\Delta V_{total} = \Delta V_v + \Delta V_h = 2V + \frac{gd}{V}$$



# Propulsive Gliding (Airless Flat Planet)

Want to choose  $V$  to minimize

$$\frac{\partial}{\partial V} \left( 2V + \frac{gd}{V} \right) = 0 \quad 2 - \frac{gd}{V^2} = 0$$

$$V_{opt} = \sqrt{\frac{gd}{2}}$$

$$\Delta V_{total} = 2\sqrt{\frac{gd}{2}} + gd\sqrt{\frac{2}{gd}} = 2\sqrt{2}\sqrt{gd}$$

# Nondimensional Forms

$$\text{Define } \nu \equiv \frac{V}{\sqrt{dg}} \quad \rho \equiv \frac{d}{r} \quad \eta \equiv \frac{h_{max}}{d}$$

$$\nu_{flat\ glide} = 2\sqrt{2}$$

$$\nu_{flat\ hop} = 2 \quad \eta = \frac{1}{4}$$

$$\nu_{spherical\ glide} = 2\sqrt{2 - \rho} \quad (0 \leq \rho \leq 1)$$



# Multiple Hops

- Assume  $n$  hops between origin and destination
- At each intermediate “touchdown”,  $v_v$  has to be reversed

$$\Delta V_{total} = 2V + 2(n - 1)V_v$$

$$t_{peak} = \frac{V_v}{g} \quad t_{total} = 2nt_{peak} = 2n\frac{V_v}{g}$$

$$d = V_h t_{total} = \frac{2n}{g} V_h V_v \quad V_v = \sqrt{2gh_{max}} \quad \nu_v = \sqrt{\frac{2\eta}{n}}$$

$$\nu \equiv \frac{V}{\sqrt{dg}} \quad \eta \equiv \frac{h_{max}}{d/n} \quad V_h = \frac{dg}{2nV_v} \quad \nu_h = \frac{1}{2} \sqrt{\frac{1}{2n\eta}}$$

# Multiple Hop Analysis

$$\Delta\nu = 2\nu + 2(n - 1)\nu_v$$

$$\Delta\nu = 2\sqrt{\nu_v^2 + \nu_h^2} + 2(n - 1)\nu_v$$

$$\Delta\nu = 2\sqrt{\frac{2\eta}{n} + \frac{1}{8n\eta}} + 2(n - 1)\sqrt{\frac{2\eta}{n}}$$

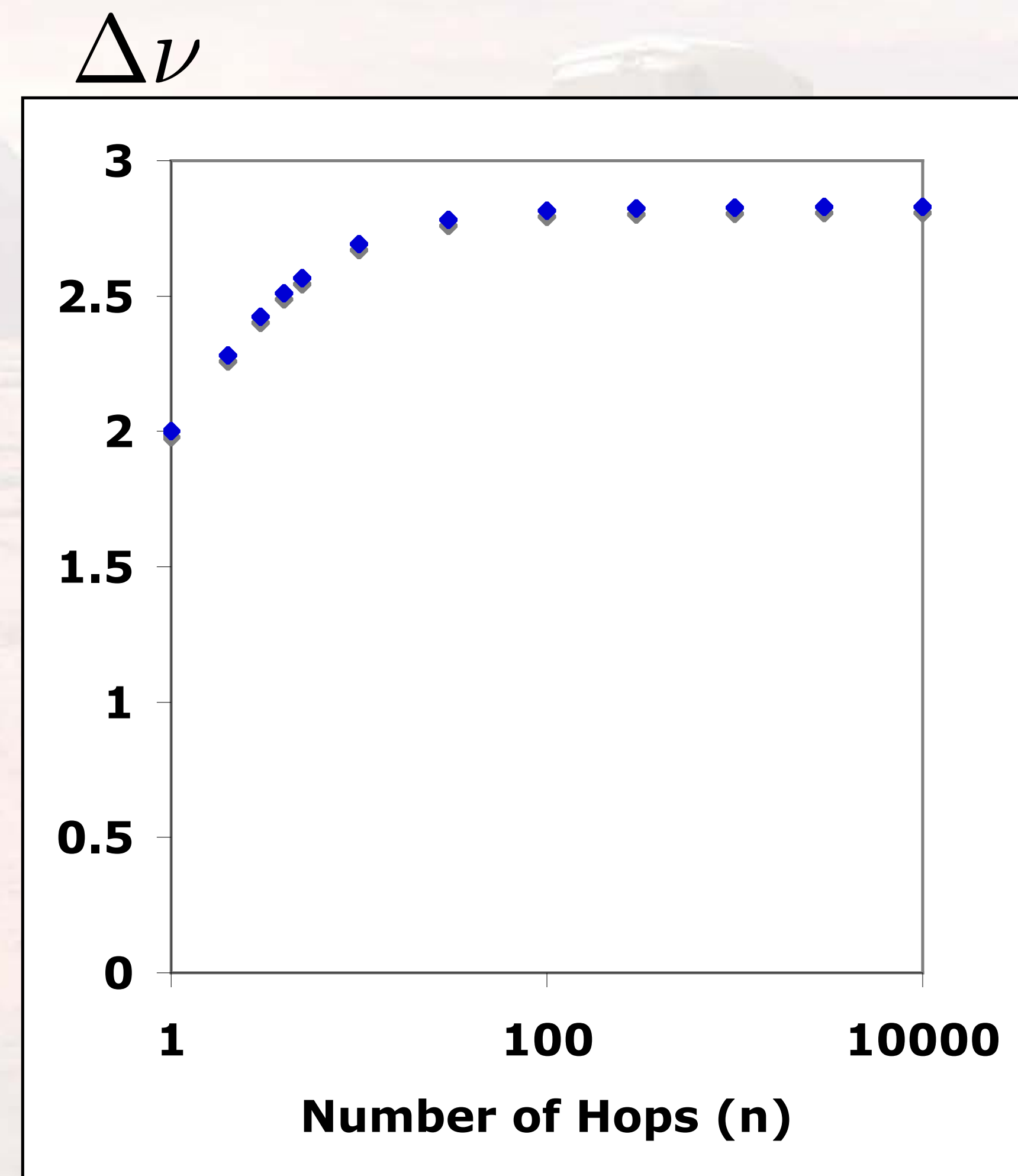
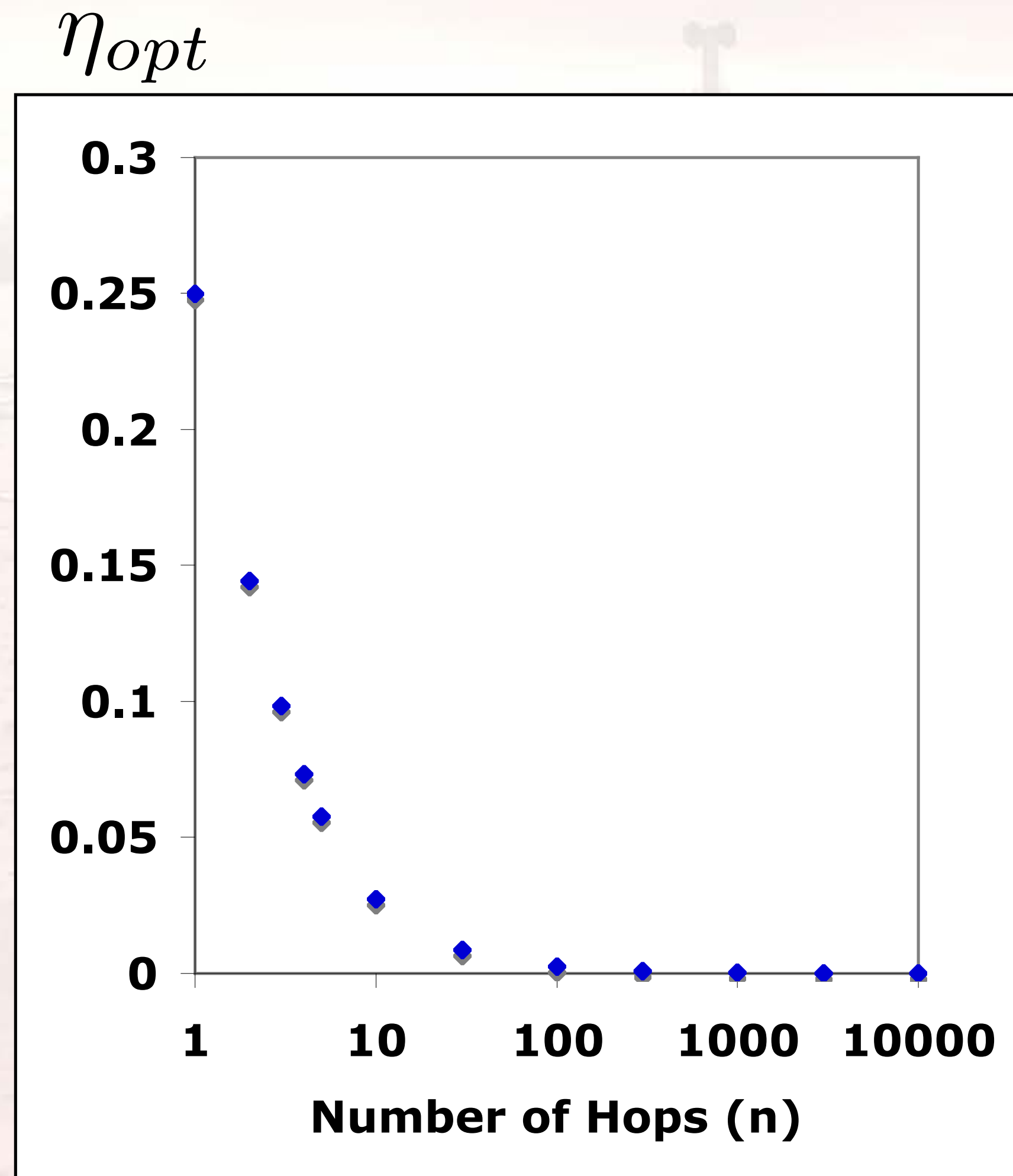
$$\frac{\partial\Delta\nu}{\partial\eta} = \left[ \frac{1}{\sqrt{\frac{2\eta}{n} + \frac{1}{8n\eta}}} \left( \frac{2}{n} - \frac{1}{8n\eta^2} \right) \right] + (n - 1)\sqrt{\frac{2}{n\eta}} = 0$$

Analytically messy, but note that for  $n = 1 \Rightarrow \eta_{opt} = \frac{1}{4}$

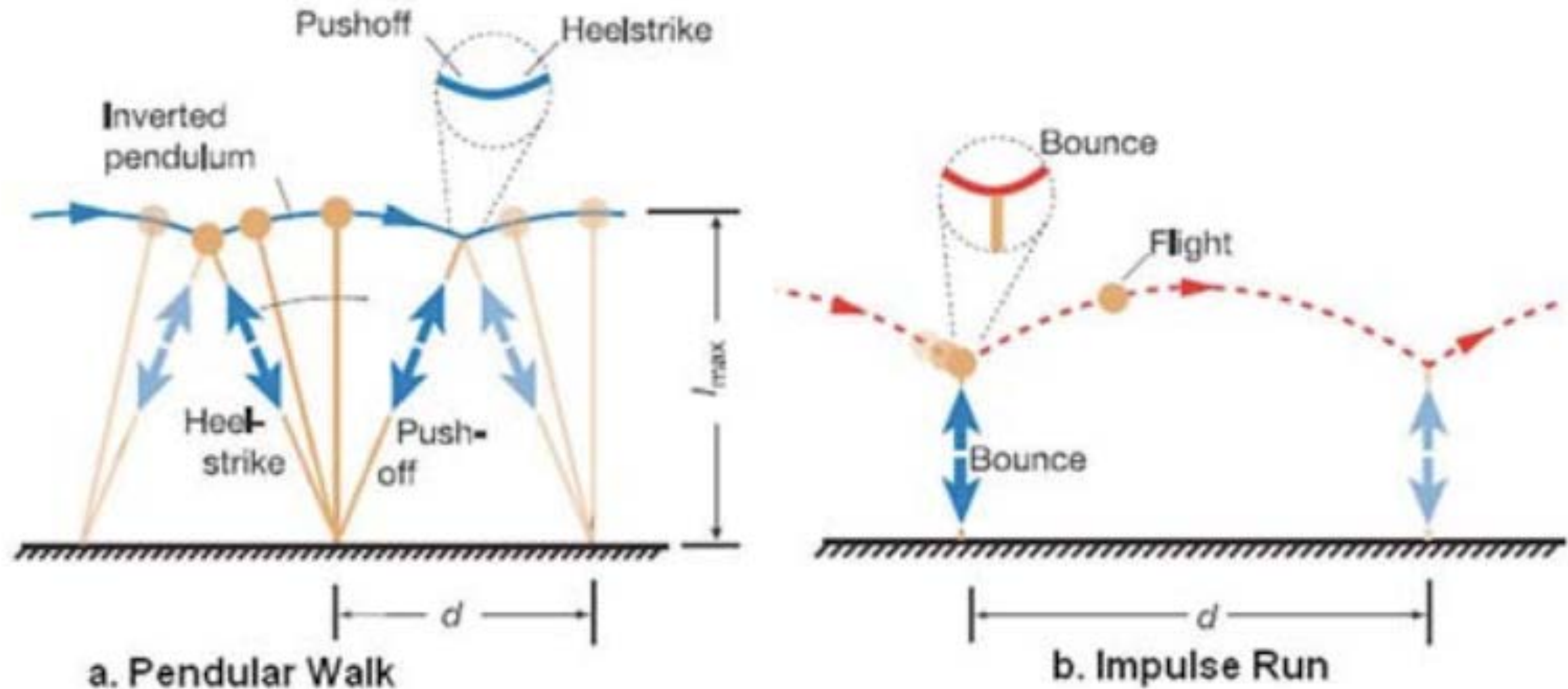
(In general, solve numerically)



# Optimal Solutions for Multiple Hops



# Walking and Running Gaits



from Rader, Newman, and Carr, *Loping: A Strategy for Reduced Gravity Human Locomotion?* ICES 2007-01-3134, International Conference on Environmental Systems, Chicago, IL, July 2007



# Implications of Pendulum Motion

- Basic period of a pendulum

$$P \approx 2\pi \sqrt{\frac{L}{g}}$$

- Inertias of point and distributed masses



$$I = mL^2$$



$$I = \frac{1}{3}mL^2$$

- For 0.75 m leg length,

$$P_{walking} \approx 1.0 \text{ sec (on Earth)}$$

# Walking Froude Number

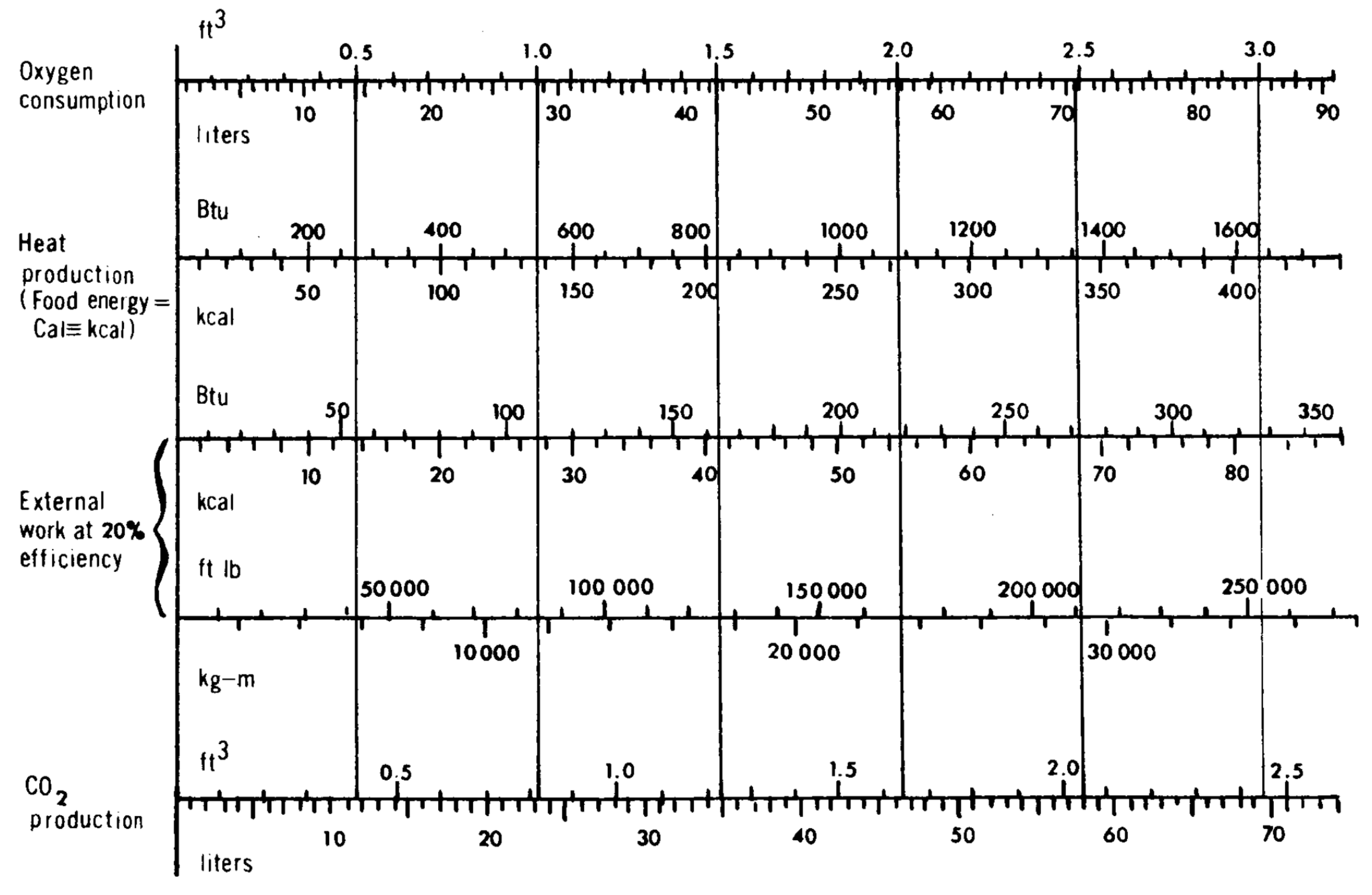
- Froude number is ratio between inertial and gravitational forces
- Primary application is boat speed (transition between displacement and planing motion)
- Walking Froude number

$$Fr = \frac{V^2}{gL} = \frac{a_{centripetal}}{g}$$

- Feet leave the ground at  $Fr=1$
- Walk-run transition typically occurs  $\sim Fr=0.5$

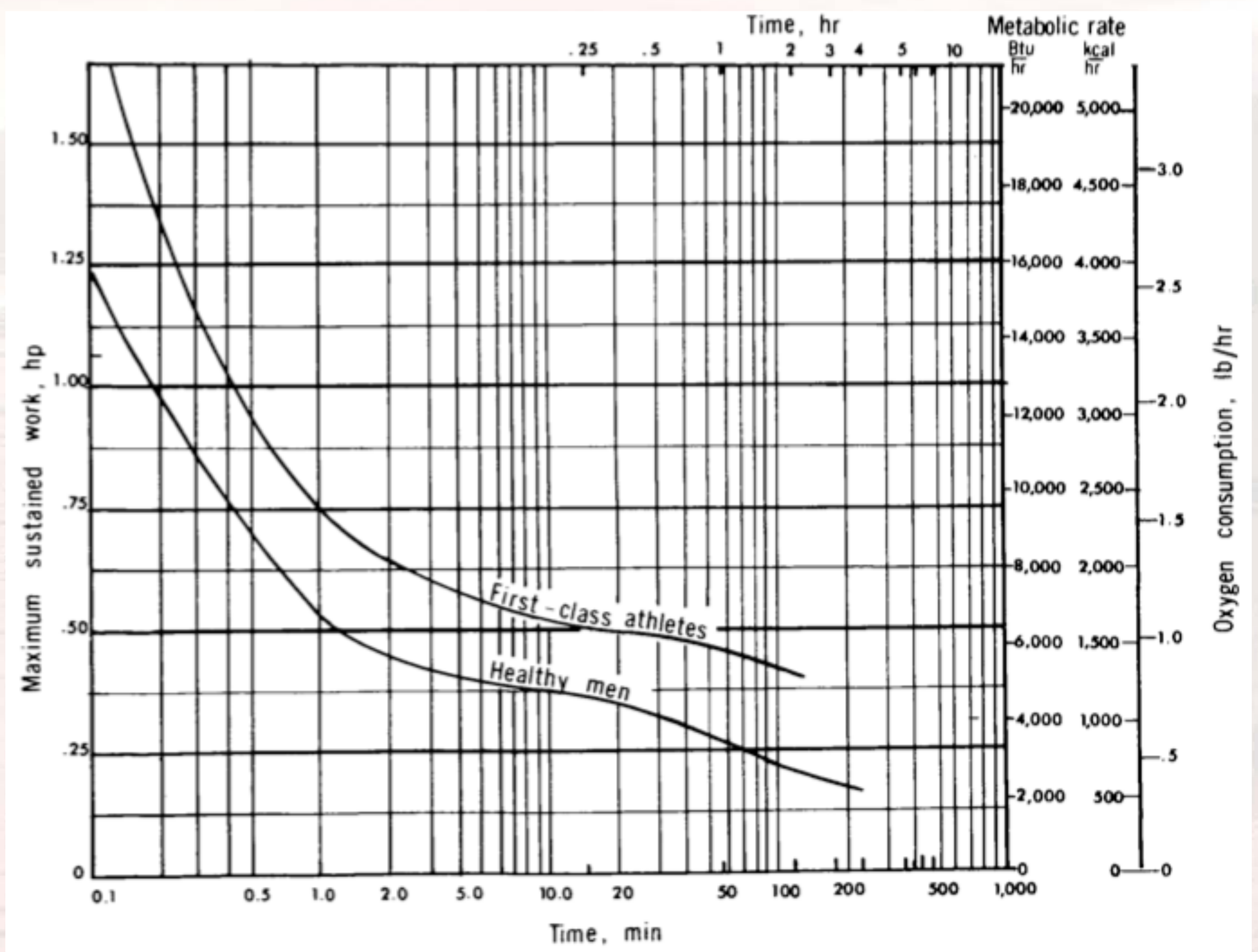


# Metabolic Costs of Physical Exertion



from Roth, *Bioenergetics of Space Suits for Lunar Exploration*, NASA SP-84, 1966

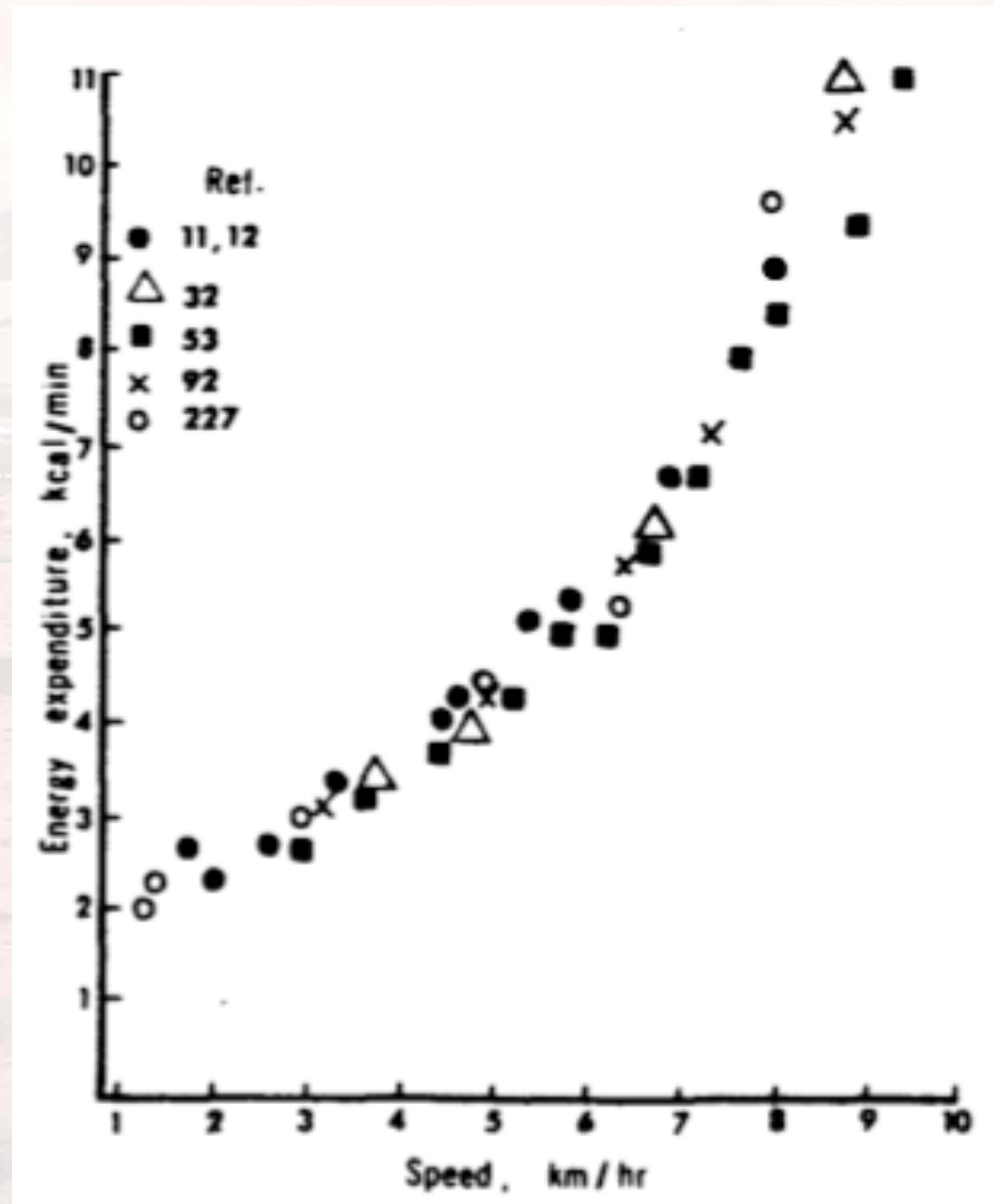
# Maximum Sustained Work Output



from Roth, *Bioenergetics of Space Suits for Lunar Exploration*, NASA SP-84, 1966



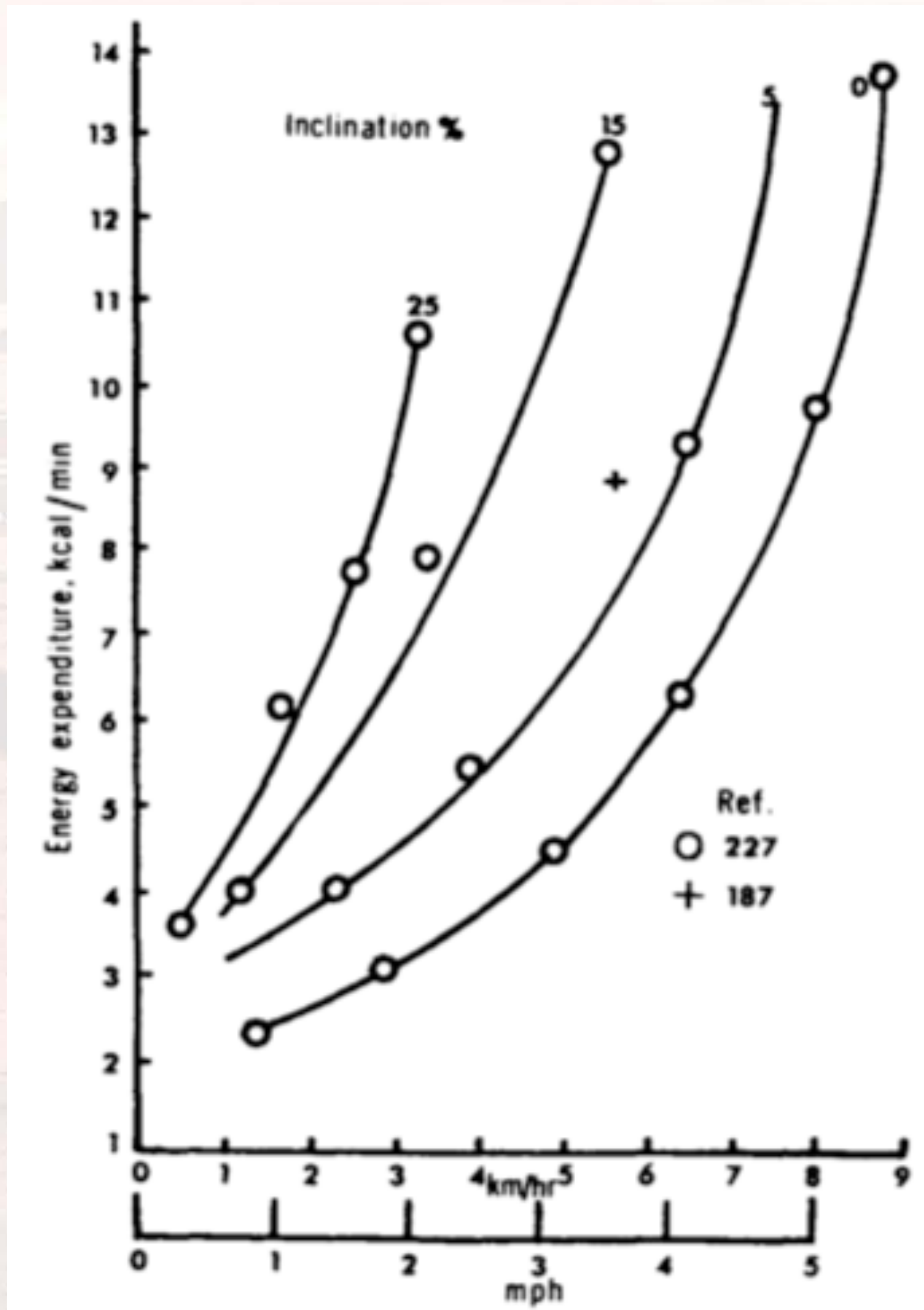
# Energy Expenditure in Walking



from Roth, *Bioenergetics of Space Suits for Lunar Exploration*, NASA SP-84, 1966



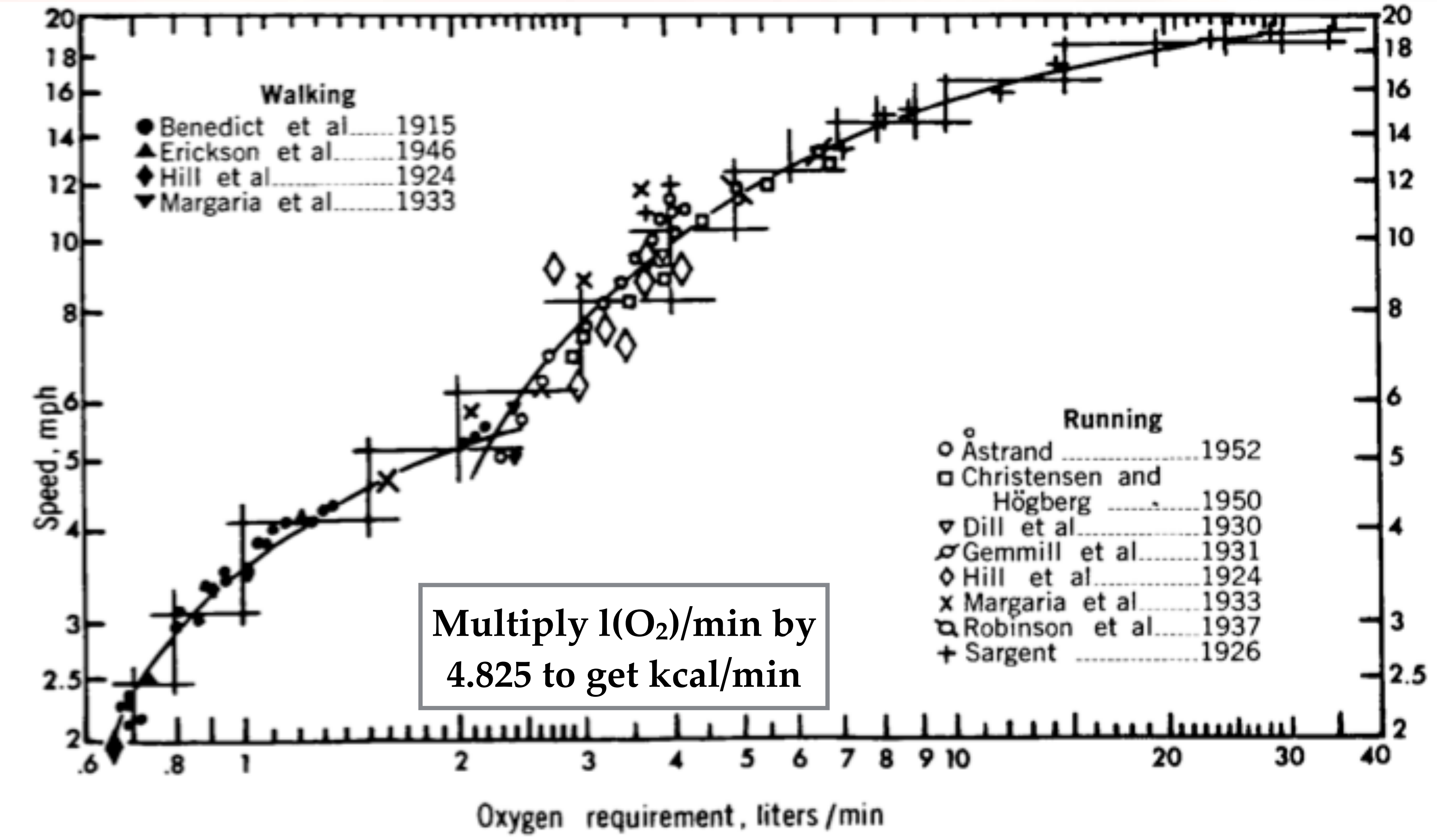
# O<sub>2</sub> Requirement to Walk and Run



from Roth, *Bioenergetics of Space Suits for Lunar Exploration*, NASA SP-84, 1966



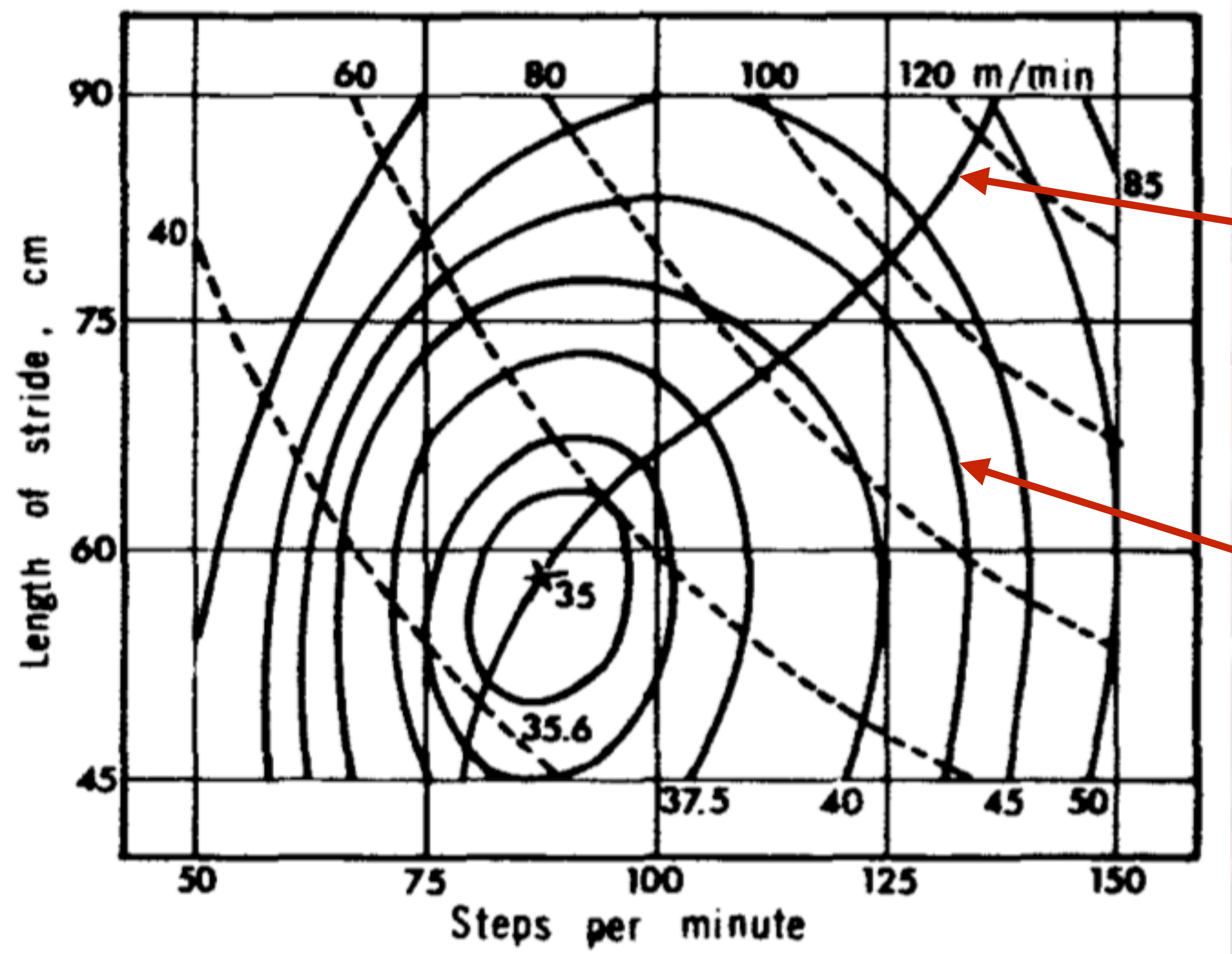
# O<sub>2</sub> Requirement to Walk and Run



from Roth, *Bioenergetics of Space Suits for Lunar Exploration*, NASA SP-84, 1966



# Effect of Stride and Cadence



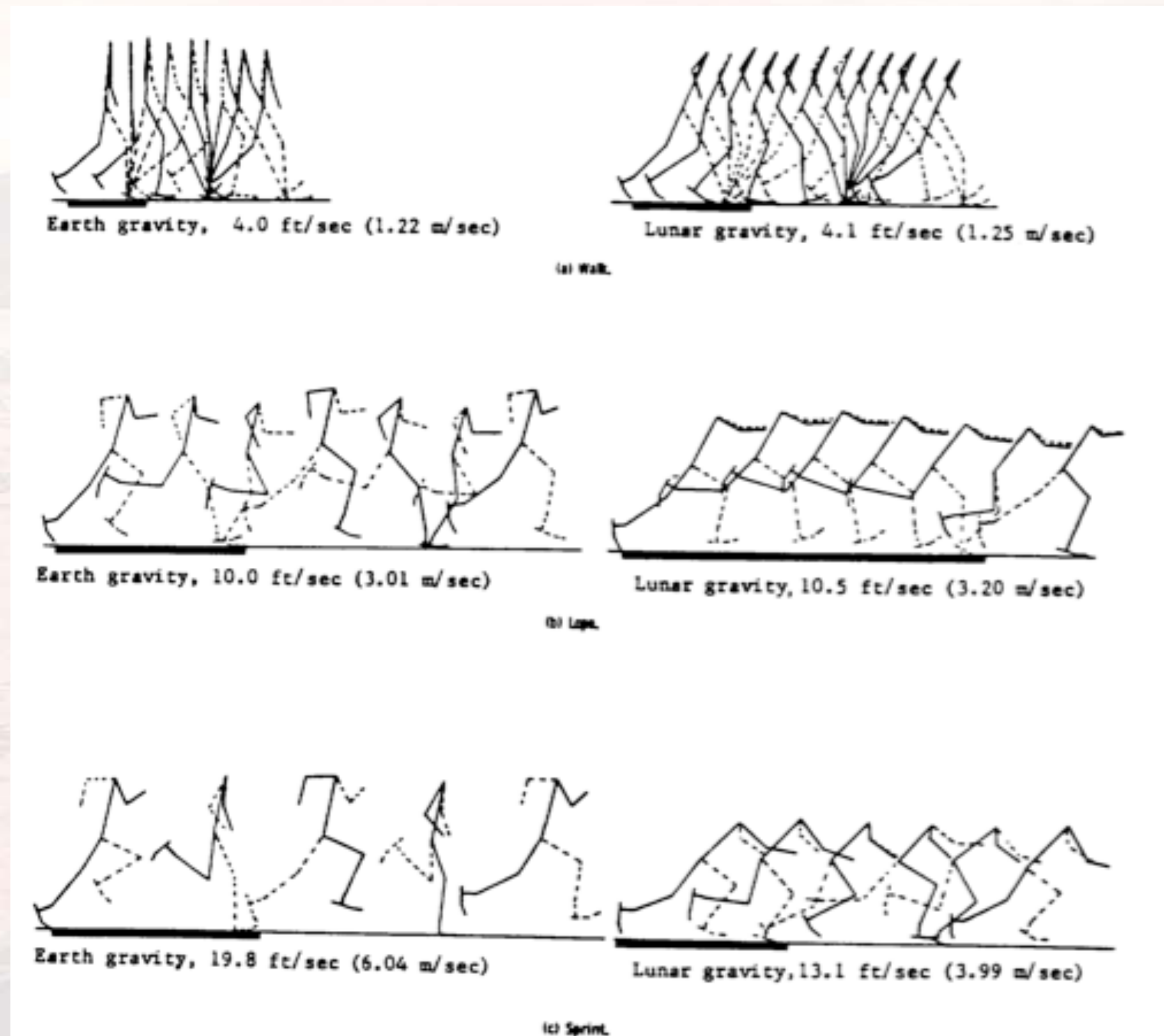
Optimum combination of cadence and stride length

Lines of constant caloric consumption (kcal/min)

from Roth, *Bioenergetics of Space Suits for Lunar Exploration*, NASA SP-84, 1966

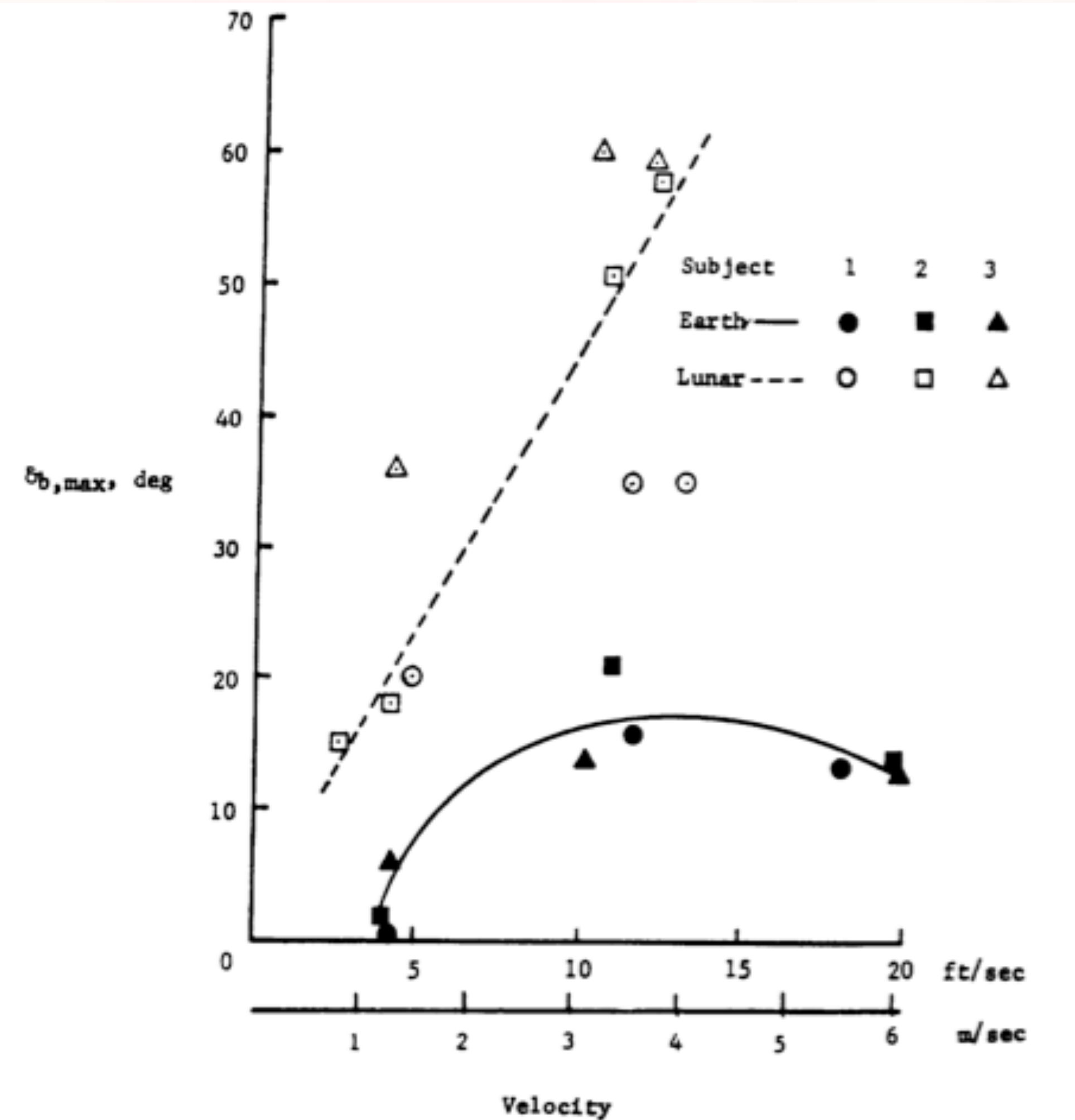


# Body Inclination in Variable Gravity



from Partial Gravity Habitat Study, Sasakawa International Center for Space Architecture,  
University of Houston, 1989

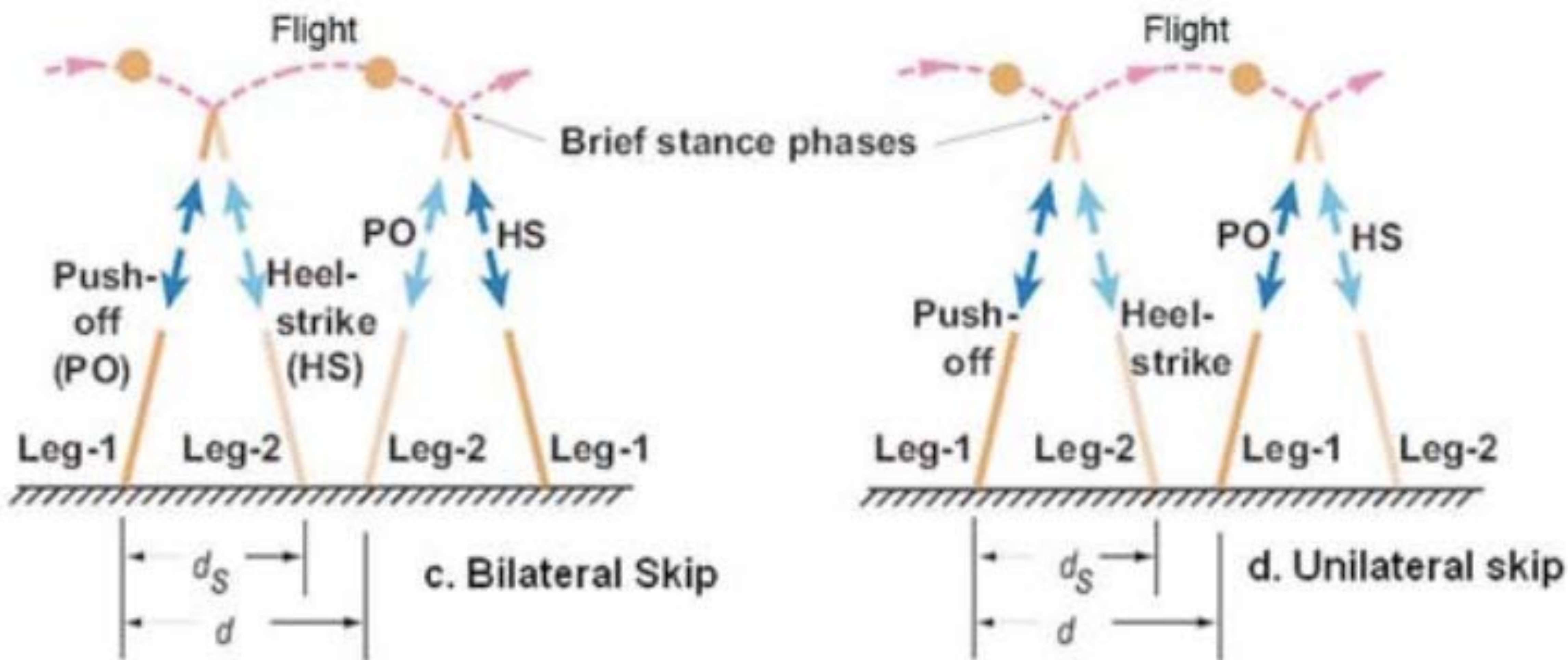
# Body Inclination in Variable Gravity



from Partial Gravity Habitat Study, Sasakawa International Center for Space Architecture, University of Houston, 1989



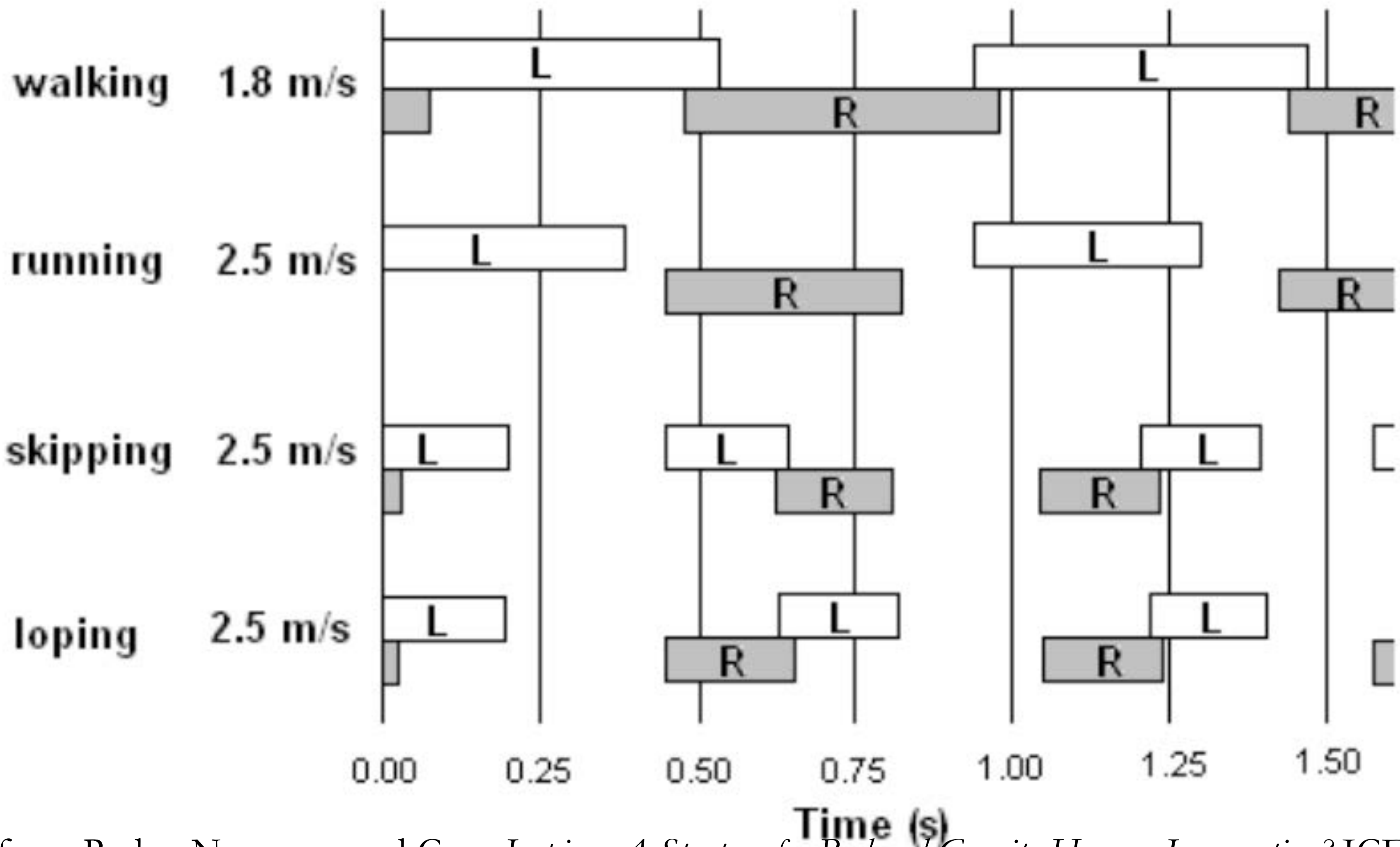
# Skipping and Loping Gaits



from Rader, Newman, and Carr, *Loping: A Strategy for Reduced Gravity Human Locomotion?* ICES 2007-01-3134, International Conference on Environmental Systems, Chicago, IL, July 2007



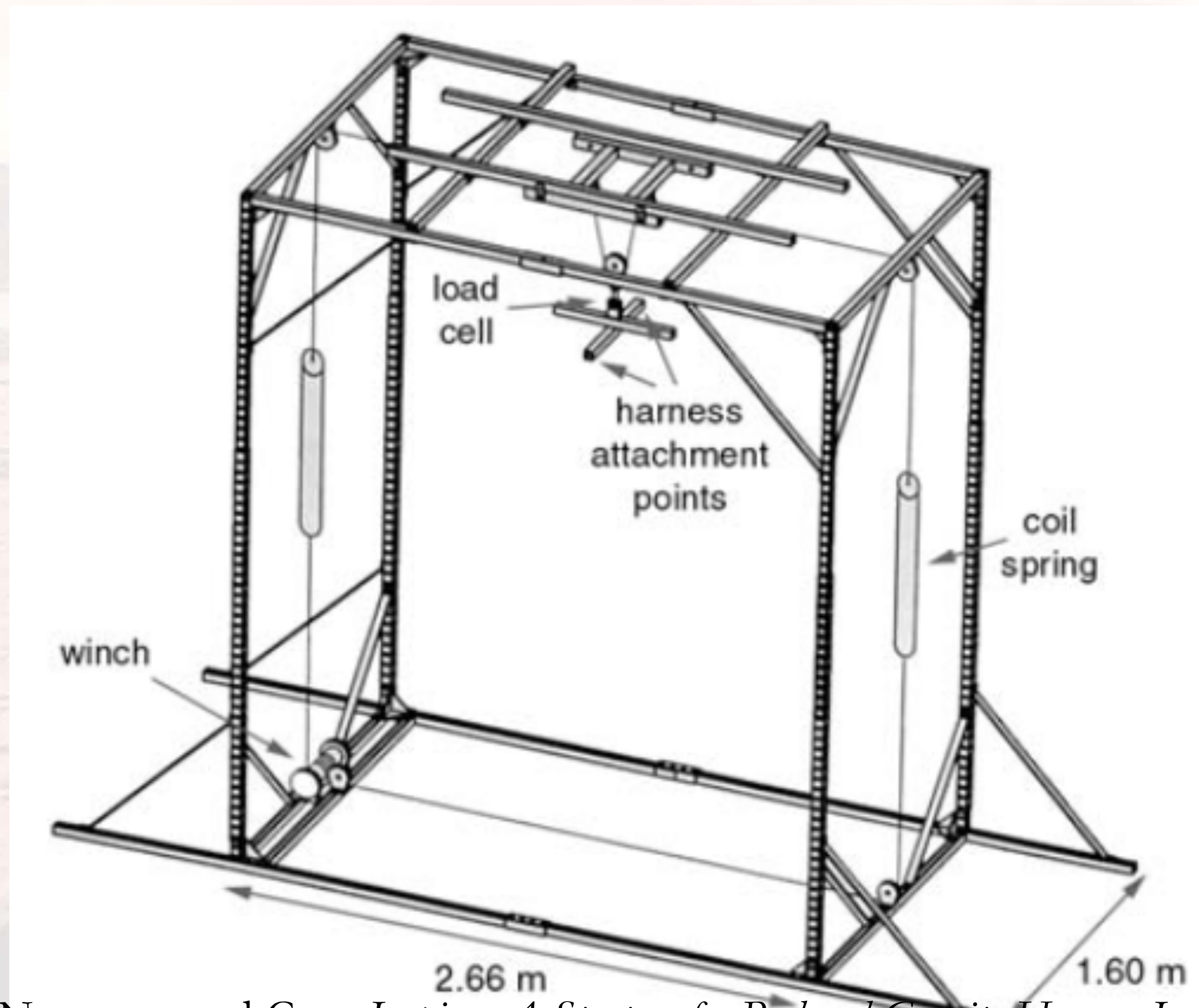
# Gait Footfalls



from Rader, Newman, and Carr, *Loping: A Strategy for Reduced Gravity Human Locomotion?* ICES 2007-01-3134, International Conference on Environmental Systems, Chicago, IL, July 2007



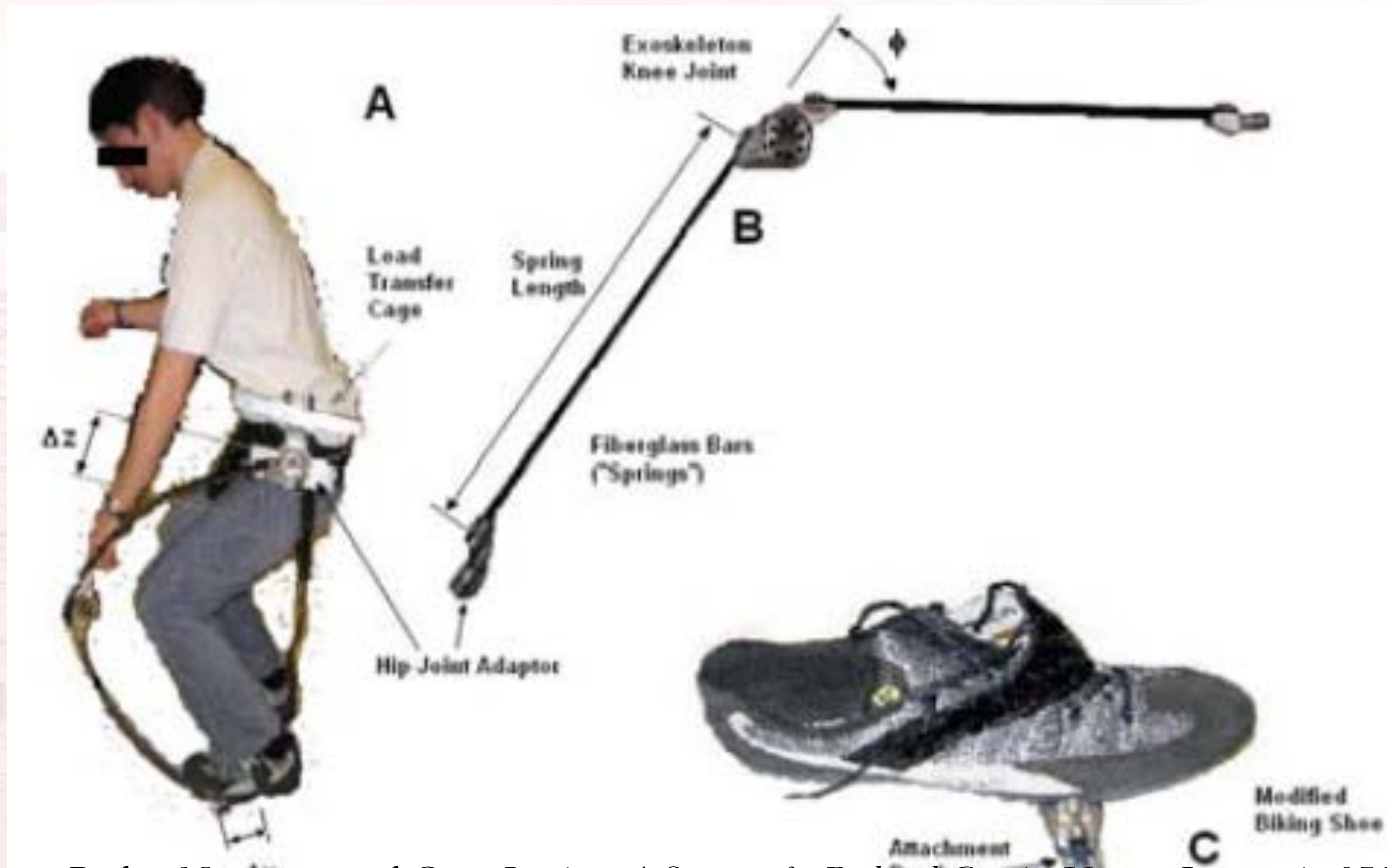
# MIT Gravity Offset System



from Rader, Newman, and Carr, *Loping: A Strategy for Reduced Gravity Human Locomotion?* ICES 2007-01-3134, International Conference on Environmental Systems, Chicago, IL, July 2007



# MIT Exoskeletal Suit Joint Simulator



from Rader, Newman, and Carr, *Loping: A Strategy for Reduced Gravity Human Locomotion?* ICES 2007-01-3134, International Conference on Environmental Systems, Chicago, IL, July 2007



# JSC Walkback Tests (2006-2007)

- Testing to verify metabolic cost of 10 km walkback from failed rover in lunar gravity
- Extra-large treadmill
- Pogo (pneumatic suspension) gravity offset device
- Mk. III suit
- Vicon motion tracking system
- Six test subjects (astronauts)
- Measured VO<sub>2</sub>, RPE, MCH

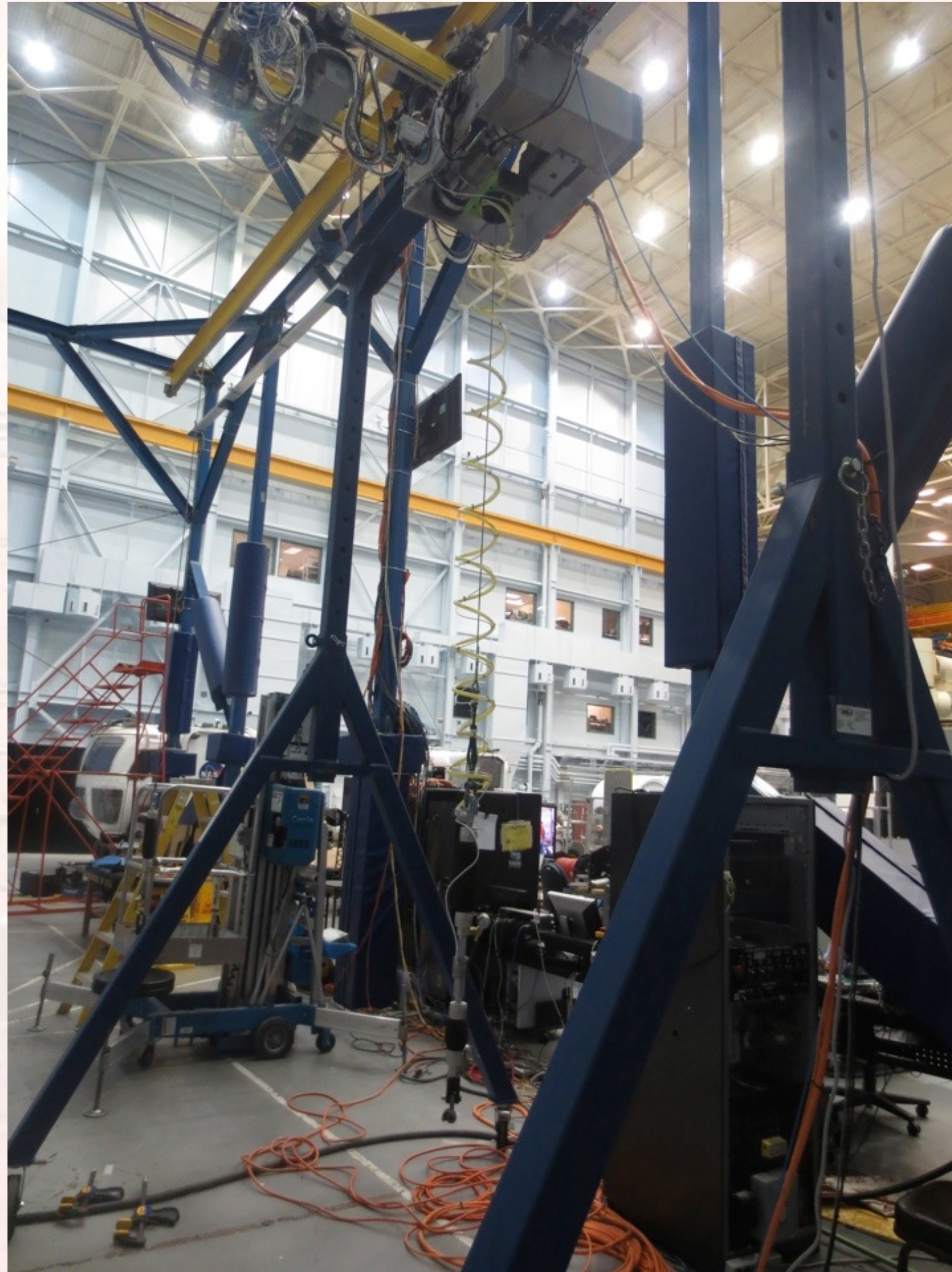


# JSC ARGOS Gravity Offset System





# ARGOS Suspension and Tracks





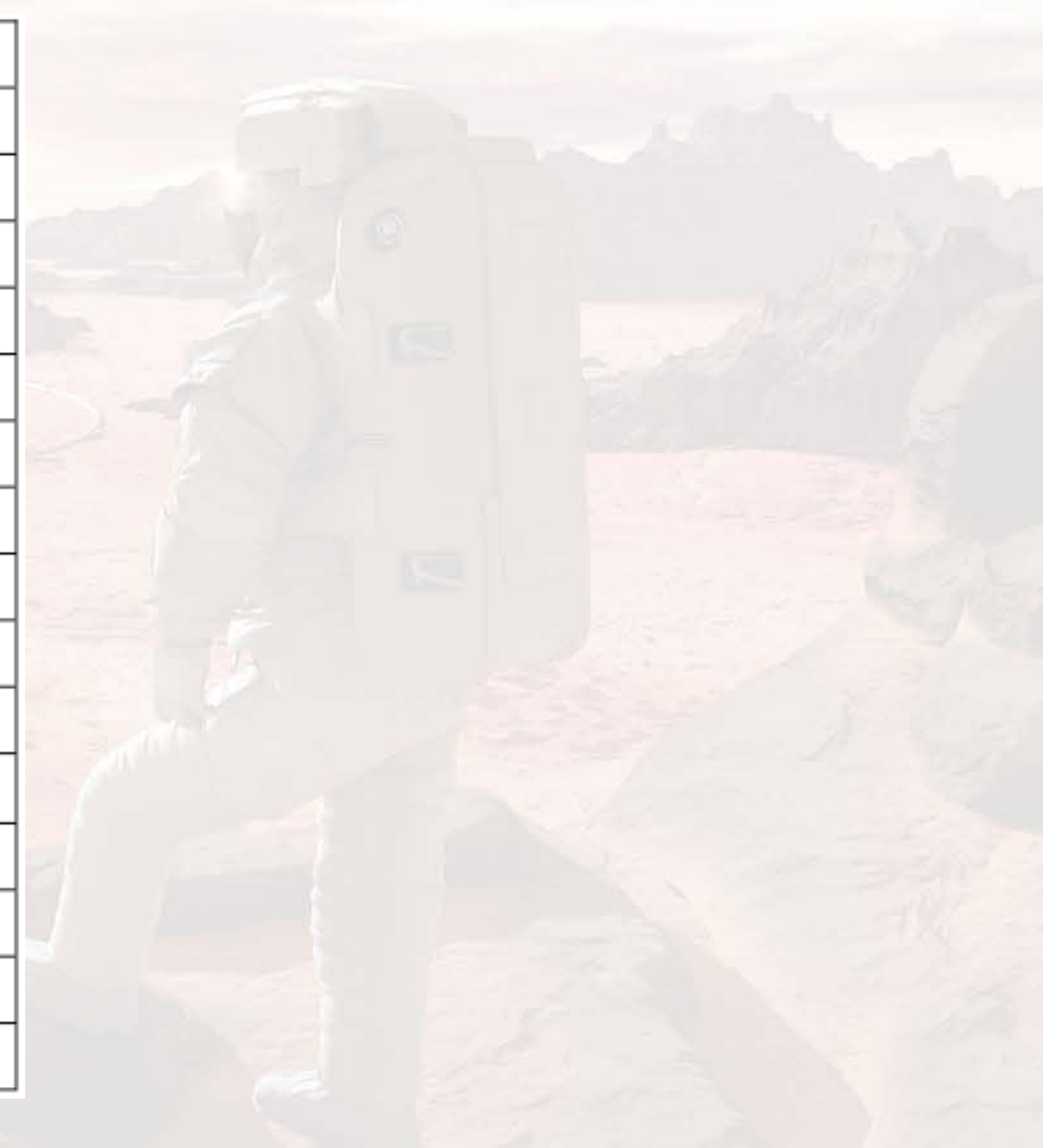
# ARGOS Suspension System





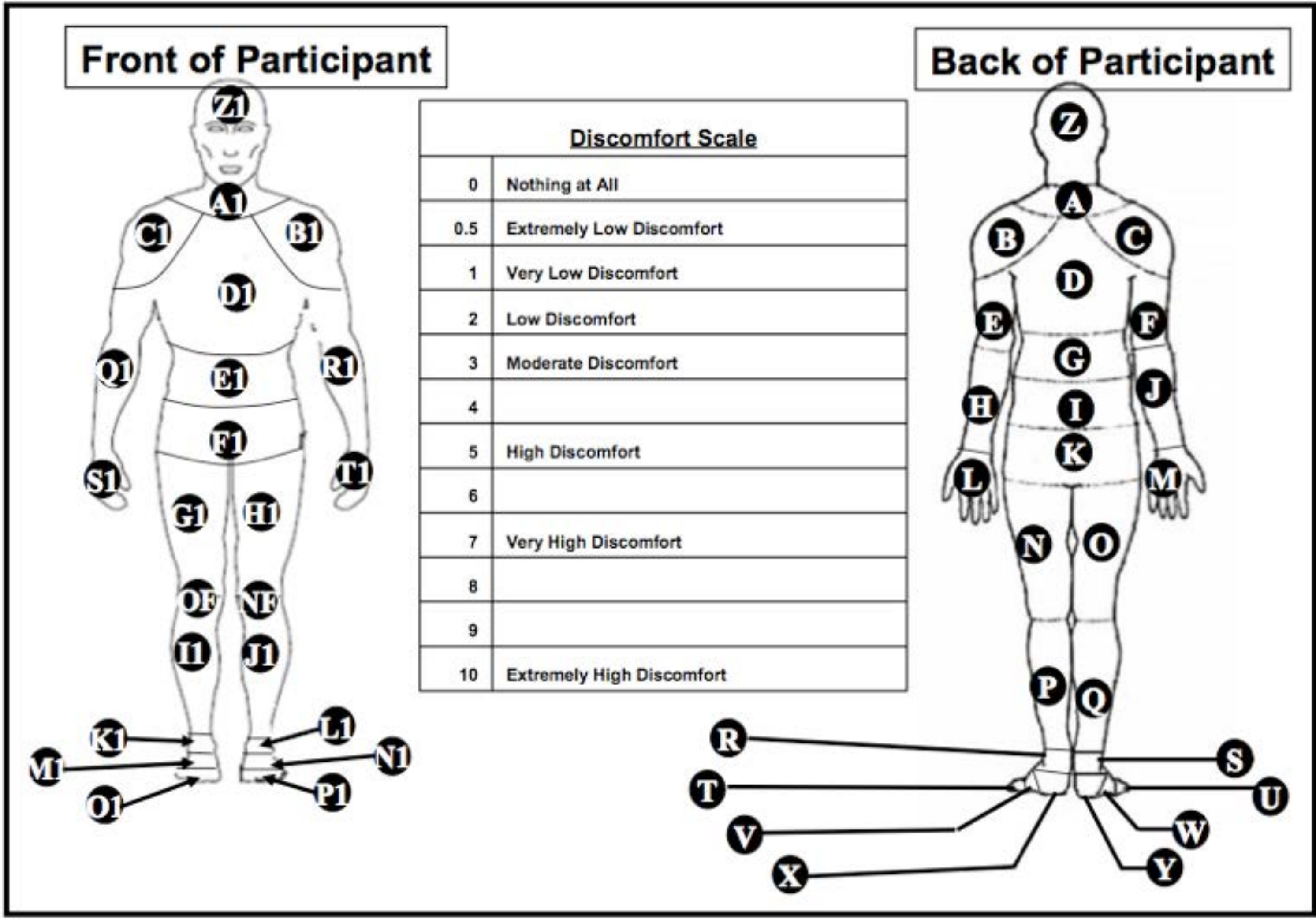
# Borg Rating of Perceived Exertion (RPE)

6	No exertion at all
7	Extremely light
8	
9	Very light
10	
11	Light
12	
13	Somewhat hard
14	
15	Hard (heavy)
16	
17	Very hard
18	
19	Extremely hard
20	Maximal exertion





# Corlett & Bishop Discomfort Scale





# Speeds Used for Testing

Speeds Used for the Energy-Velocity Tests:		
Stage	Speed	Comments
1	X minus 1.1 mph	Subtract 0.3 mph per stage; need smaller increments for walking
2	X minus 0.8 mph	
3	X minus 0.5 mph	Subtract 0.5 mph to assure walking out of transition zone
<b>PTS = X</b>		<b>No data collected in transition zone</b>
4	X plus 0.5 mph	Add 0.5 mph to assure running out of transition zone
5	X plus 1.5 mph	Add 1.0 mph to distinguish metabolic/biomechanical differences at running speeds
6	X plus 2.5 mph	



# Shirt-Sleeve Suspension



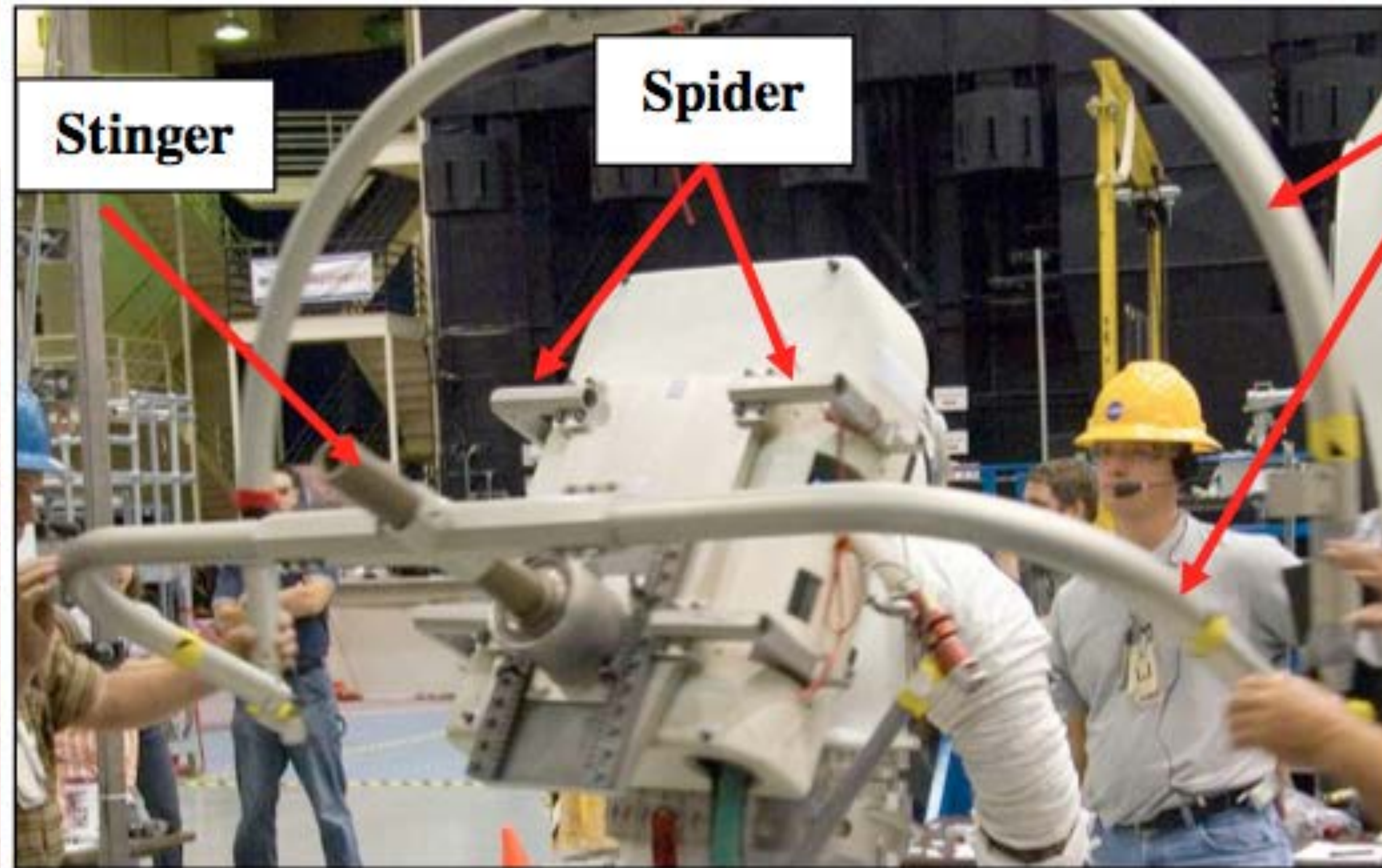


# Suited Partial-Gravity Suspension





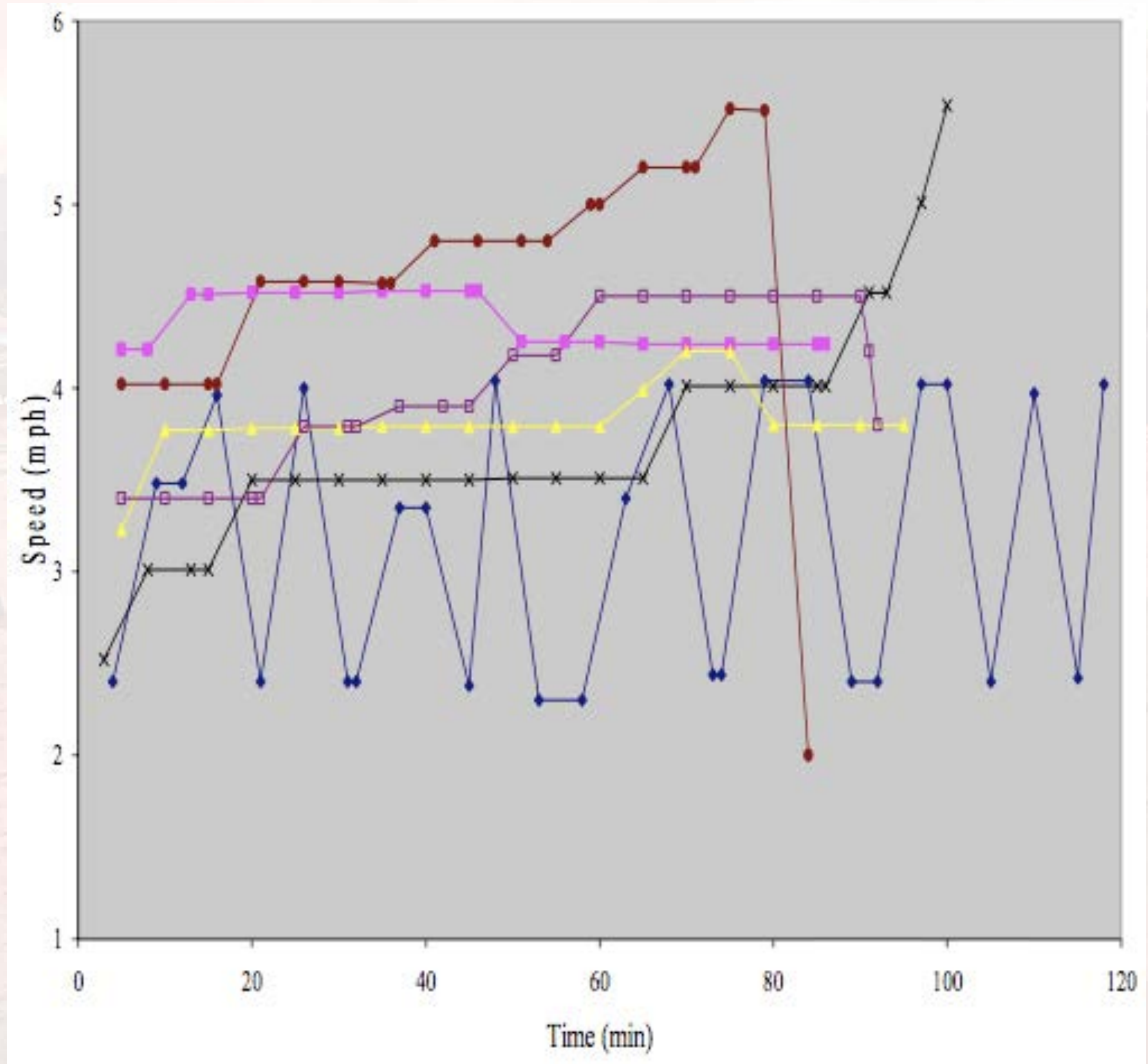
# Details of Gimbal Mount to Pogo System



**Gimbal Support Structure**

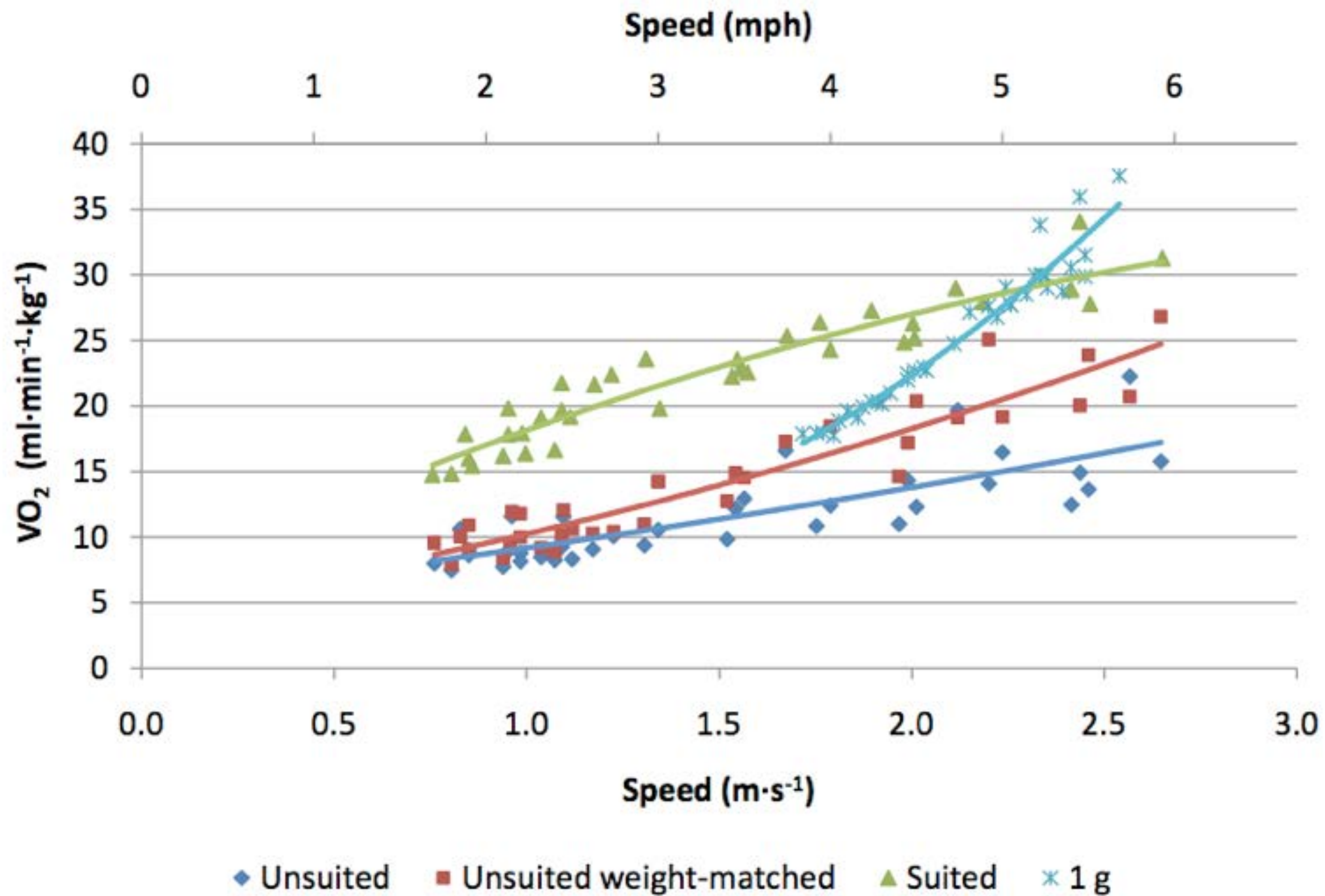


# Test Subject Performing 10 km Traverse



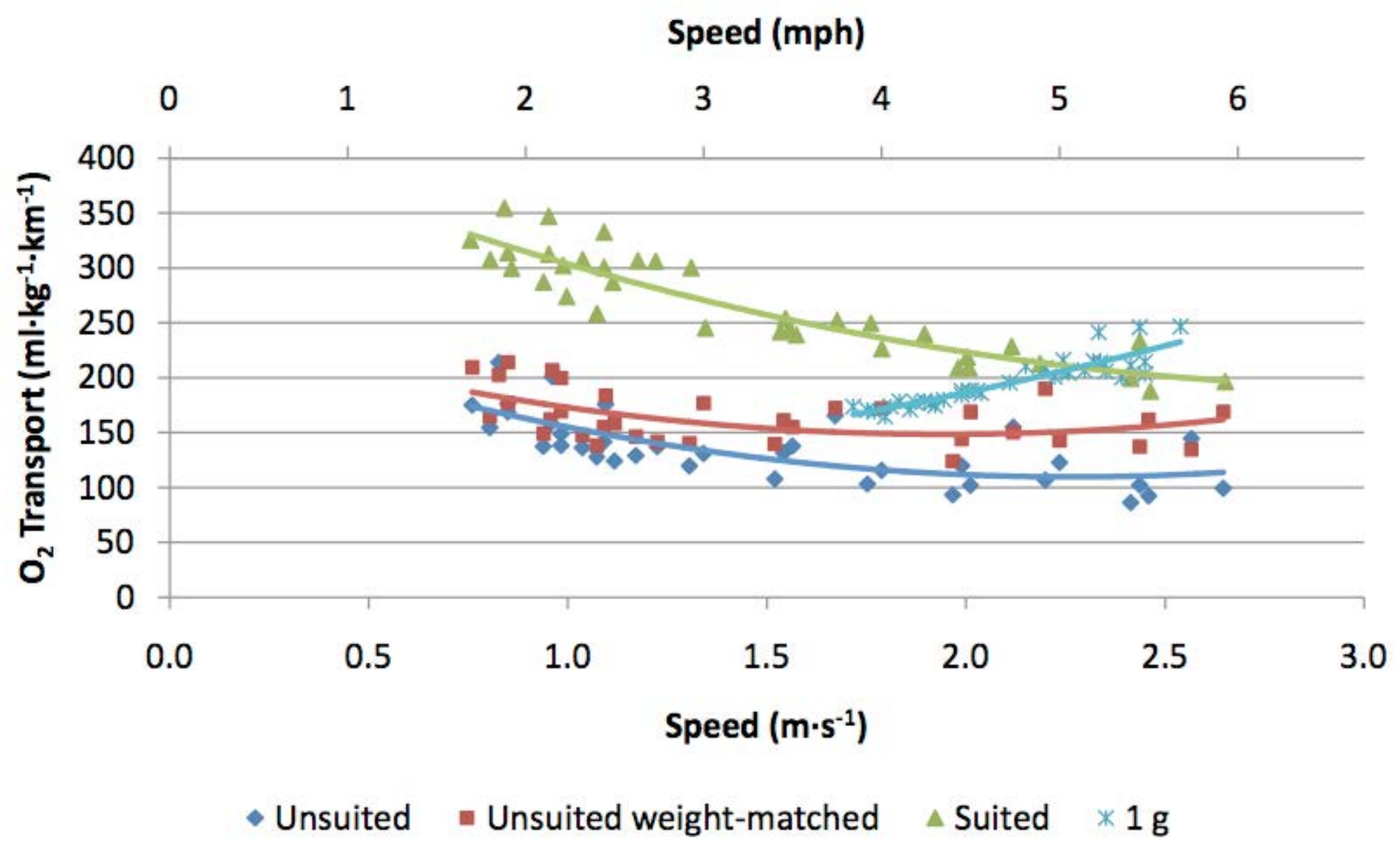


# Metabolic Costs of Lunar Locomotion



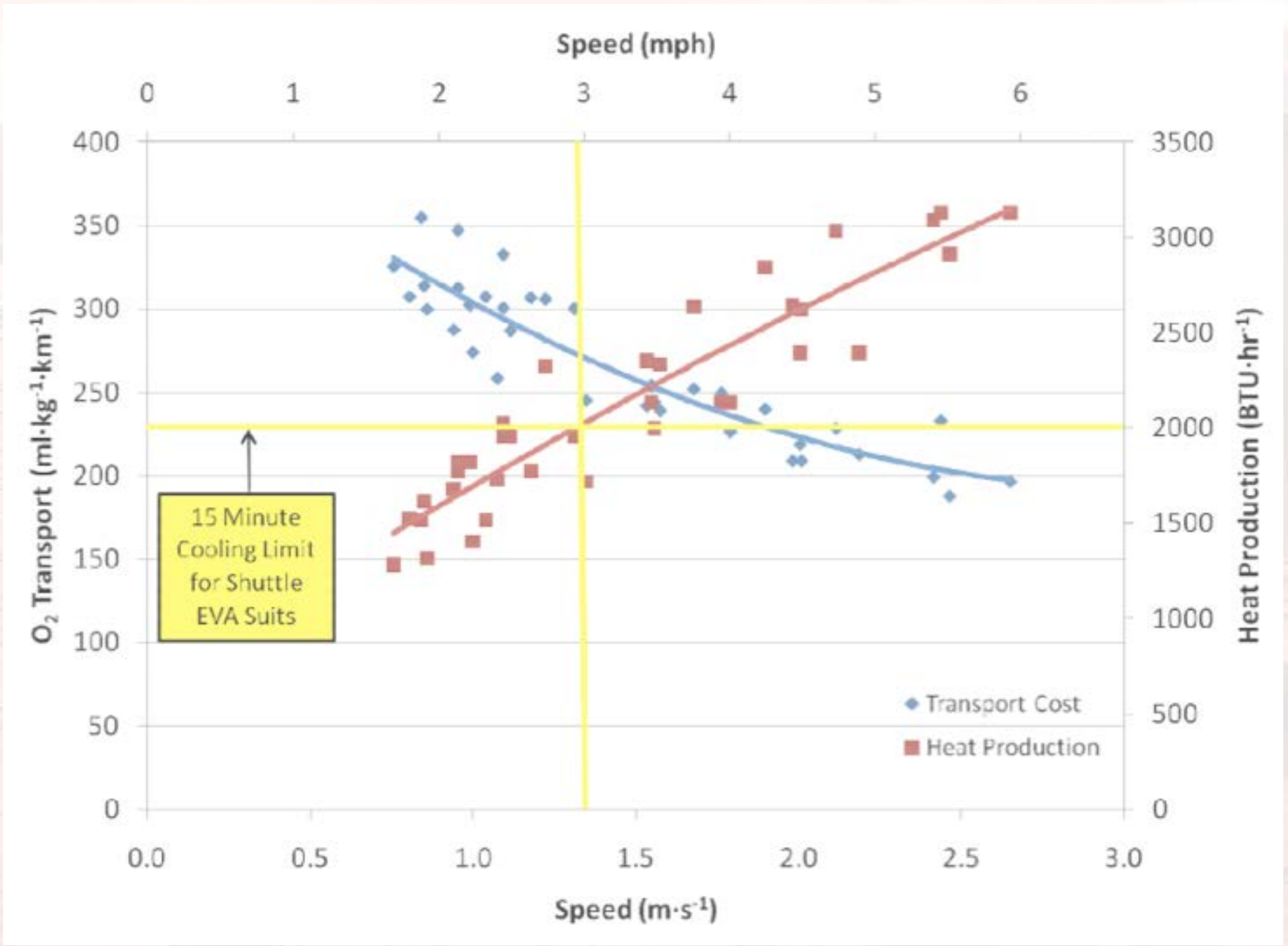


# O<sub>2</sub> Transport Cost of Lunar Locomotion





# Cooling and Energy Use in Lunar Run





# References for This Lecture

- Gernhardt, Norcross, and Vos, *Integrated Suit Test 1 - A Study to Evaluate Effects of Suit Weight, Pressure, and Kinematics on Human Performance During Lunar Ambulation* ICES 2008-01-1951, International Conference on Environmental Systems, San Francisco, CA, July 2008
- Vos, Gernhardt, and Lee, *The Walkback Test: A Study to Evaluate Suit and Life Support System Performance Requirements for a 10 Kilometer Lunar Traverse in a Planetary Suit* ICES 2007-01-3133, International Conference on Environmental Systems, Chicago, IL, July 2007
- Rader, Newman, and Carr, *Loping: A Strategy for Reduced Gravity Human Locomotion?* ICES 2007-01-3134, International Conference on Environmental Systems, Chicago, IL, July 2007